



# Systematic nuclear potential for stable, weakly bound and exotic nuclei reactions

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Dr. Juan Pablo Fernández García  
Dpto. Física Atómica Molecular y Nuclear  
Universidad de Sevilla

# The International Research Collaborators

## Argentina:

- Laboratorio Tandem - Comisión Nacional de Energía Atómica (CNEA)



## Brazil:

- Laboratorio Aberto de Física Nuclear (LAFN) – Universidade de São Paulo (IFUSP)



## Italy:

- Laboratori Nazionali del Sud (LNS) – Istituto Nazionale di Fisica Nucleare (INFN).
- Università degli Studi di Padova



## Spain:

- Universidad de Sevilla (US)
- Universidad de Huelva (UHU)



## Portugal:

- Faculty of Sciences of Lisbon (LIP)



## Mexico:

- Universidad Nacional Autónoma de México (UNAM)

## Costa Rica:

- Universidad de Costa Rica - CICANUM

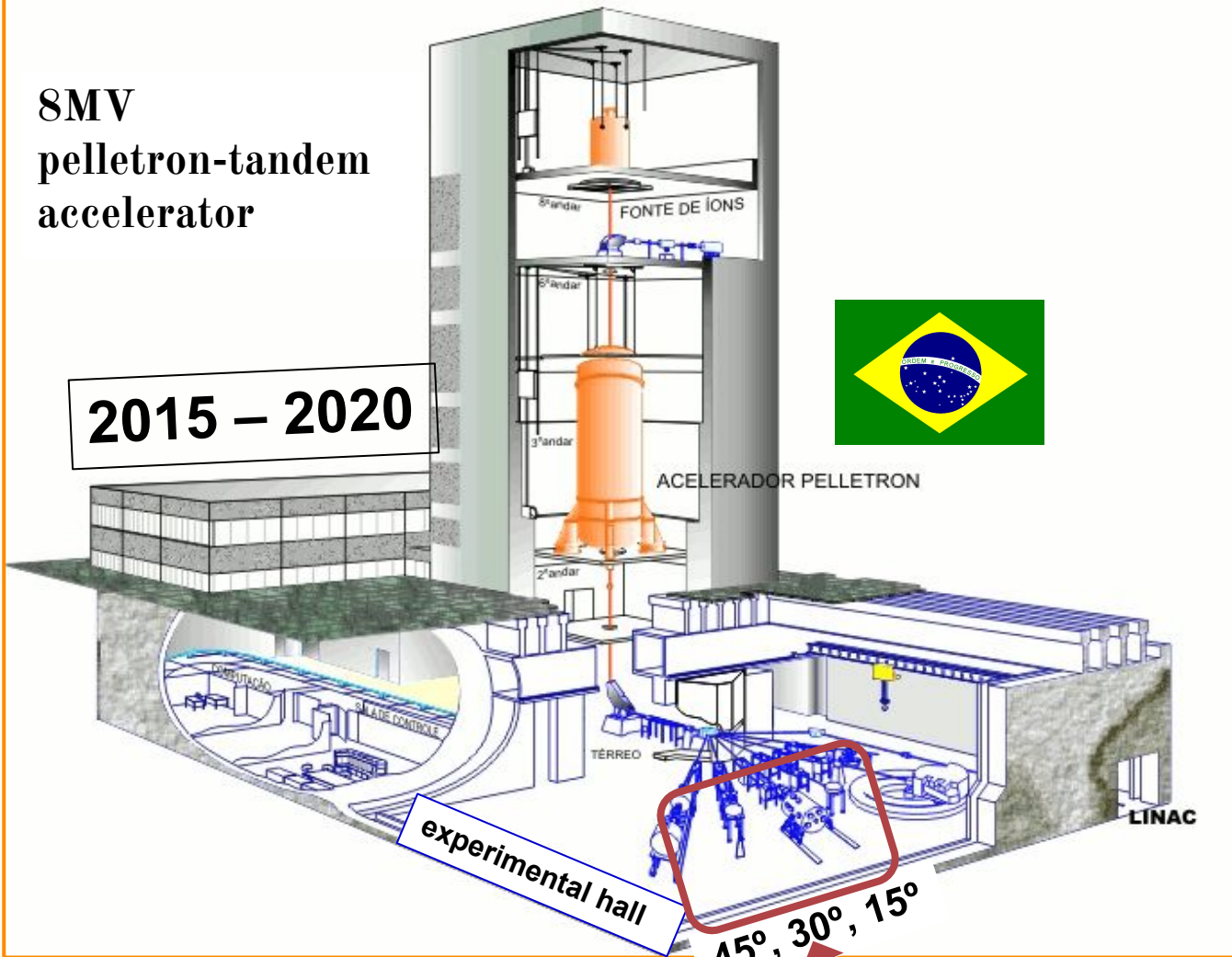


- 1. The Laboratories and SETUP's**
- 2. The Theoretical Optical Model**
- 3. Experimental Data x Theoretical Calculations**
- 4. Conclusions**

1. **The Laboratories and SETUP's**
2. **The Theoretical Optical Model**
3. **Experimental Data x Theoretical Calculations**
4. **Conclusions**

8MV  
pelletron-tandem  
accelerator

2015 – 2020



30B beam line

## ❑ Open Laboratory of Nuclear Physics

Experimental hall is divided into  
two rooms: A and B

Room B: 3 experimental beam lines  
15B; 30B and 45B (RIBRAS)

Goals:

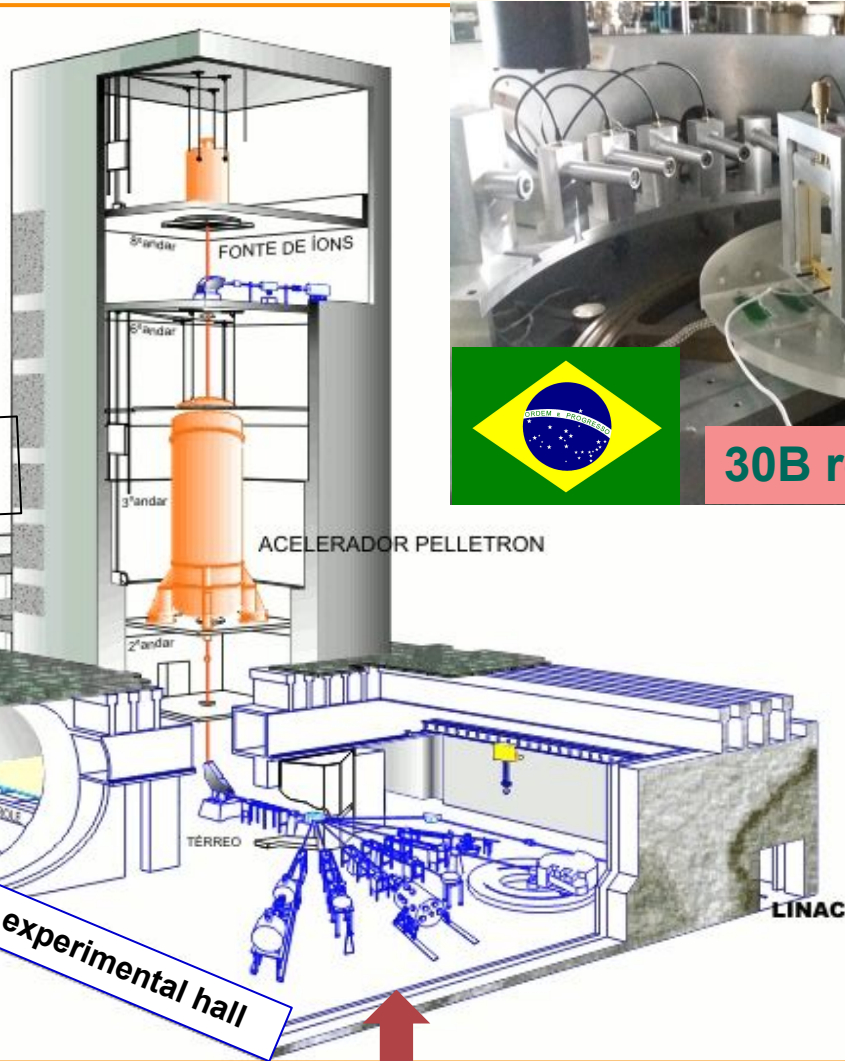


- Permanent dedicated setup
- Long term experimental campaigns

- ✓ beam time availability
- ✓ good statistics
- ✓ precise new data

# SMV pelletron-tandem accelerator

2015 – 2020



30B reaction chamber

- Permanent dedicated setup
- Long term experimental campaigns

- $^{6,7}\text{Li} + ^{120}\text{Sn}, ^{197}\text{Au}$  (2017)
- $^{10,11}\text{B} + ^{120}\text{Sn}, ^{197}\text{Au}$  (2018-9)
- $^{12,13}\text{C} + ^{120}\text{Sn}, ^{197}\text{Au}$  (2020)

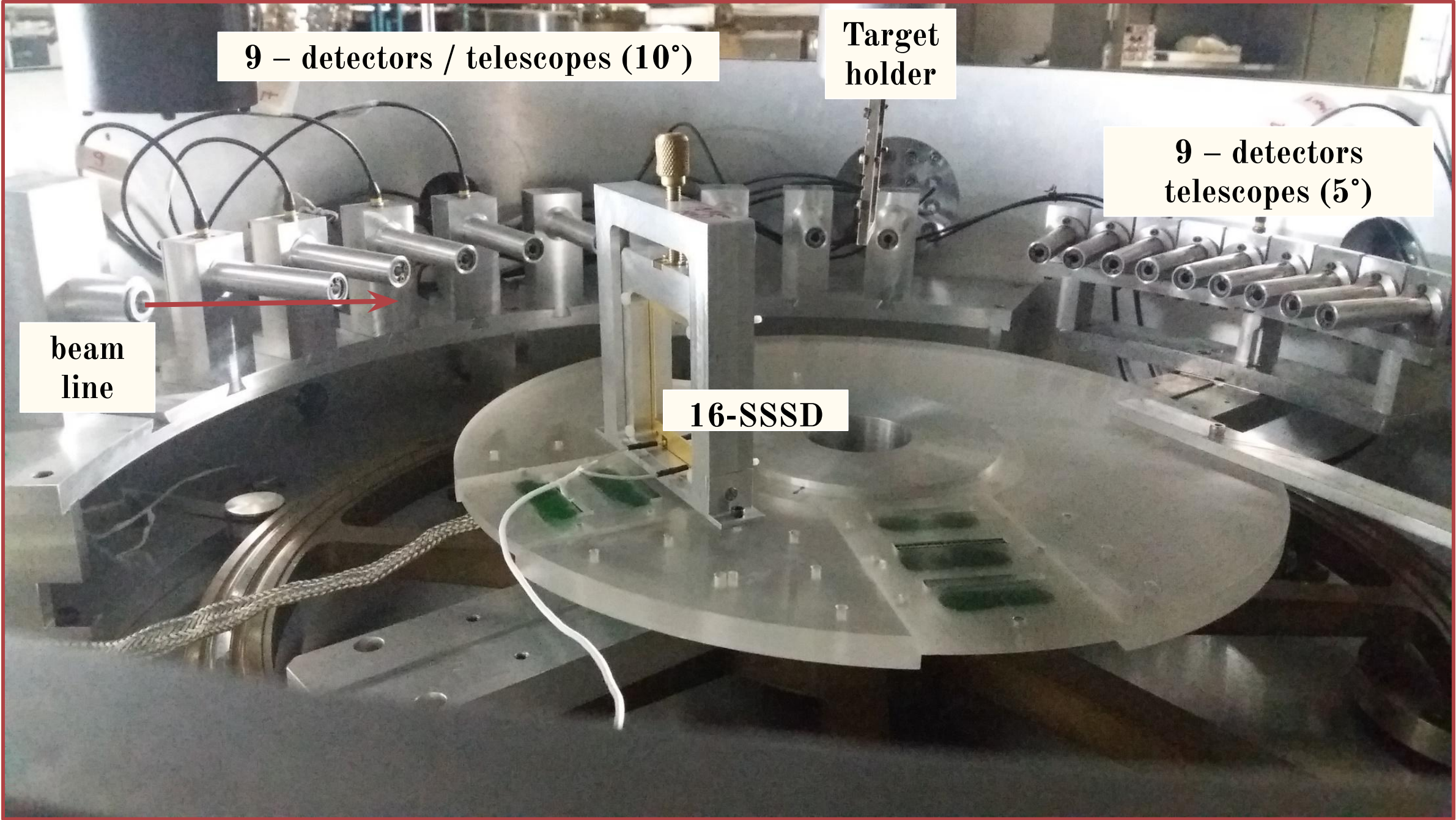
## Local Research Team:

- Leandro Gasques
- Luiz Carlos Chamon
- Alinka Lèpine
- Valdir Scarduelli
- Vinicius Zagatto
- José Roberto Brandão

## Theoretical Support:

- University of Seville (US) (M. R. Gallardo)
- Università degli Studi di Padova (J. Casal)

30B beam line



9 - detectors / telescopes (10°)

Target holder

9 - detectors telescopes (5°)

beam line

16-SSSD

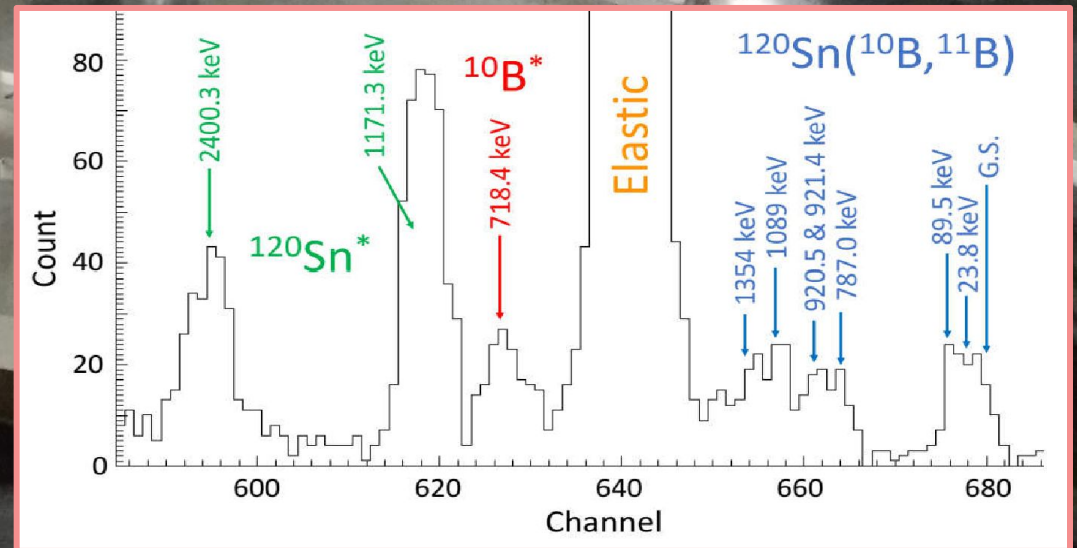
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Target holder

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beam  
line

16-SSSD





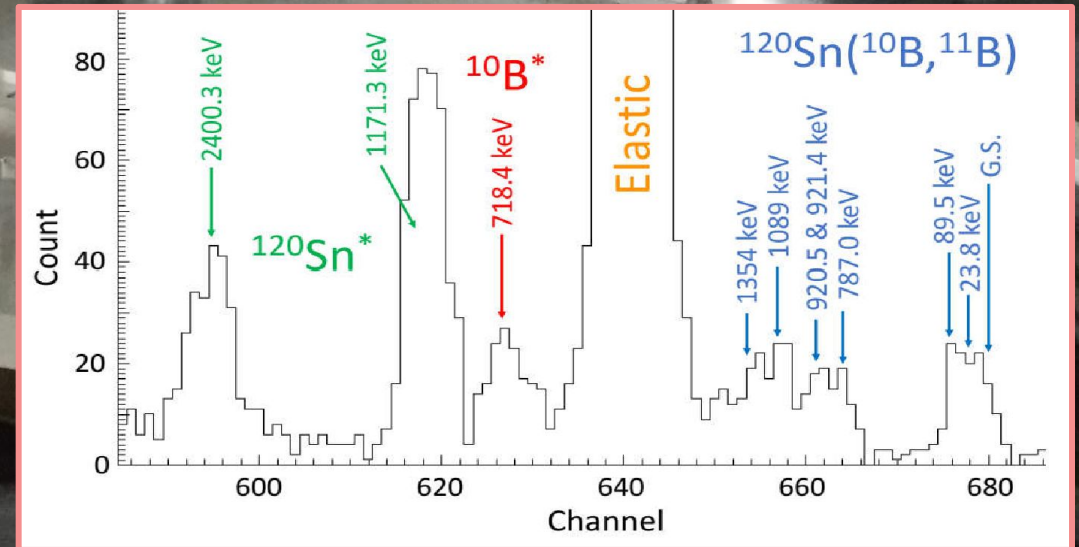
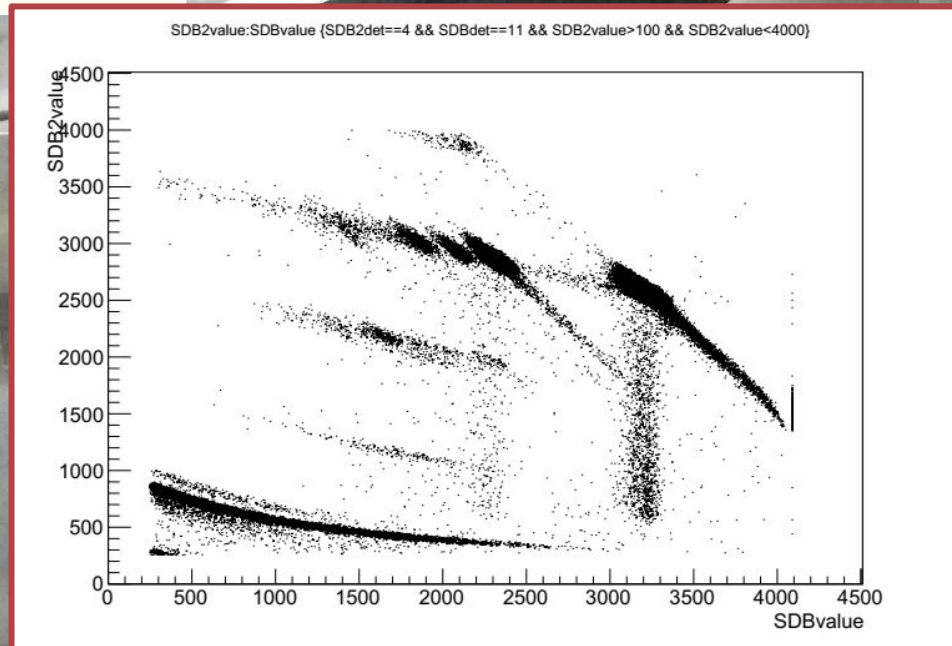
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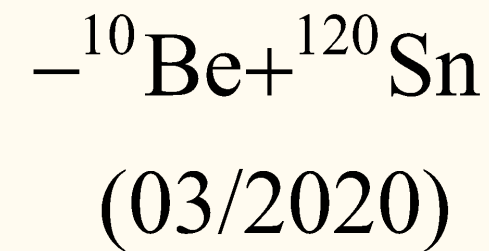
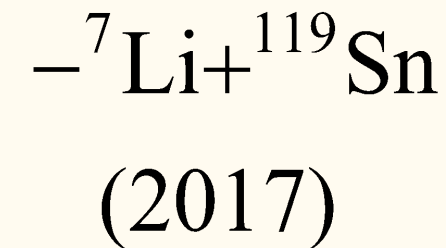
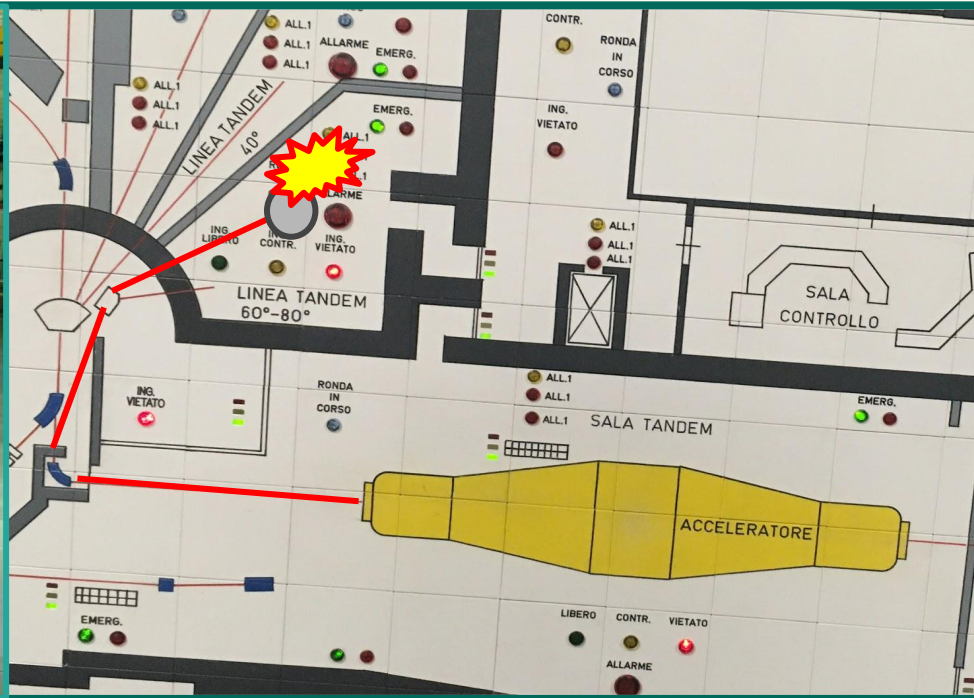
beam line

16-SSSD





14MV  
pelletron-tandem  
accelerator



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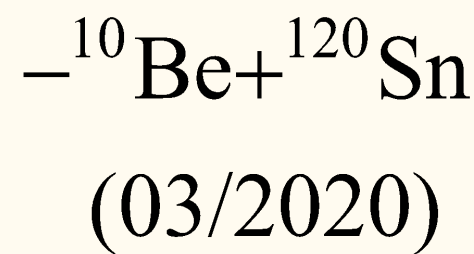
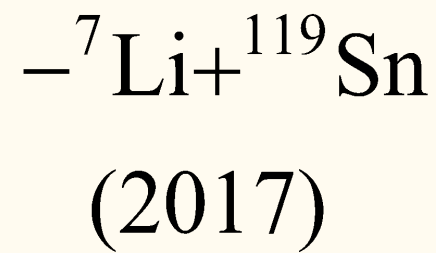
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- D. Torresi
- M. La Cognata

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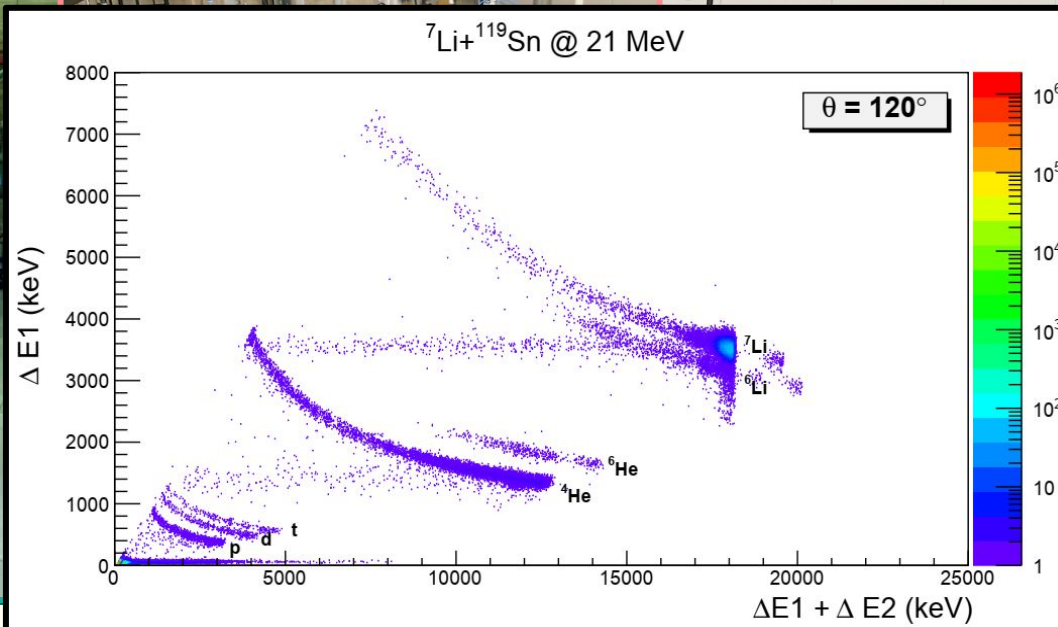
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${}^7\text{Li} + {}^{119}\text{Sn}$   
(2017)

${}^{10}\text{Be} + {}^{120}\text{Sn}$   
(03/2020)



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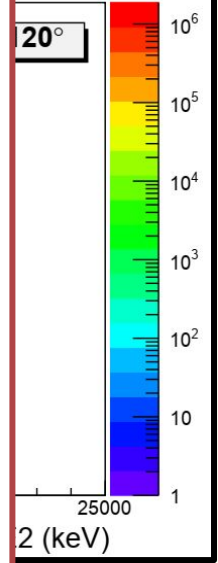
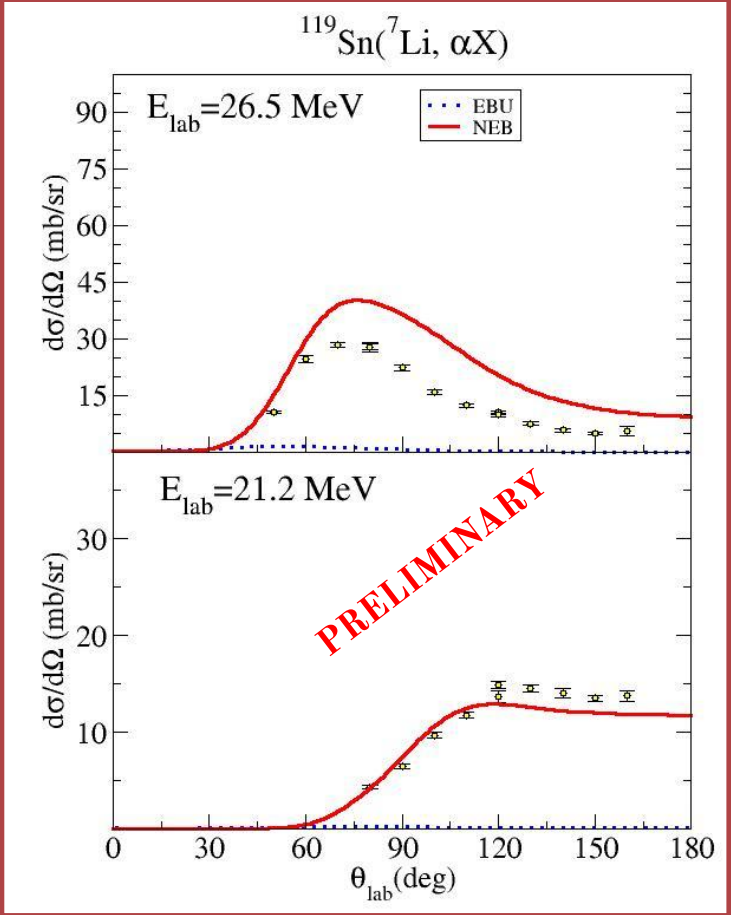
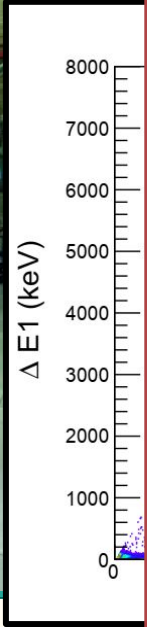
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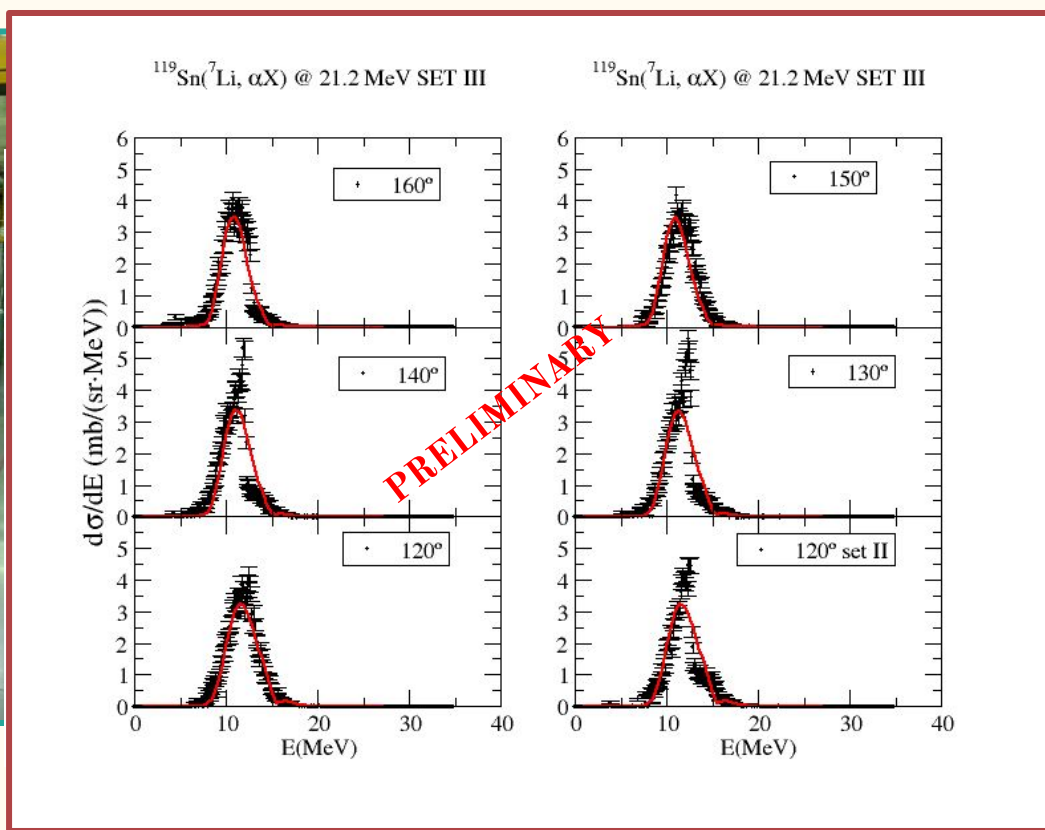


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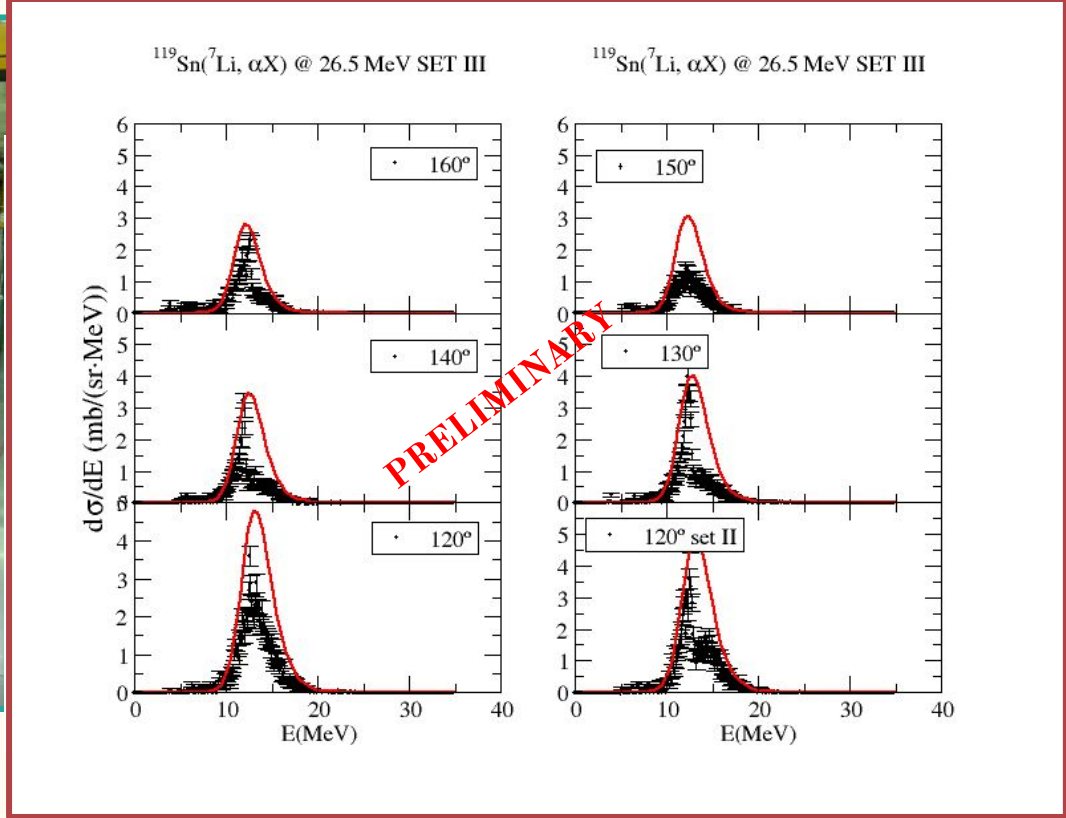
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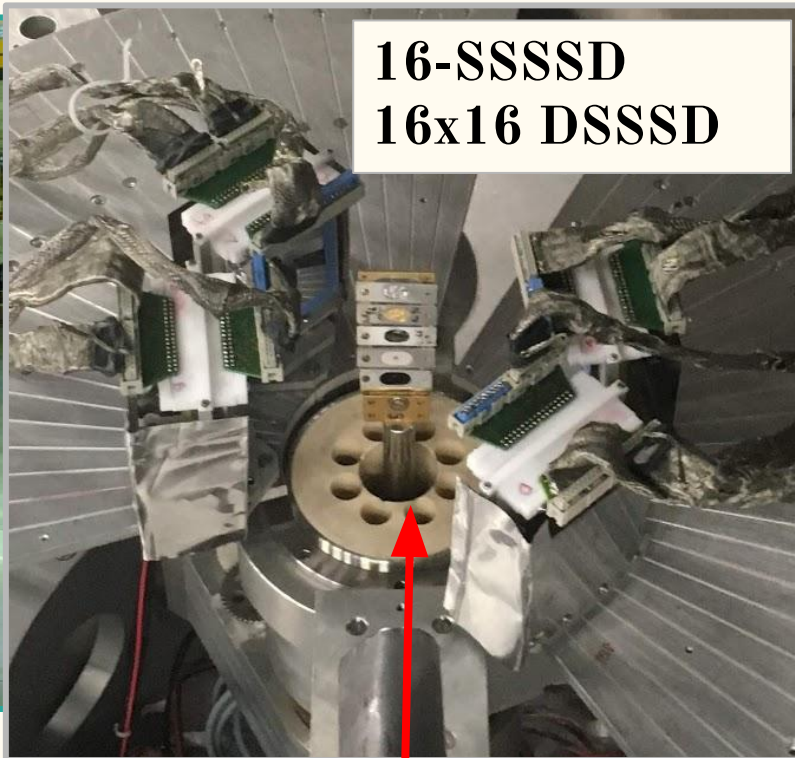
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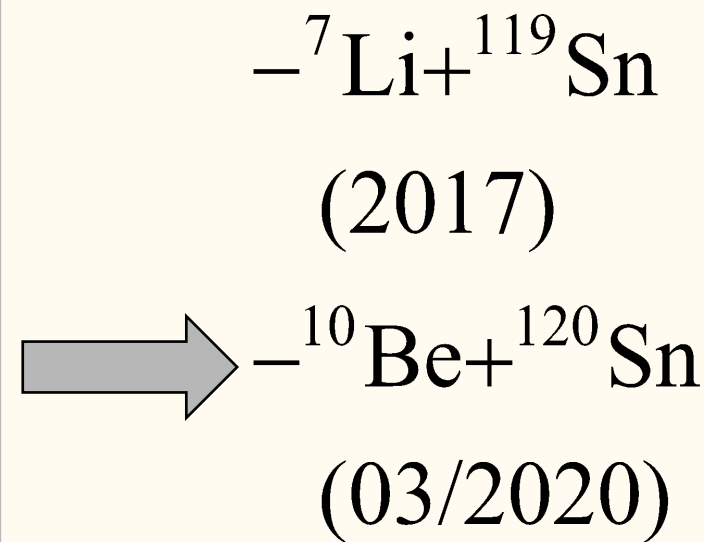
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16-SSSSD  
16x16 DSSSD



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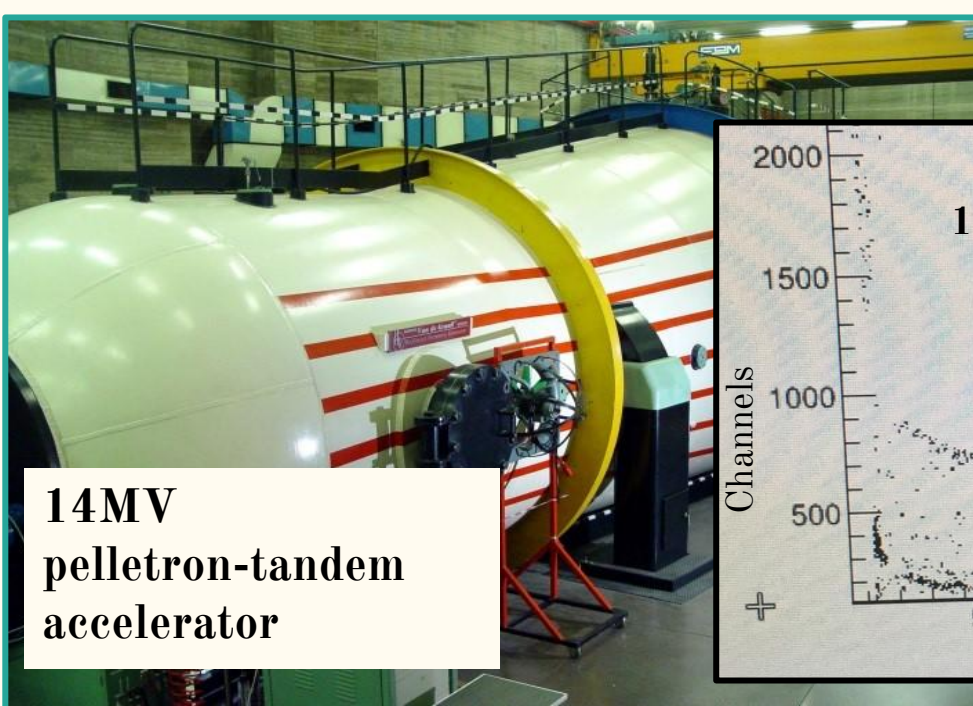


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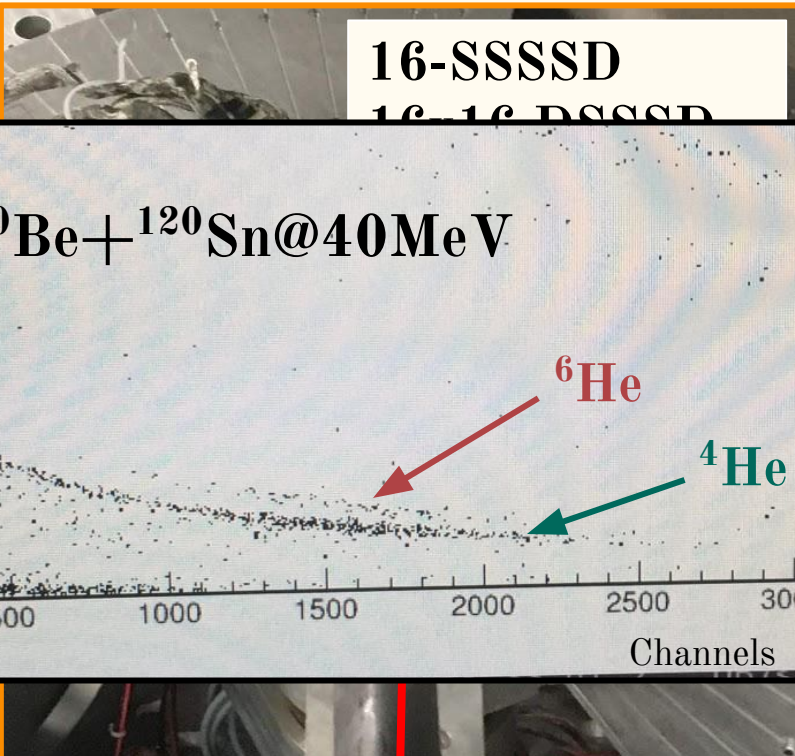
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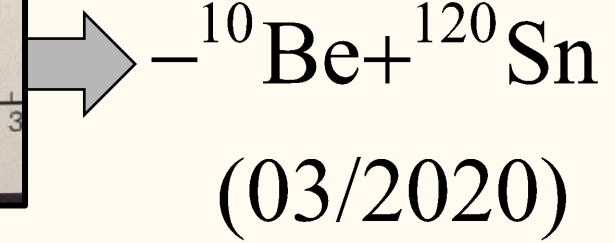
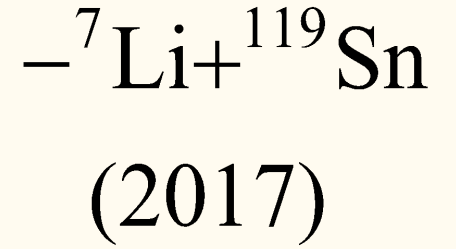
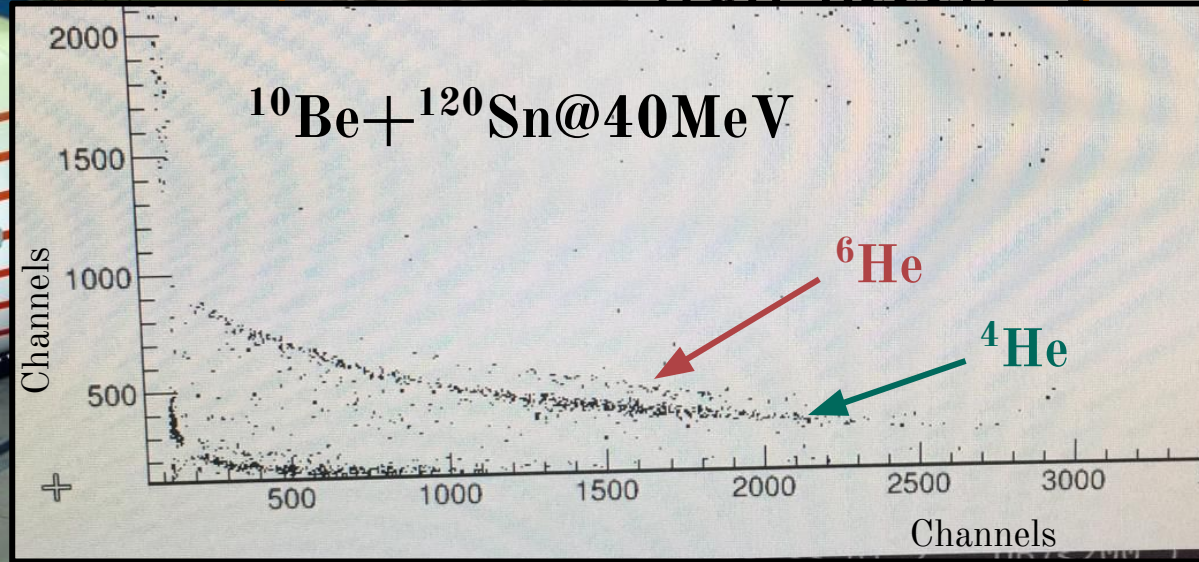




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16-SSSSD



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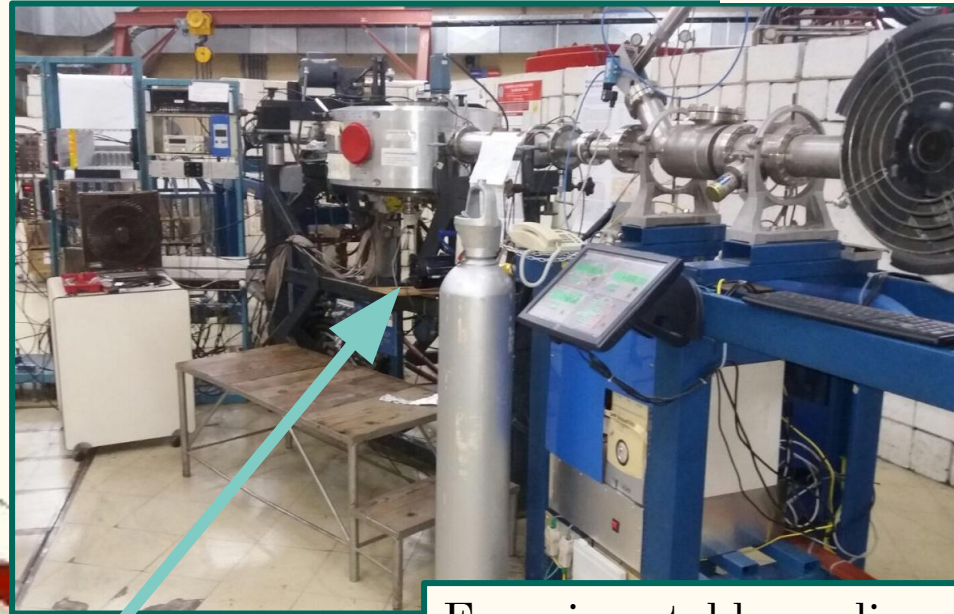
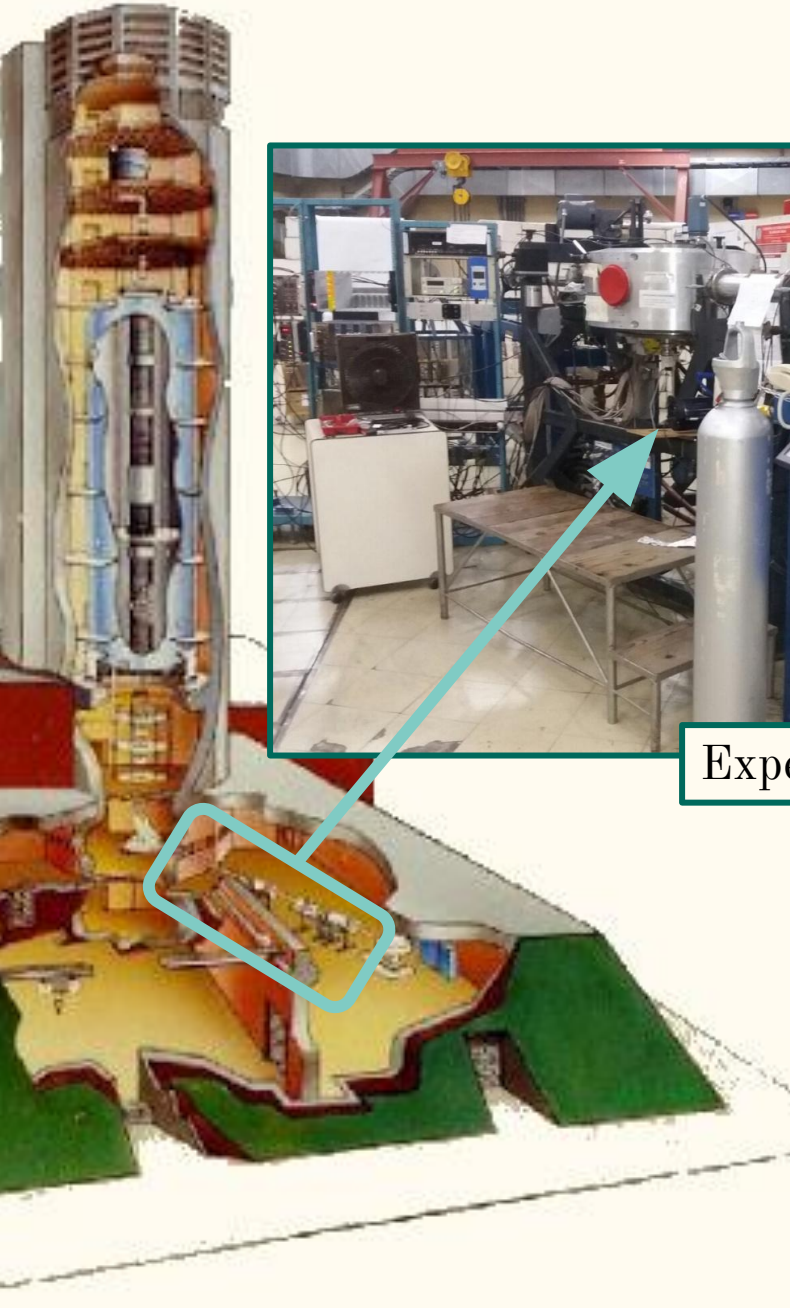
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Comisión Nacional  
de Energía Atómica

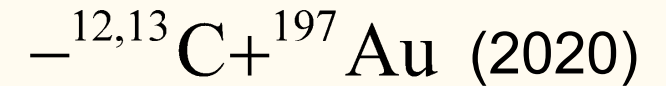
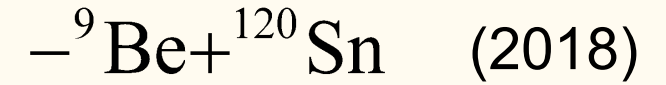


**20MV  
pelletron-tandem  
accelerator**



Experimental beam line

- ❑ Permanent dedicated setup
- ❑ Long term experimental campaigns



**Local Research Team:**

- ❑ Daniel Abriola
- ❑ Andrés Arazi
- ❑ Daniel Hojman
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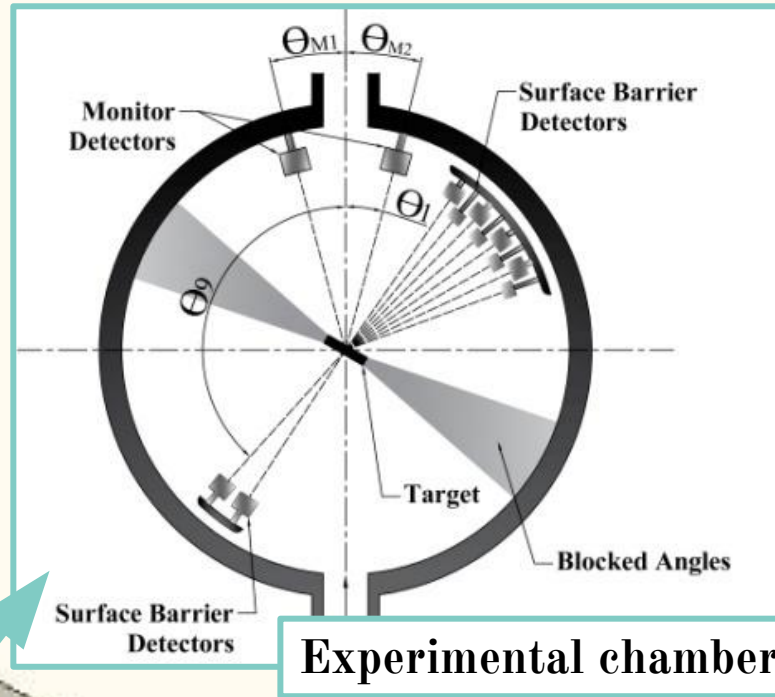
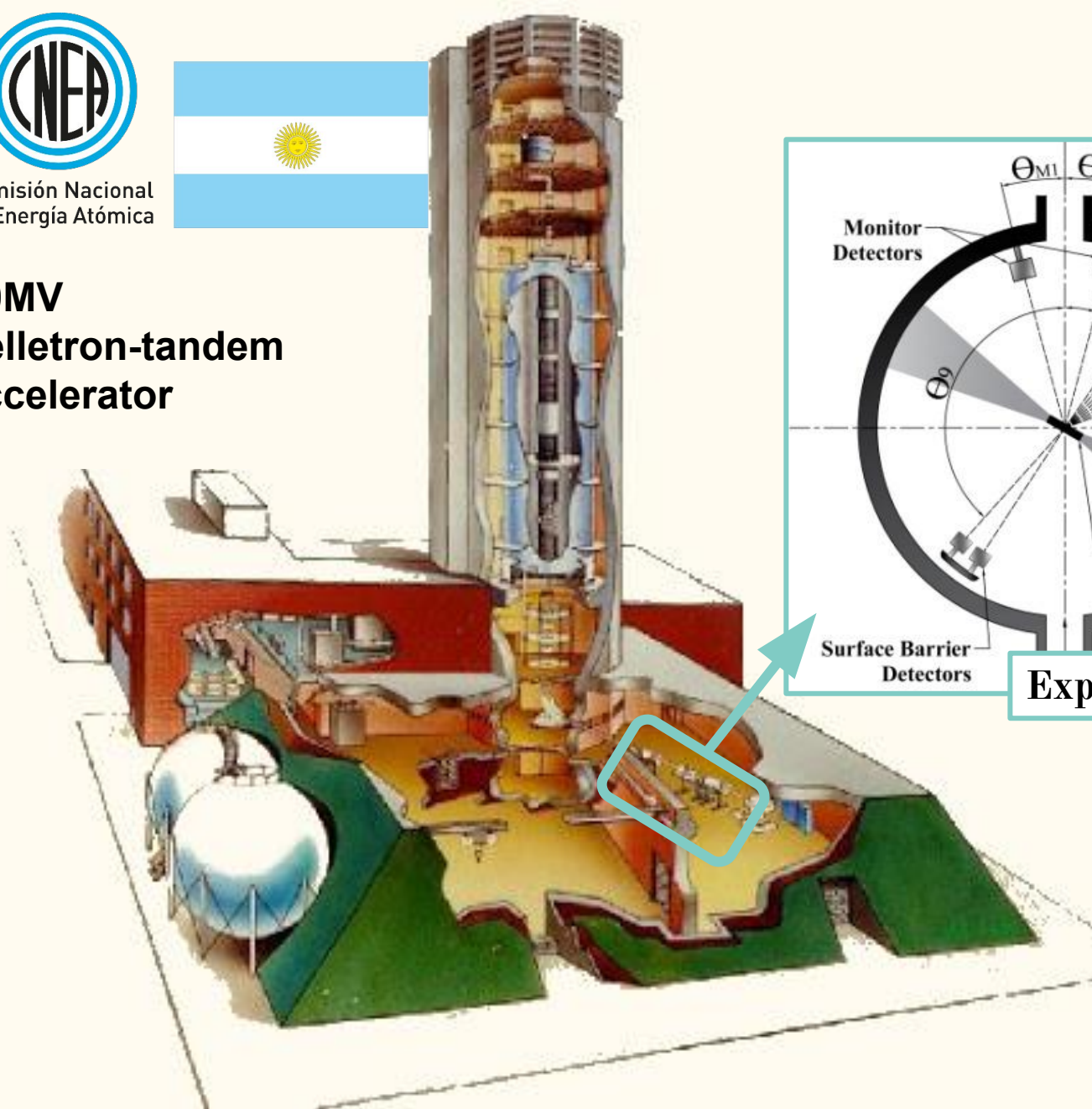
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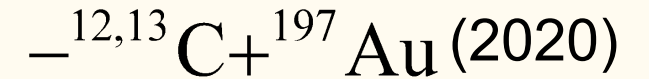


Comisión Nacional de Energía Atómica

20MV pelletron-tandem accelerator



- Permanent dedicated setup
- Long term experimental campaigns



Local Research Team:

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Theoretical Support:

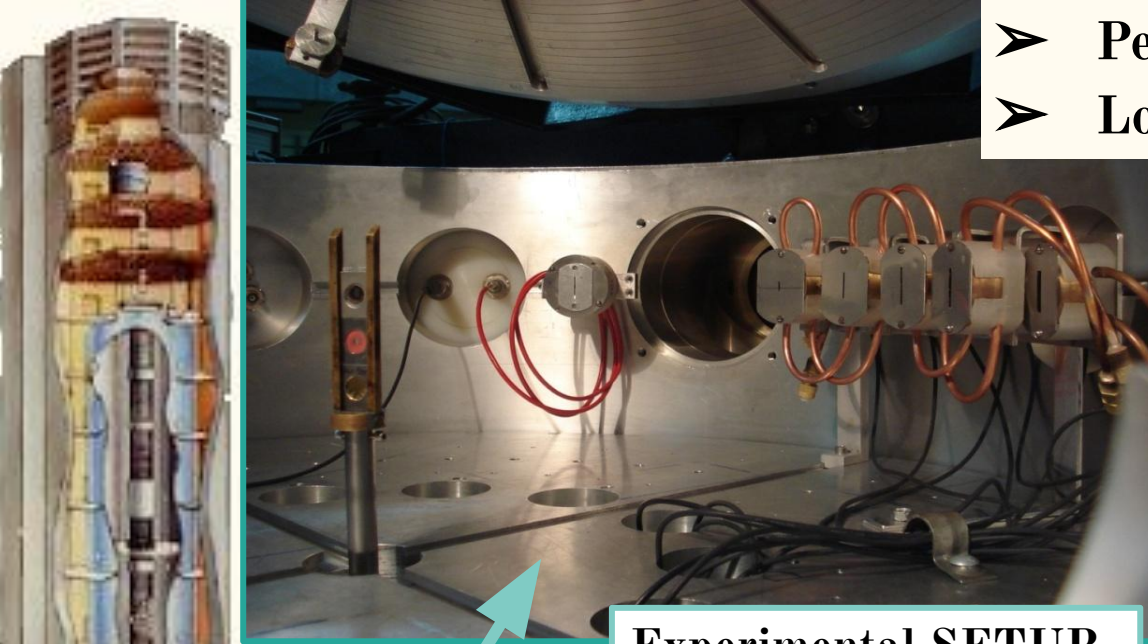
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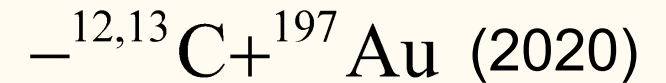


**20MV  
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**Experimental SETUP**

- Permanent dedicated setup
- Long term experimental campaigns



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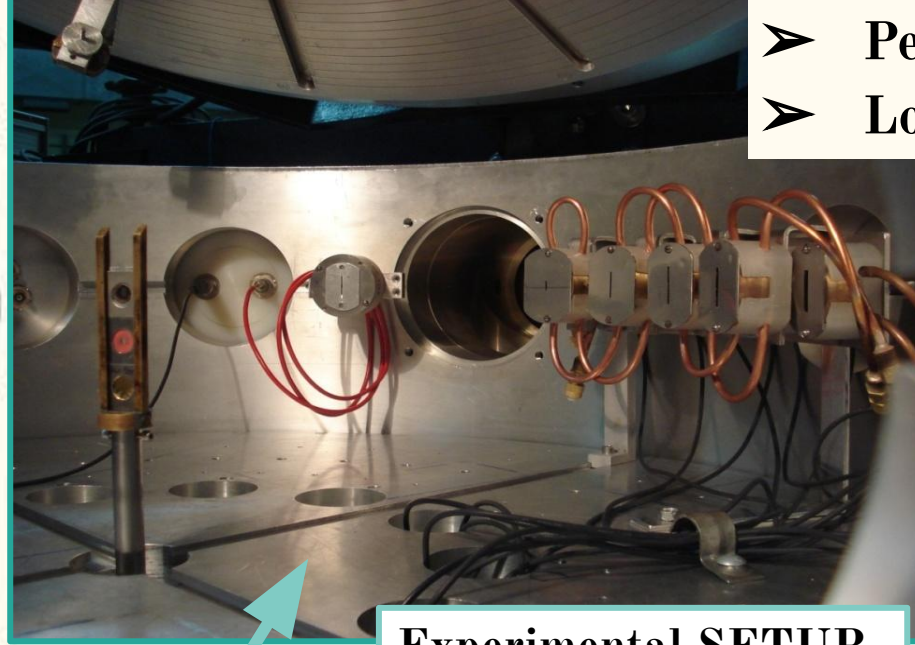
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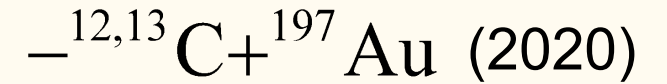
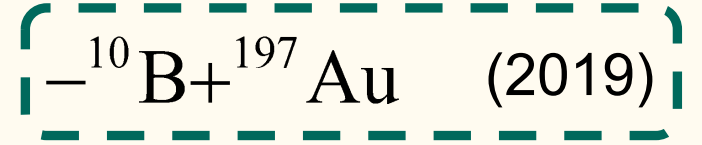


Comisión Nacional de Energía Atómica



Experimental SETUP

- Permanent dedicated setup
- Long term experimental campaigns



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- ELASTIC SCATTERING
- INELASTIC EXCITATION
- NUCLEON TRANSFER  
L. Gasques *et al.* PRC101 (4), 044604 (2020)
- FUSION  
M. Aversa *et al.*, PRC101 (4), 044601 (2020)

Theoretical Support:

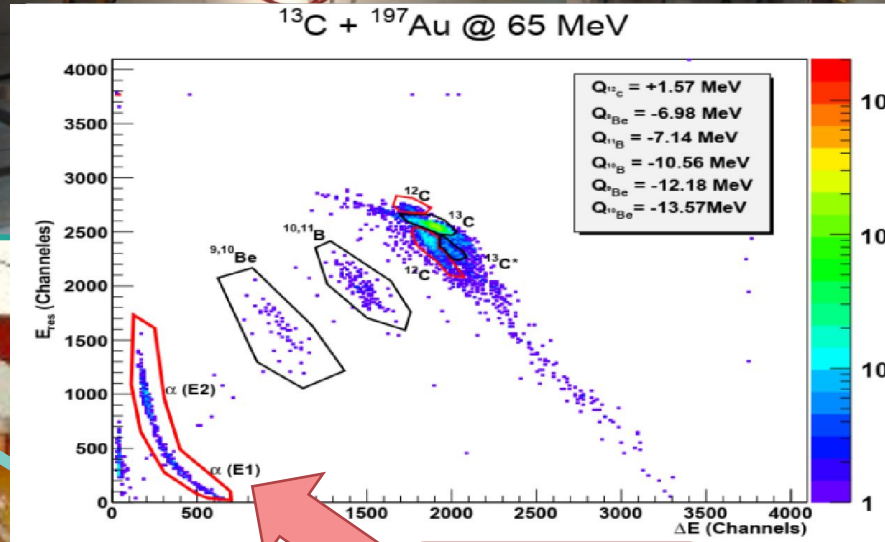
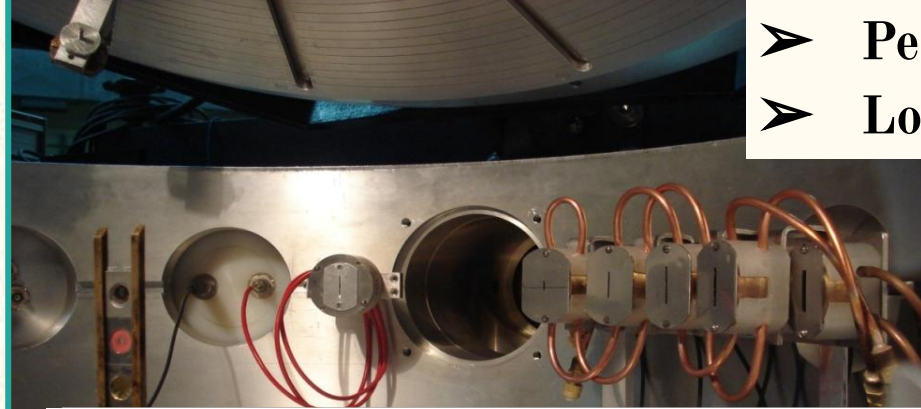
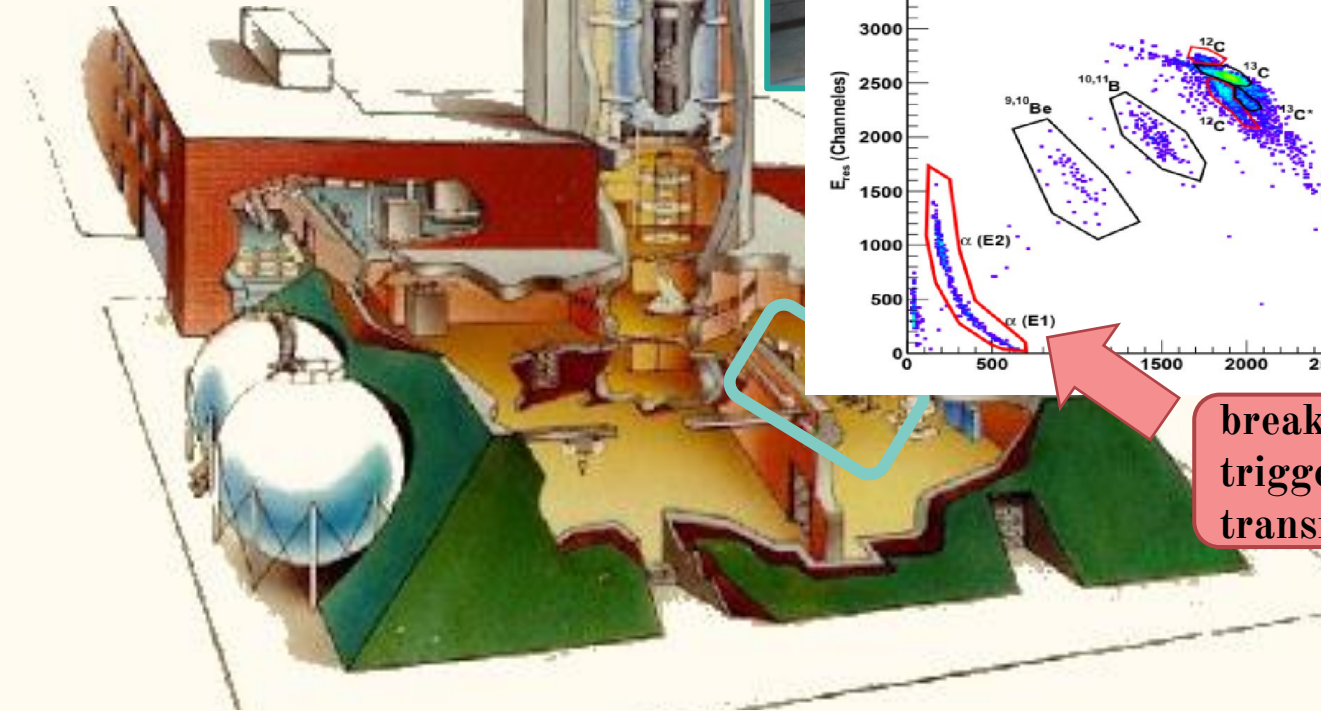
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${}^{10}\text{B} + {}^{197}\text{Au}$  @ 38, 40, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 61 MeV



Comisión Nacional de Energía Atómica

**20MV  
pelletron-tandem  
accelerator**



break up  
triggered by  
transfer

- Permanent dedicated setup
- Long term experimental campaigns



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$^{13}\text{C} + ^{197}\text{Au}$  @ 60, 65 and 70 MeV (2018)

## **FROM AN EXPERIMENTAL POINT OF VIEW**

**We have four main TOOLS:**

- 1. Access to the facilities.**
- 2. High beam intensities.**
- 3. Permanent/dedicated experimental setups.**
- 4. Long term experimental campaigns.**

**RECENT GOOD EXPERIMENTAL DATA ARE AVAILABLE**

- 1. The Laboratories and SETUP's**
- 2. The Theoretical Optical Model**
- 3. Experimental Data x Theoretical Calculations**
- 4. Conclusions**



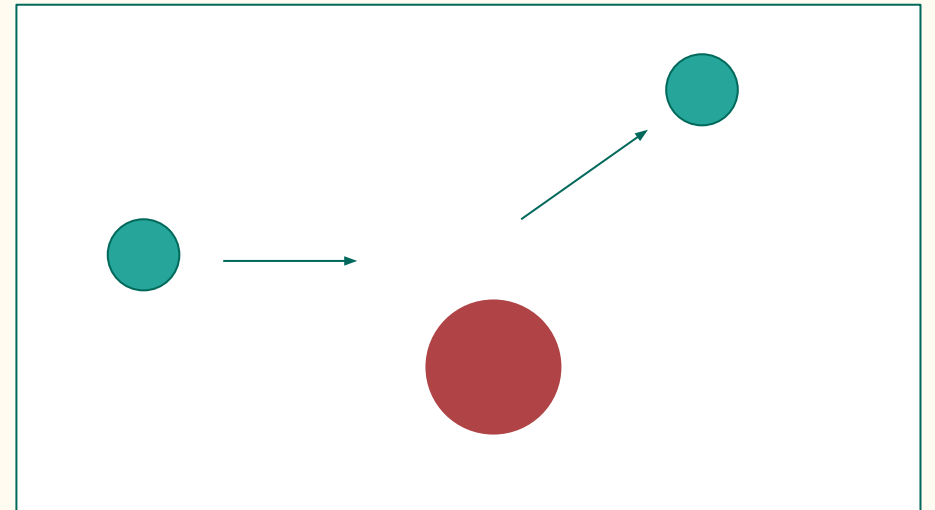
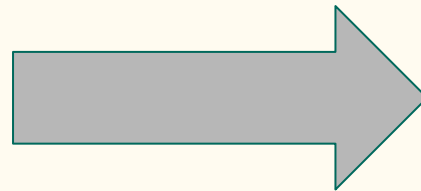
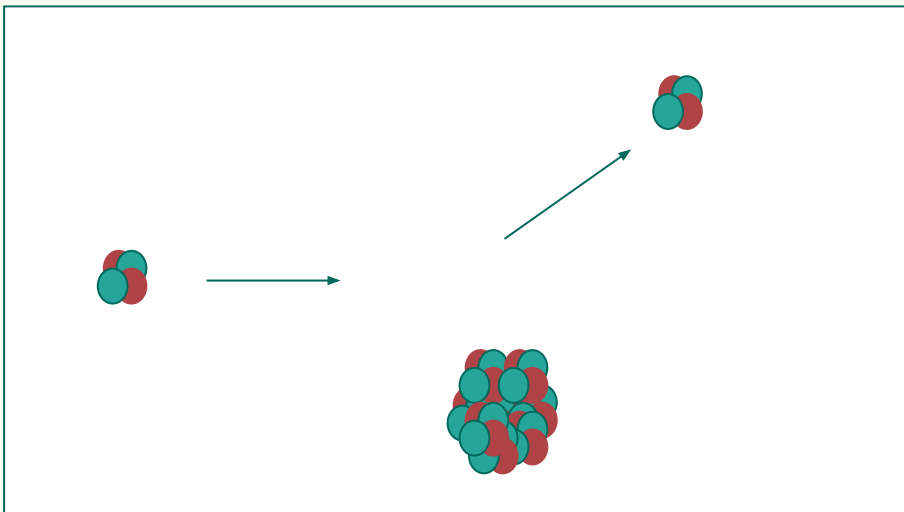
## GOALS:

- ✓ How the weakly (**stable or exotic**) bound structures affect the dynamics of nuclei reactions?
- ✓ May theoretical models developed to study stable nuclei be applied to weakly bound & exotic ones?

## CONCEPTS:

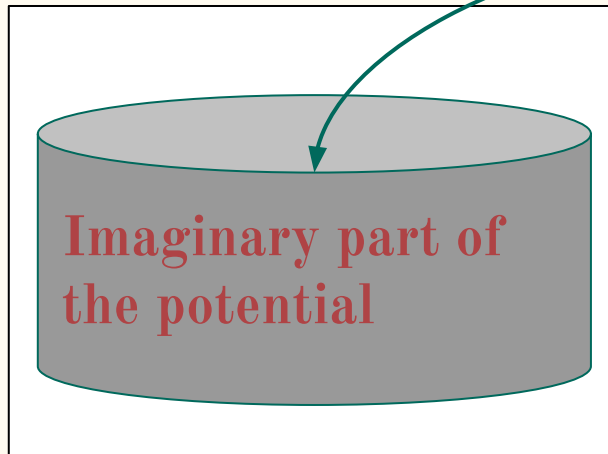
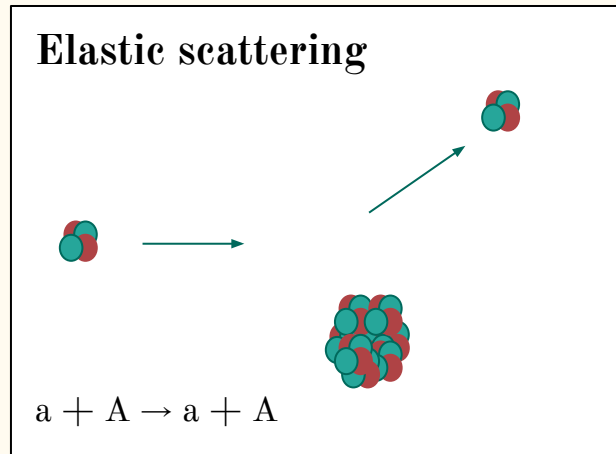
- ❑ The **elastic scattering** is the simplest process to test a **theoretical model**.
- ❑ The **optical model (OM)** is the most used theoretical approach for the corresponding **DATA** analysis.

$$U_N(R, E) \approx U_{opt}(R) = V(R) + iW(R)$$



# Optical Model

The imaginary part of the nuclear potential represents the absorption of the elastic channel.



- Inelastic scattering
- Transfer reaction
- Breakup reaction
- Knock-out reaction
- Pick-up reaction
- Fusion

$$U_N(R, E) \approx U_{opt}(R) = V(R) + iW(R)$$



# Double-folding nuclear São Paulo potential (SPP).

$$-\frac{\hbar^2}{2\mu} \nabla^2 \Psi(R) + U(R, E) \Psi(R) = E \Psi(R)$$

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# Double-folding nuclear São Paulo potential (SPP).

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$$U(R, E) \approx U_N(R) + V_{Coul}(R) \approx U_{opt}(R) + V_{Coul}(R)$$

$$U_{opt}(R) = \underbrace{V_{bare}(R) + V_{pol}(R)}_{\text{real potential}} + \underbrace{i W_{pol}(R)}_{\text{imaginary potential}}$$

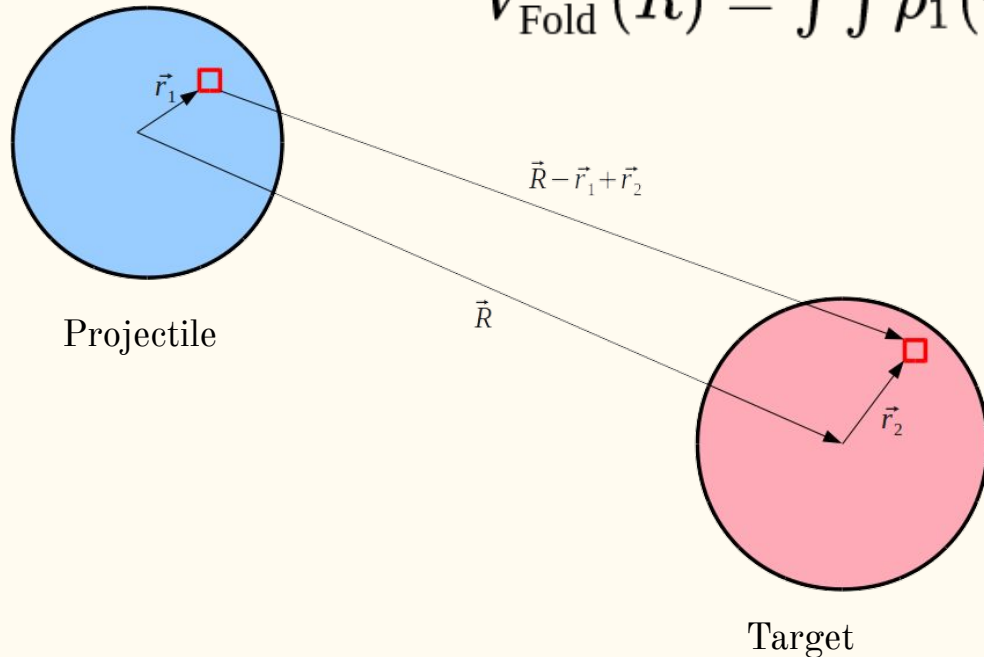
$$U_{opt}(R) = \underbrace{N_R V_{SPP}(R)}_{\text{real potential}} + \underbrace{N_i V_{SPP}(R)}_{\text{imaginary potential}}$$

# Double-folding nuclear São Paulo potential (SPP).

$$U_{opt}(R) = N_R V_{SPP}(R) + N_i V_{SPP}(R)$$

$$V_{SPP}(R) = V_{Fold}(R) e^{-4v^2/c^2}$$

$$V_{Fold}(R) = \int \int \rho_1(\vec{r}_1) \rho_2(\vec{r}_2) \nu_{NN}(\vec{R} - \vec{r}_1 + \vec{r}_2) d\vec{r}_1 d\vec{r}_2$$



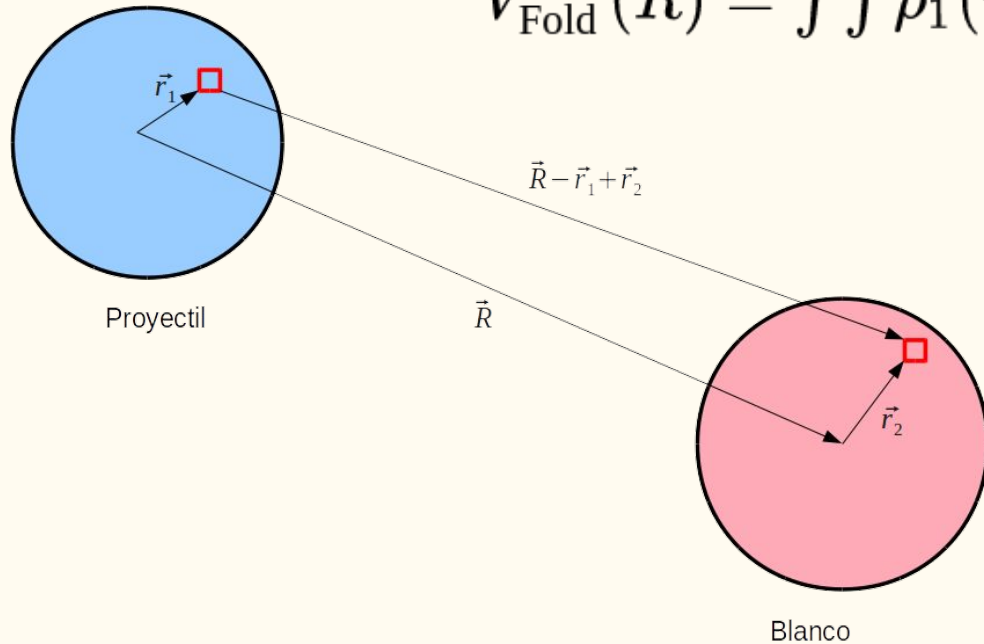
**Zero-range interaction:**  $\nu_{NN} = V_0 \delta(\vec{R} - \vec{r}_1 + \vec{r}_2)$   
 The NN interaction range is negligible compared to nuclear density  
 $V_0 = -456 \text{ MeV fm}^3$  [1]

# Double-folding nuclear São Paulo potential (SPP).

$$U_{opt}(R) = N_R V_{SPP}(R) + N_i V_{SPP}(R)$$

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**Zero-range interaction:**

The NN interaction range is negligible compared to nuclear density

$$\nu_{NN} = V_0 \delta(\vec{R} - \vec{r}_1 + \vec{r}_2)$$

$$V_0 = -456 \text{ MeV fm}^3 [1]$$

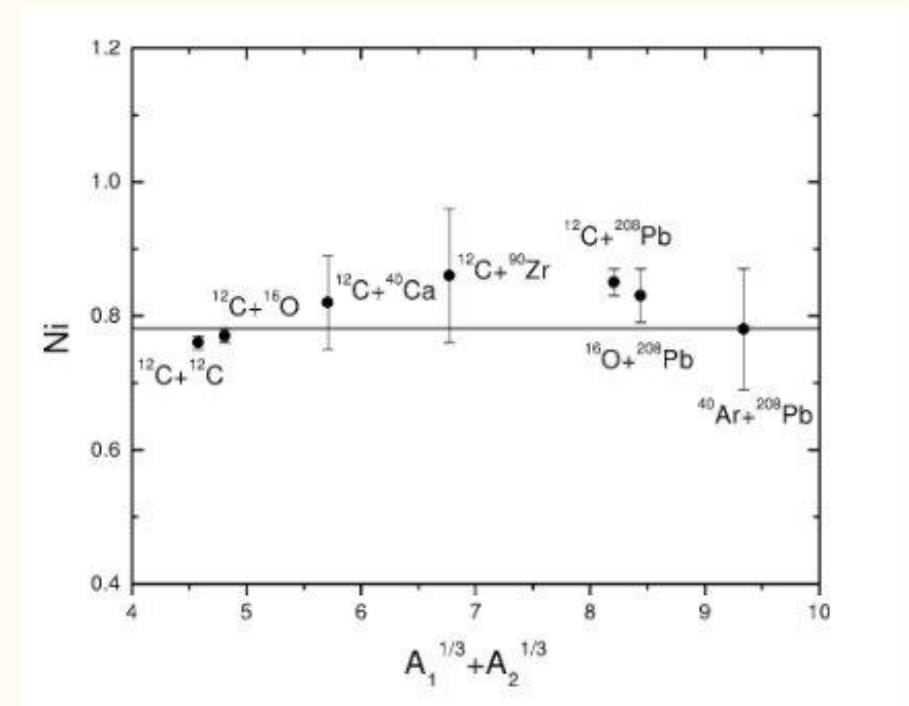
# Double-folding nuclear São Paulo potential (SPP).

$$U_{opt}(R) = V_{SPP}(R) + iN_I V_{SPP}(R) + V_{pol}(R) + iW_{pol}(R)$$

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Stable nuclei reactions have been successfully described assuming the fundamental double-folding nuclear São Paulo potential (SPP).



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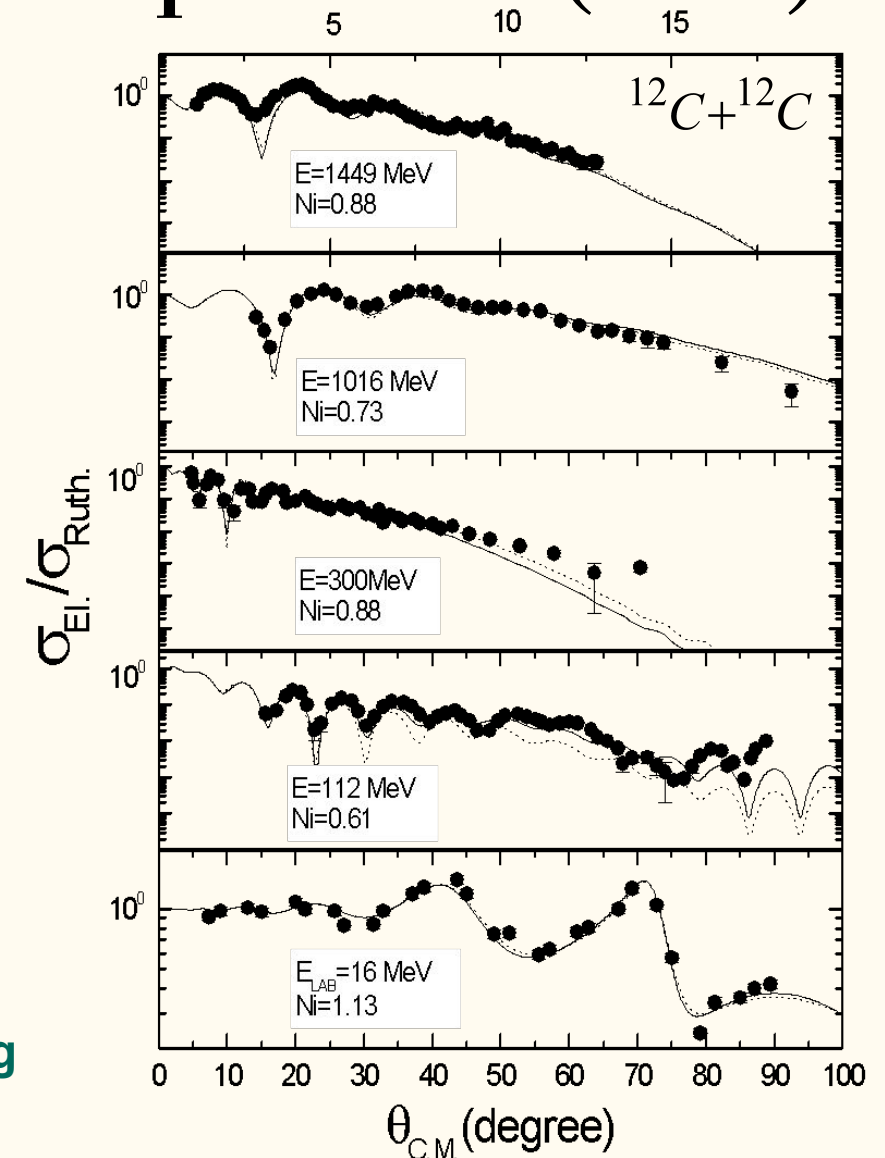
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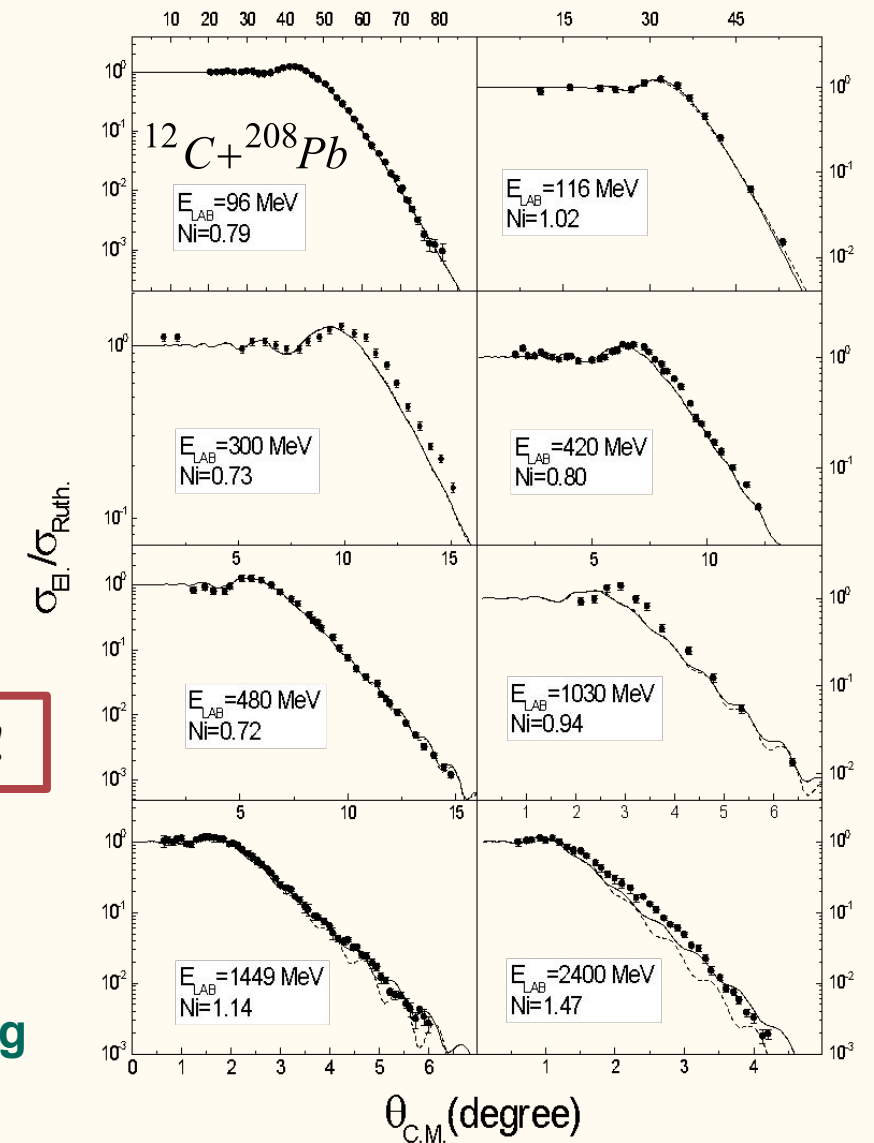
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Reproduce more than 40 systems!!

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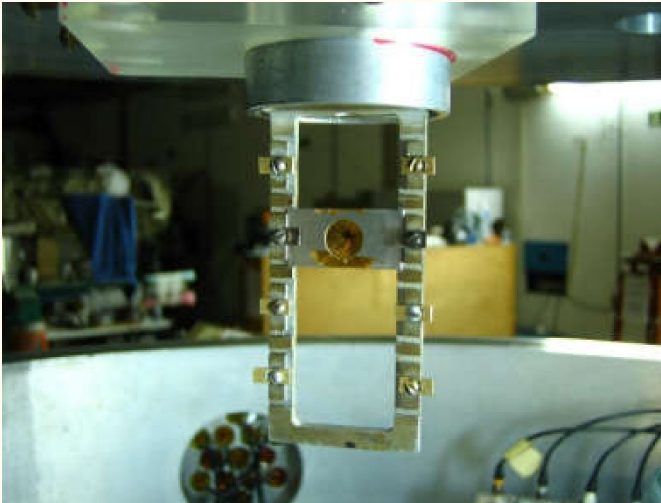
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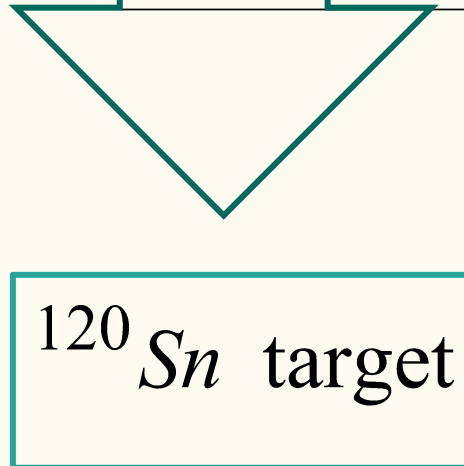


- 1. The Laboratories and SETUP's**
- 2. The Theoretical Optical Model**
- 3. Experimental Data x Theoretical Calculations**
- 4. Conclusions**

$$E_{Red} = E_{c.m.} - V_B$$

projectile	$V_B$ (MeV)	$R_B$ (fm)	$\hbar\omega$ (MeV)
$^4\text{He}$	14.22	9.48	4.92
$^6\text{He}$	12.78	10.52	3.35
$^6\text{Li}$	19.76	10.16	4.20
$^7\text{Li}$	19.45	10.34	3.86
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- Different projectiles +  $^{120}\text{Sn}$  @ energies below, around and above the respective Coulomb barrier

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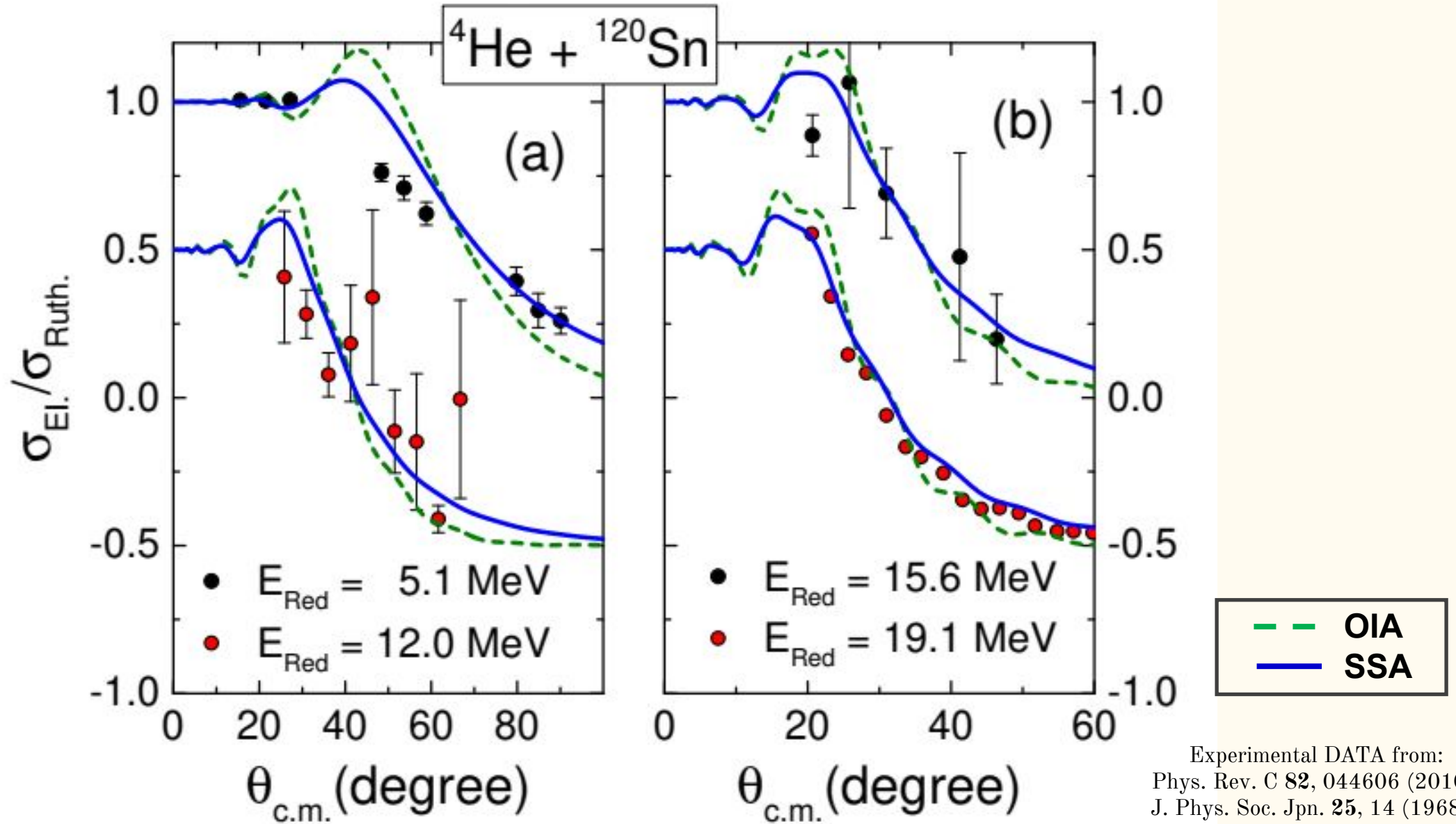
↓

**0.78**

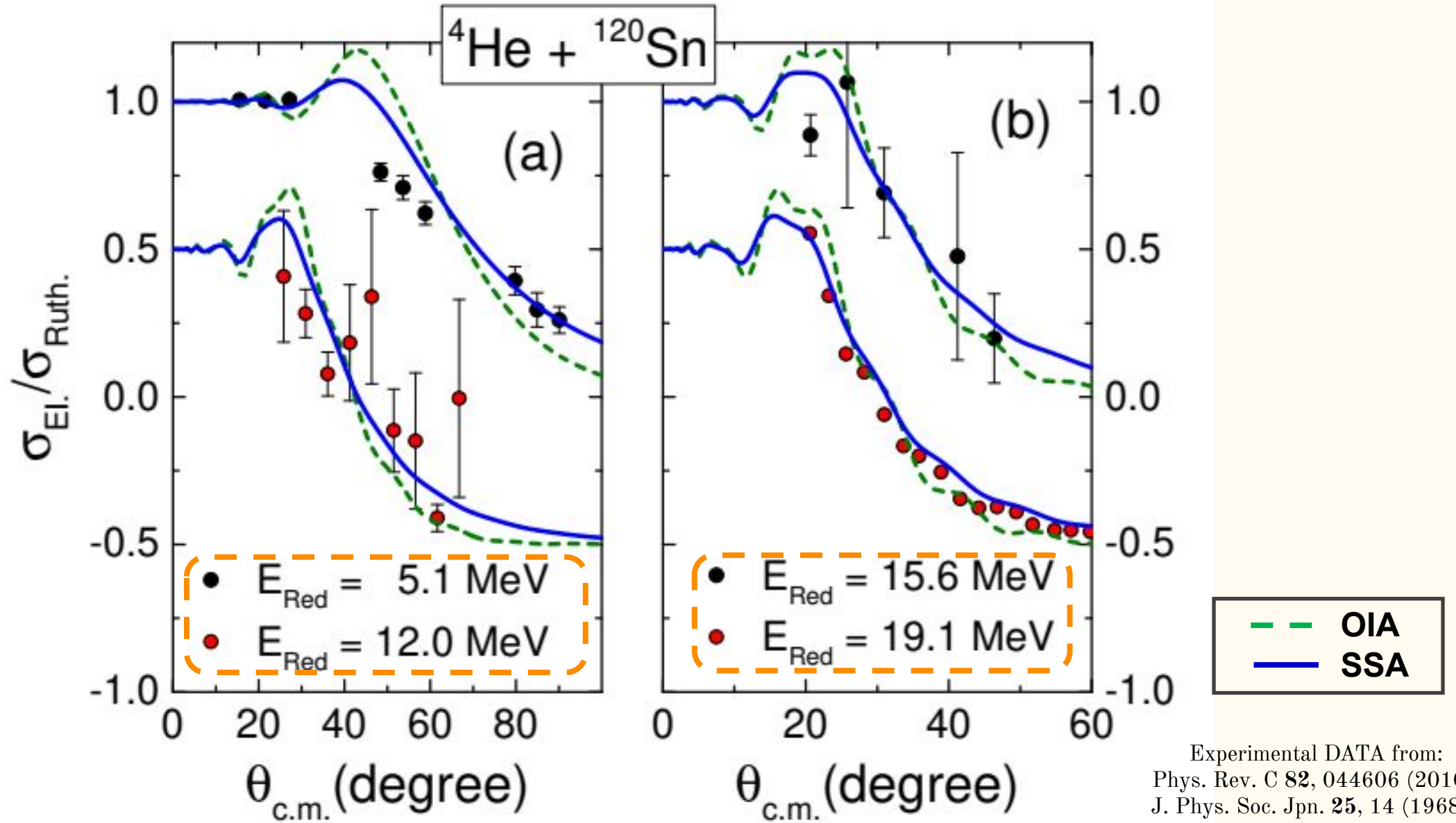
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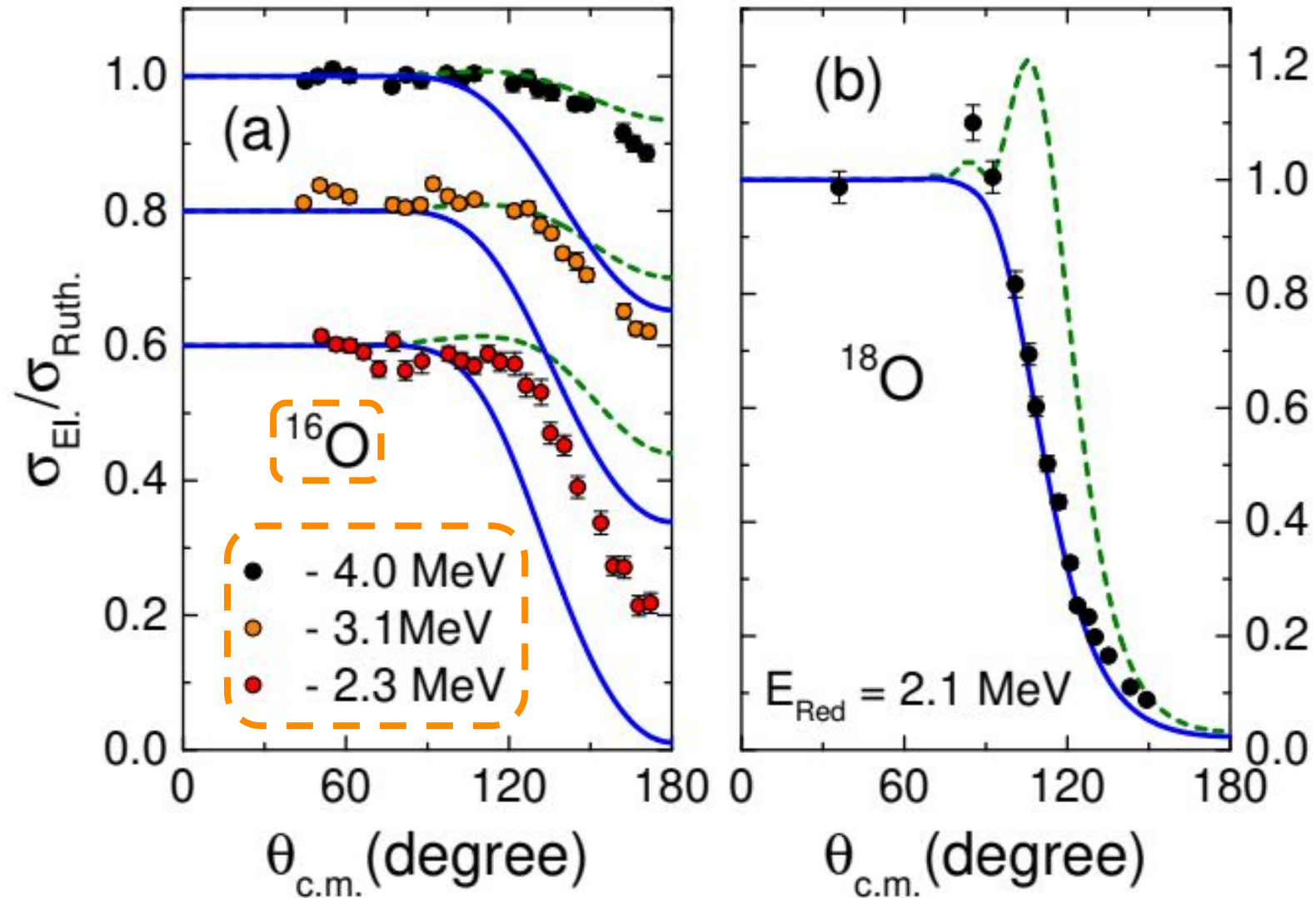
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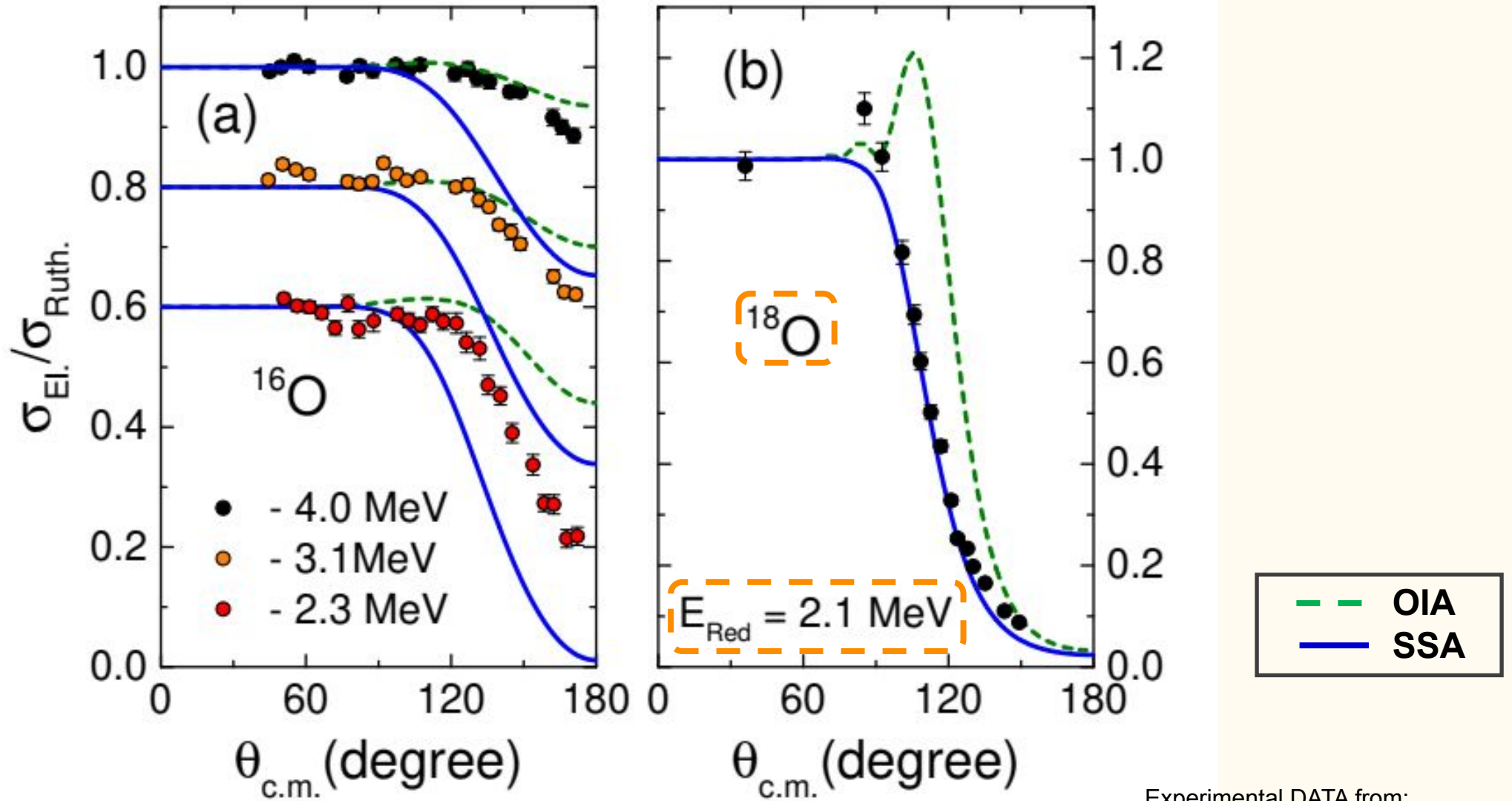


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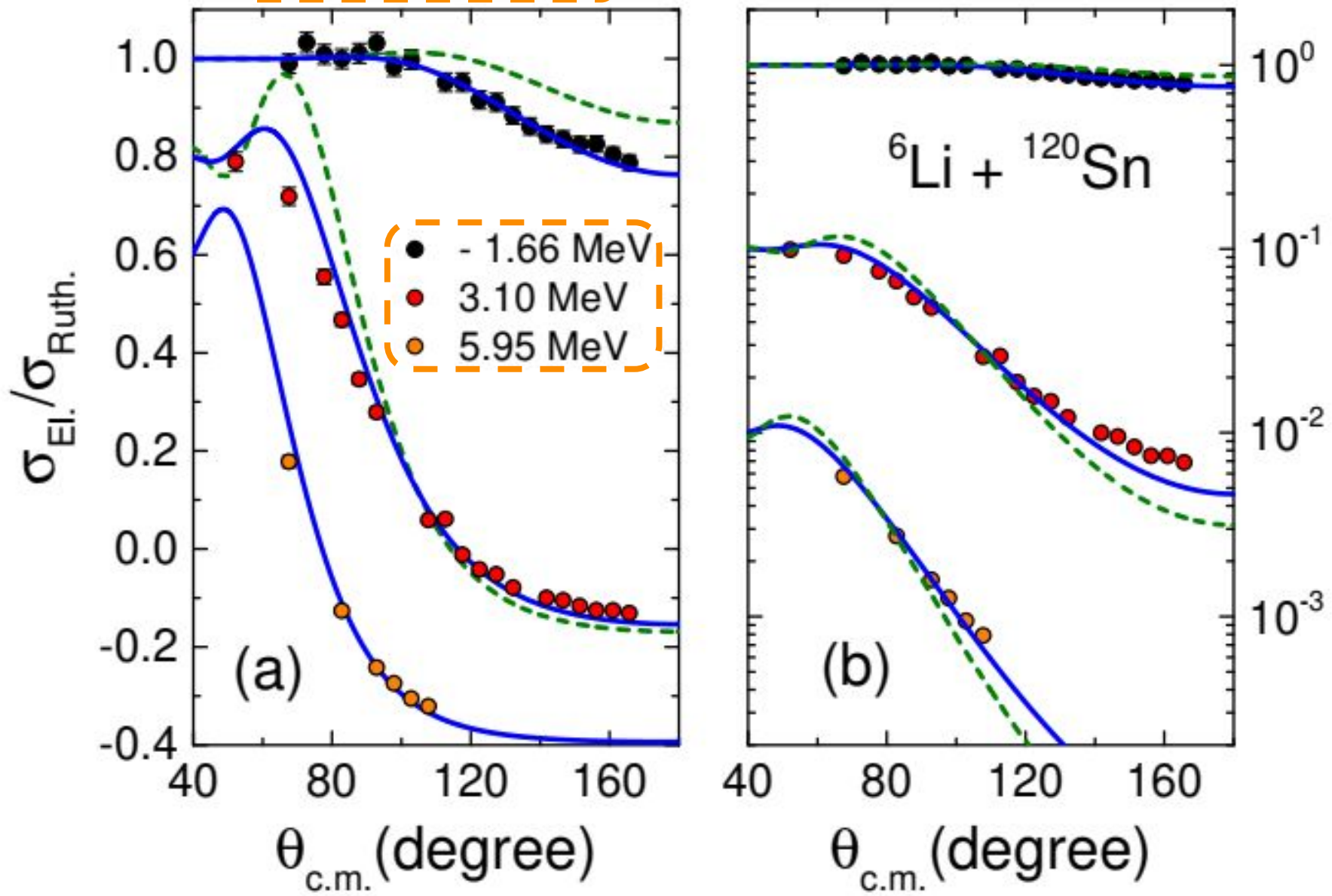
Experimental DATA from:  
Nucl. Phys. A **679**, 287 (2001).

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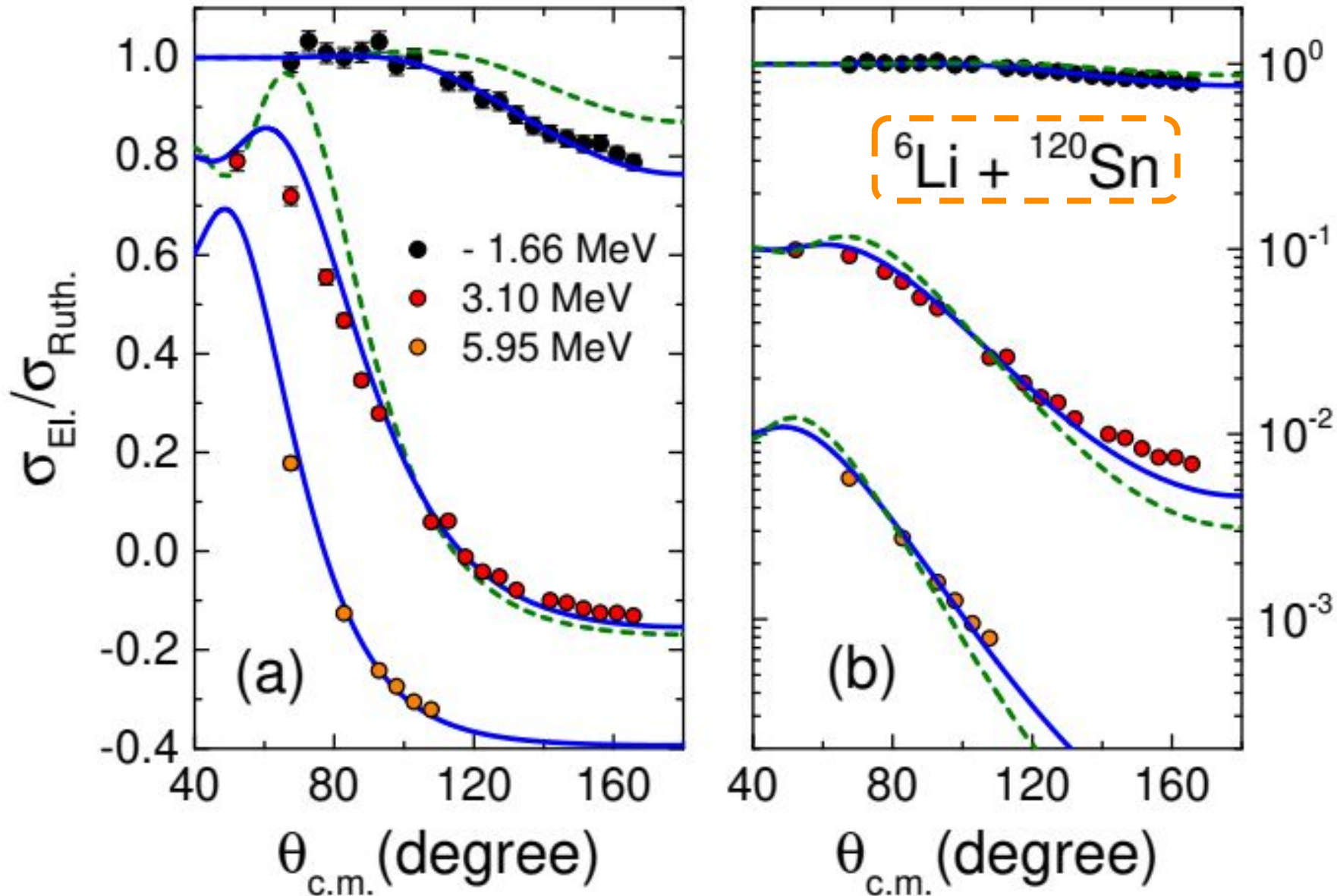


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Z. Phys. A: At. Nucl. **273**, 211 (1975).

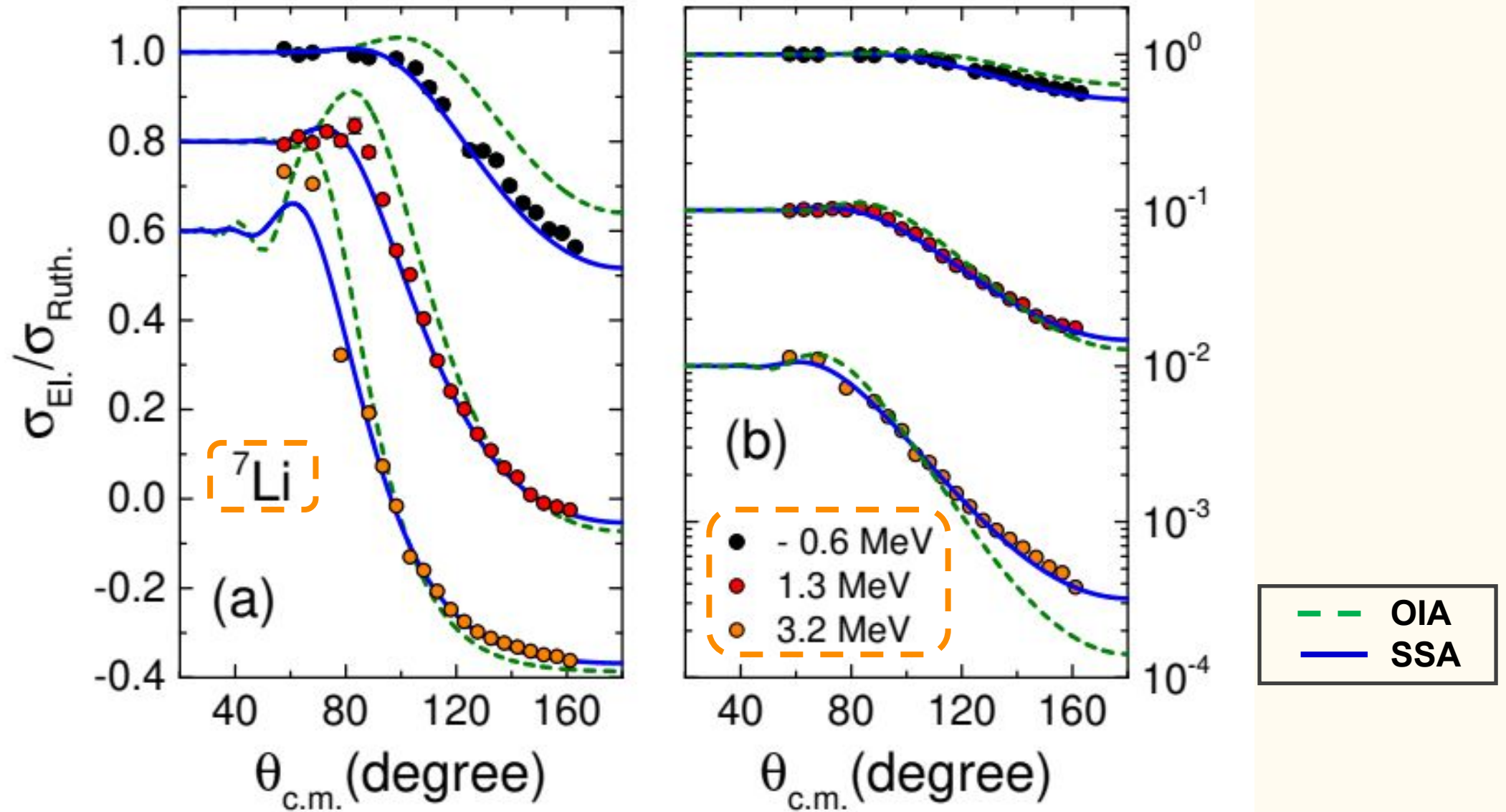
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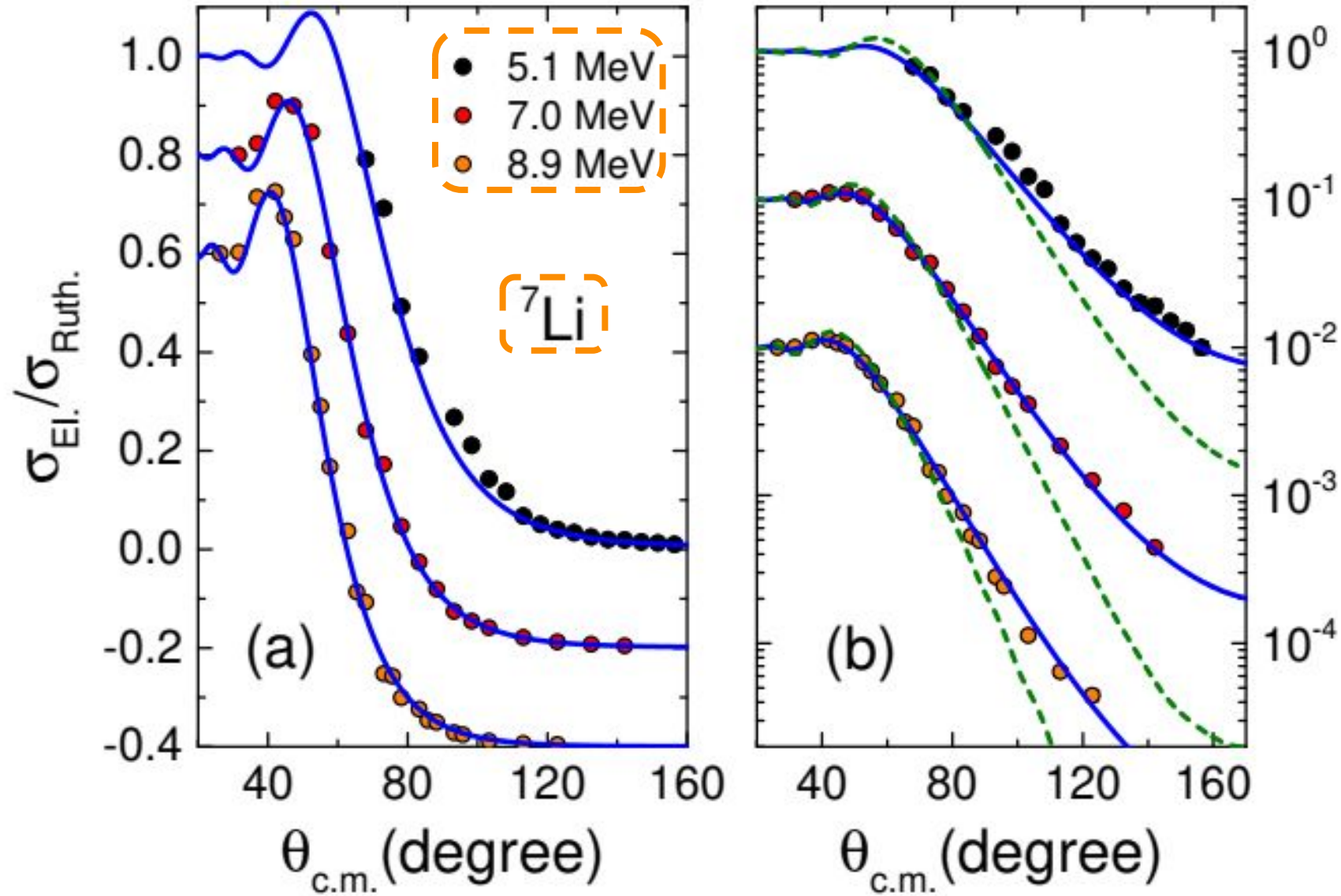
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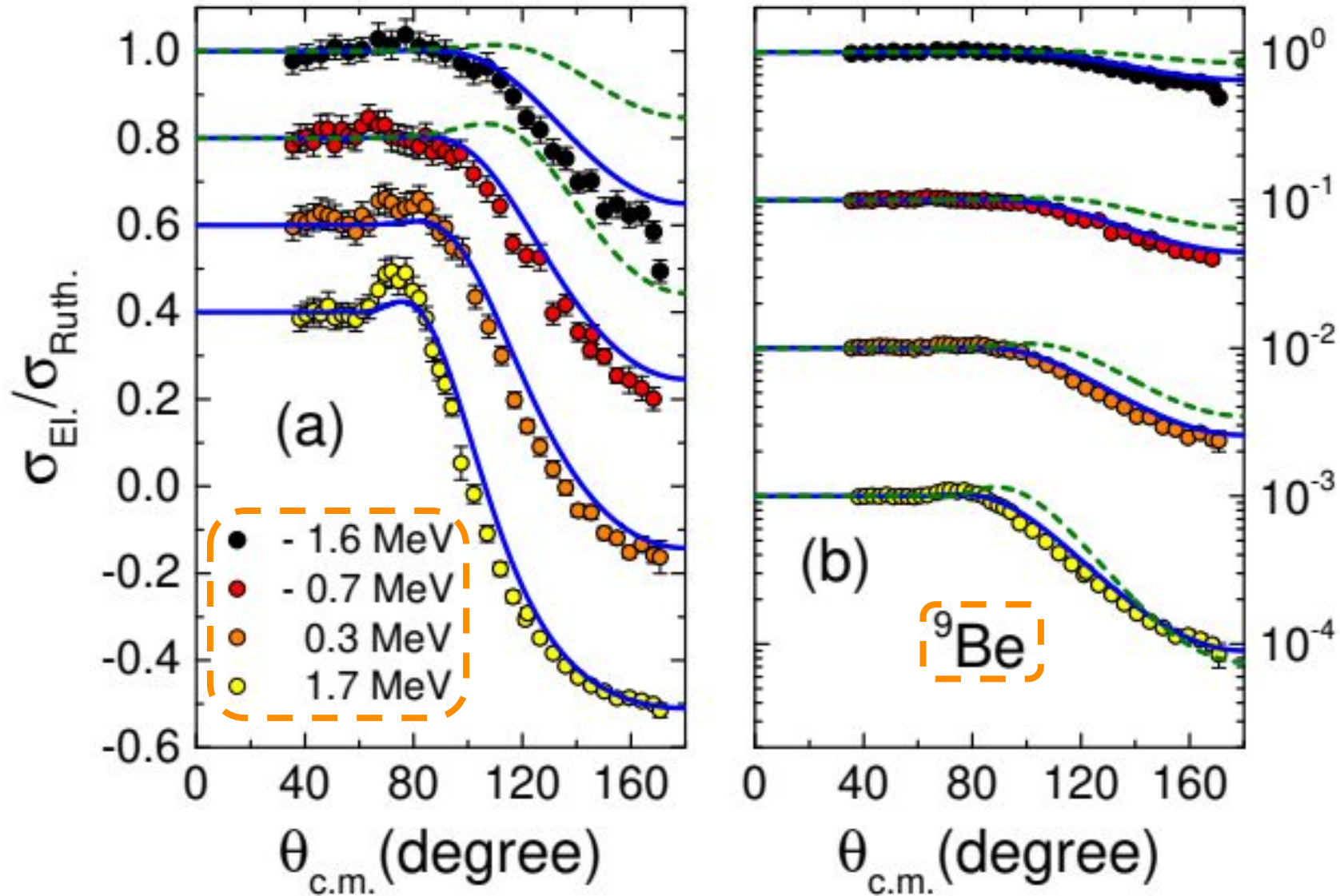


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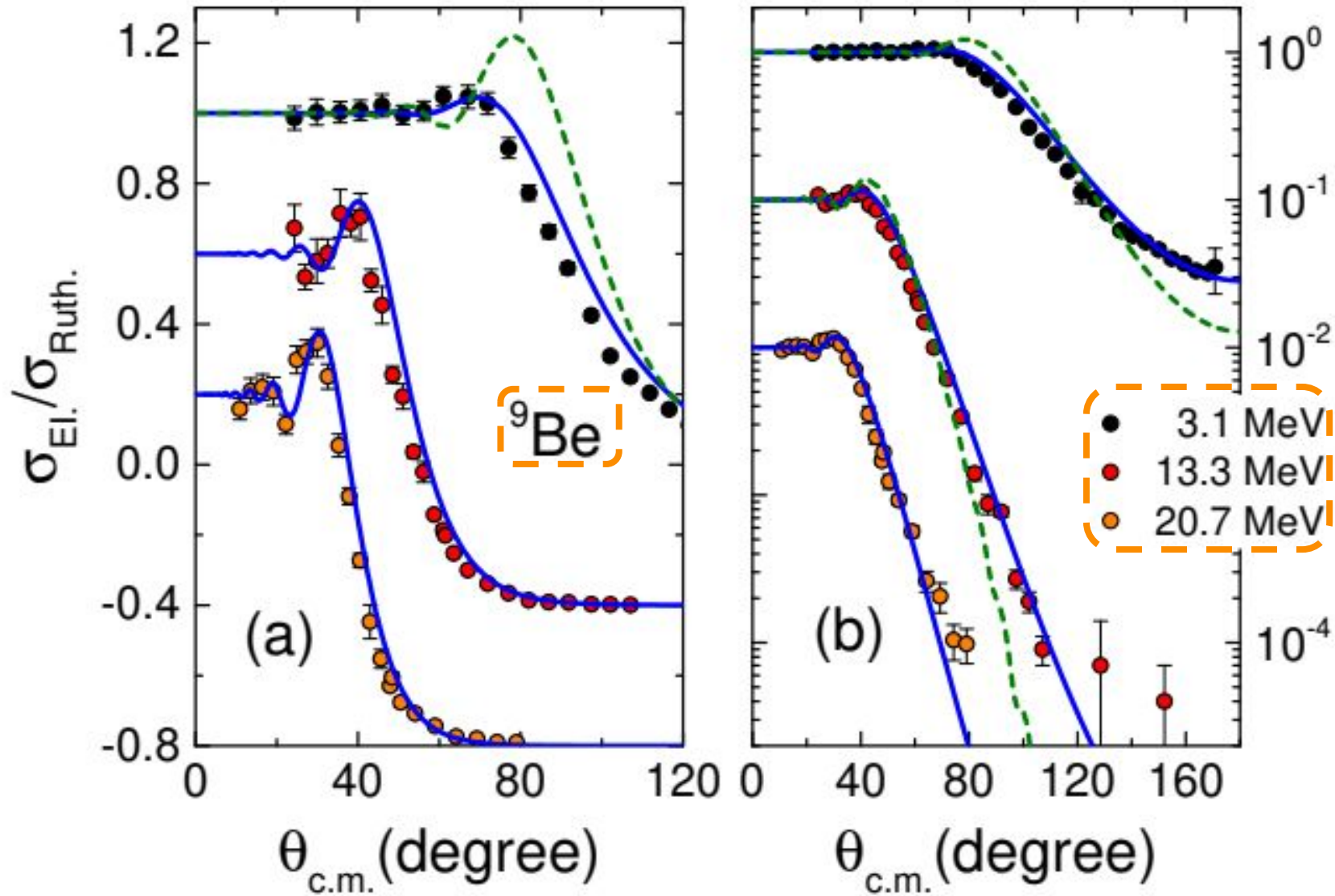




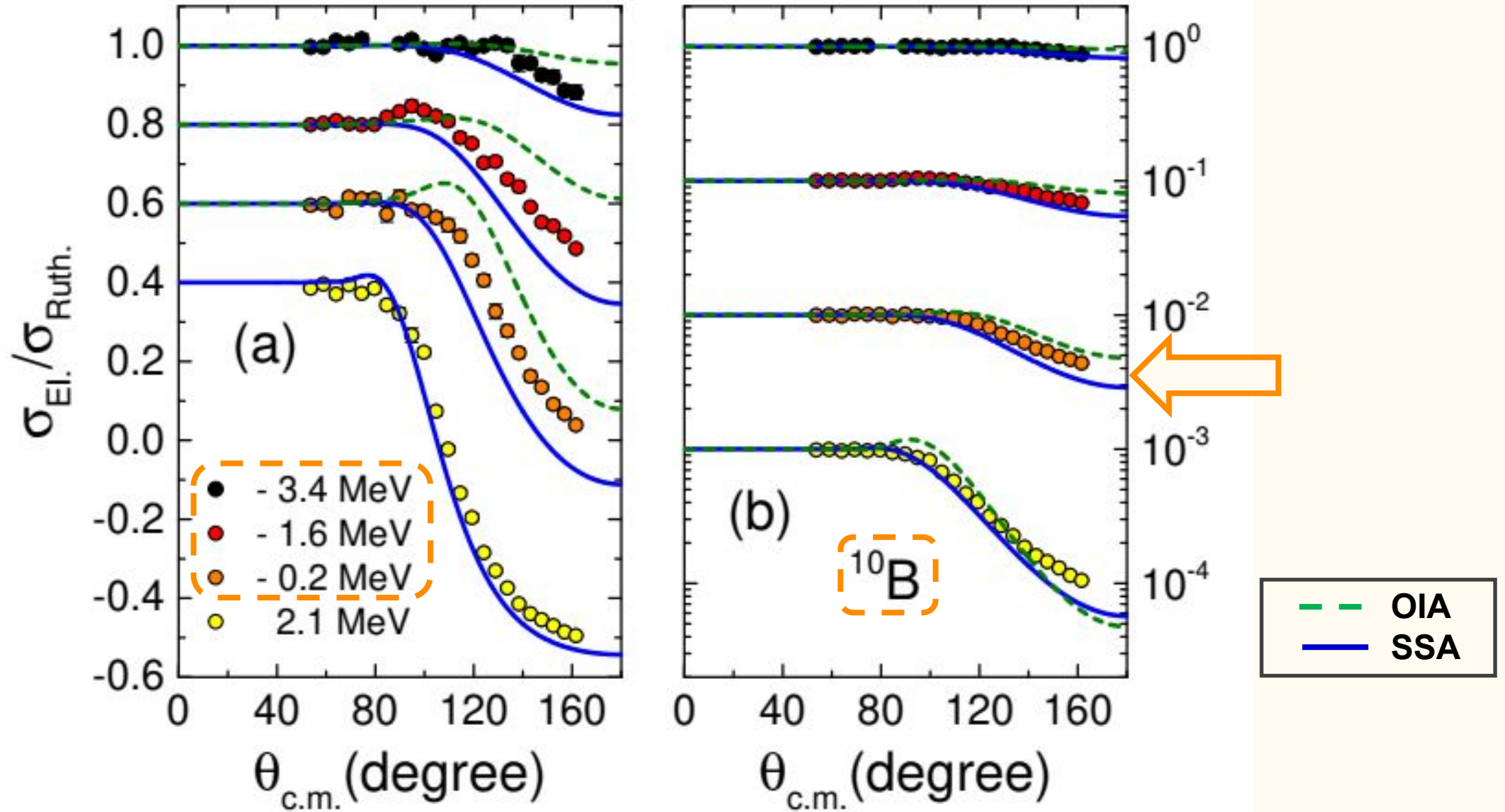
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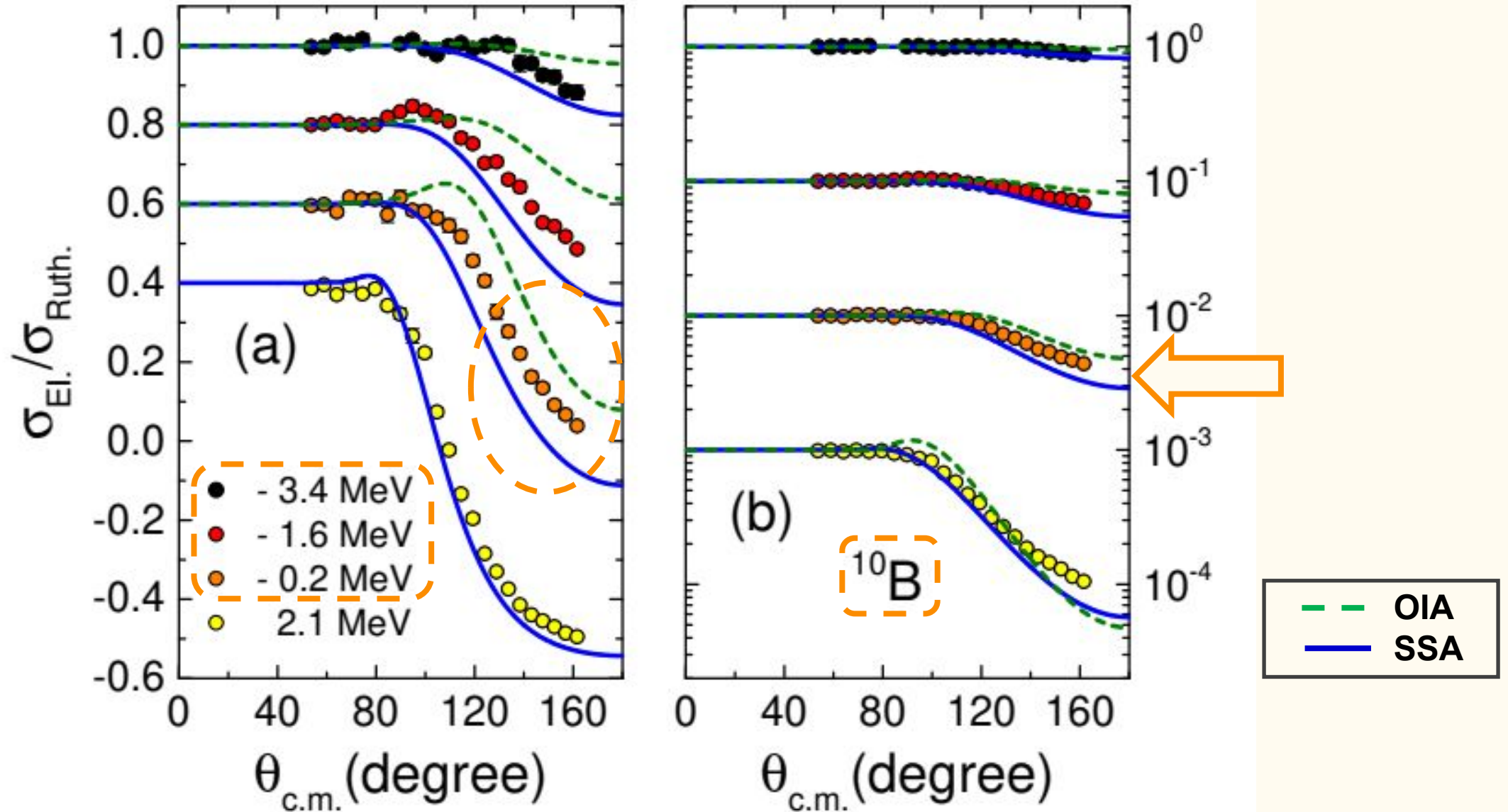
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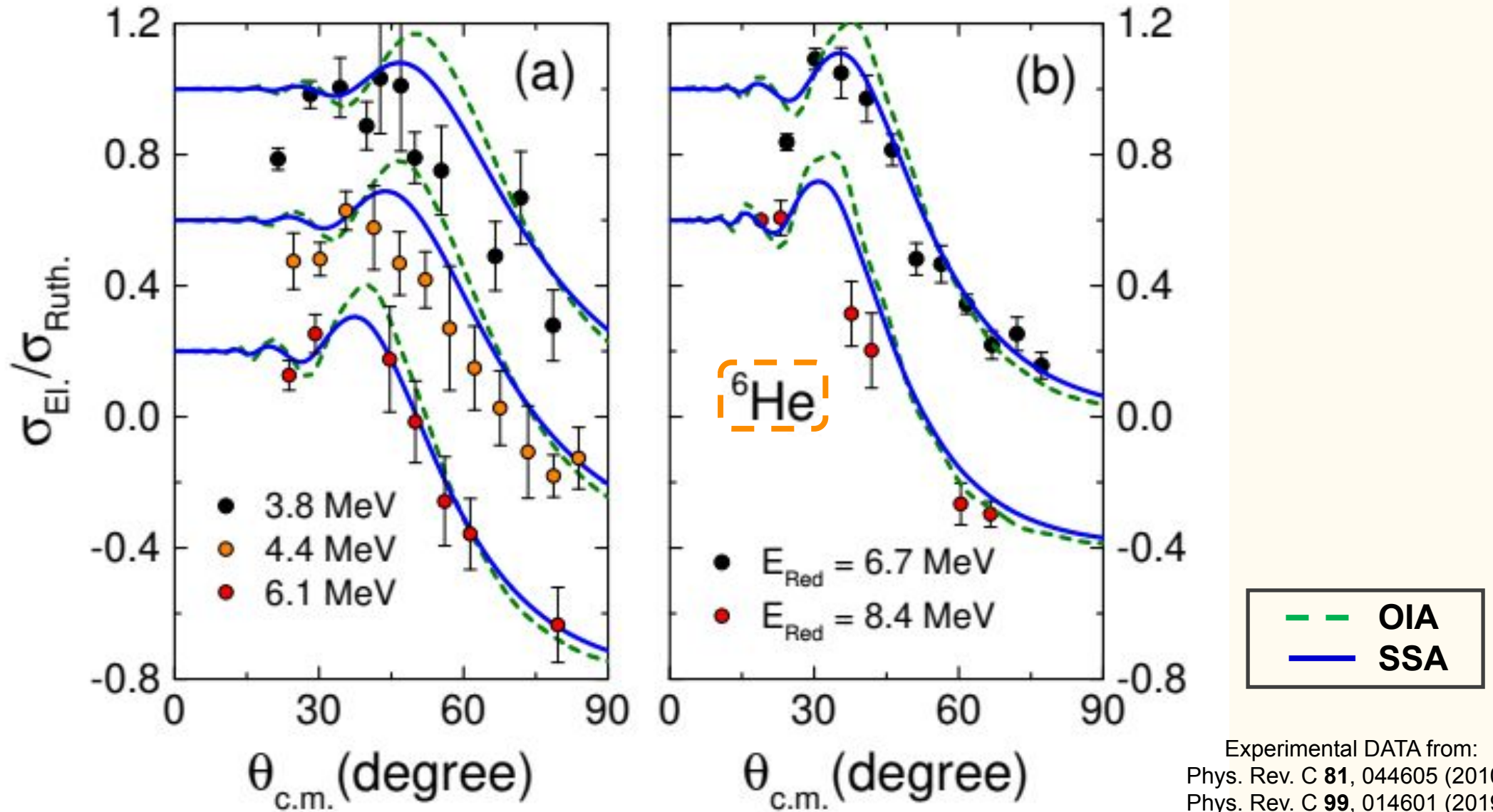
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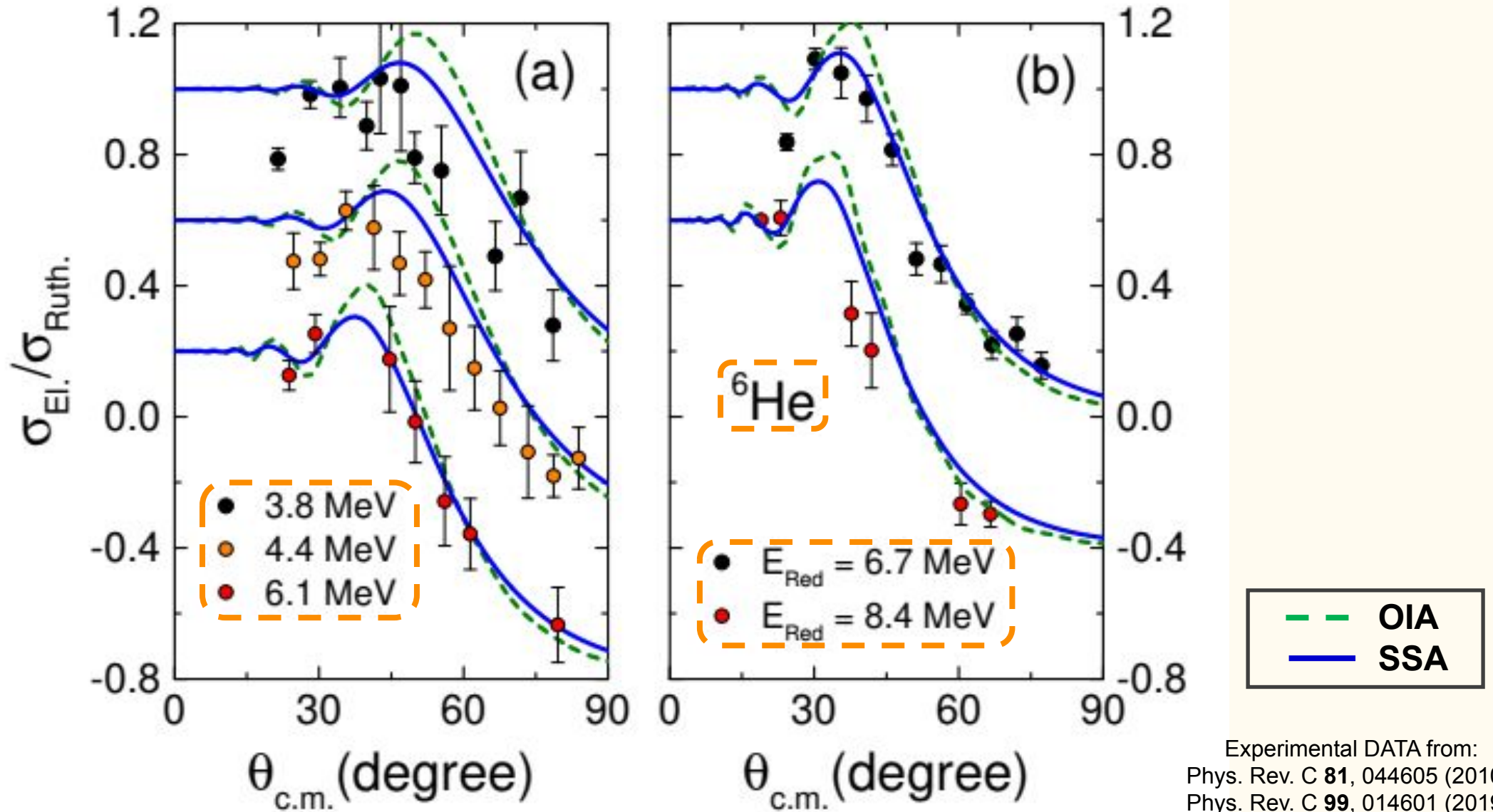
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Strong Surface Absorption  
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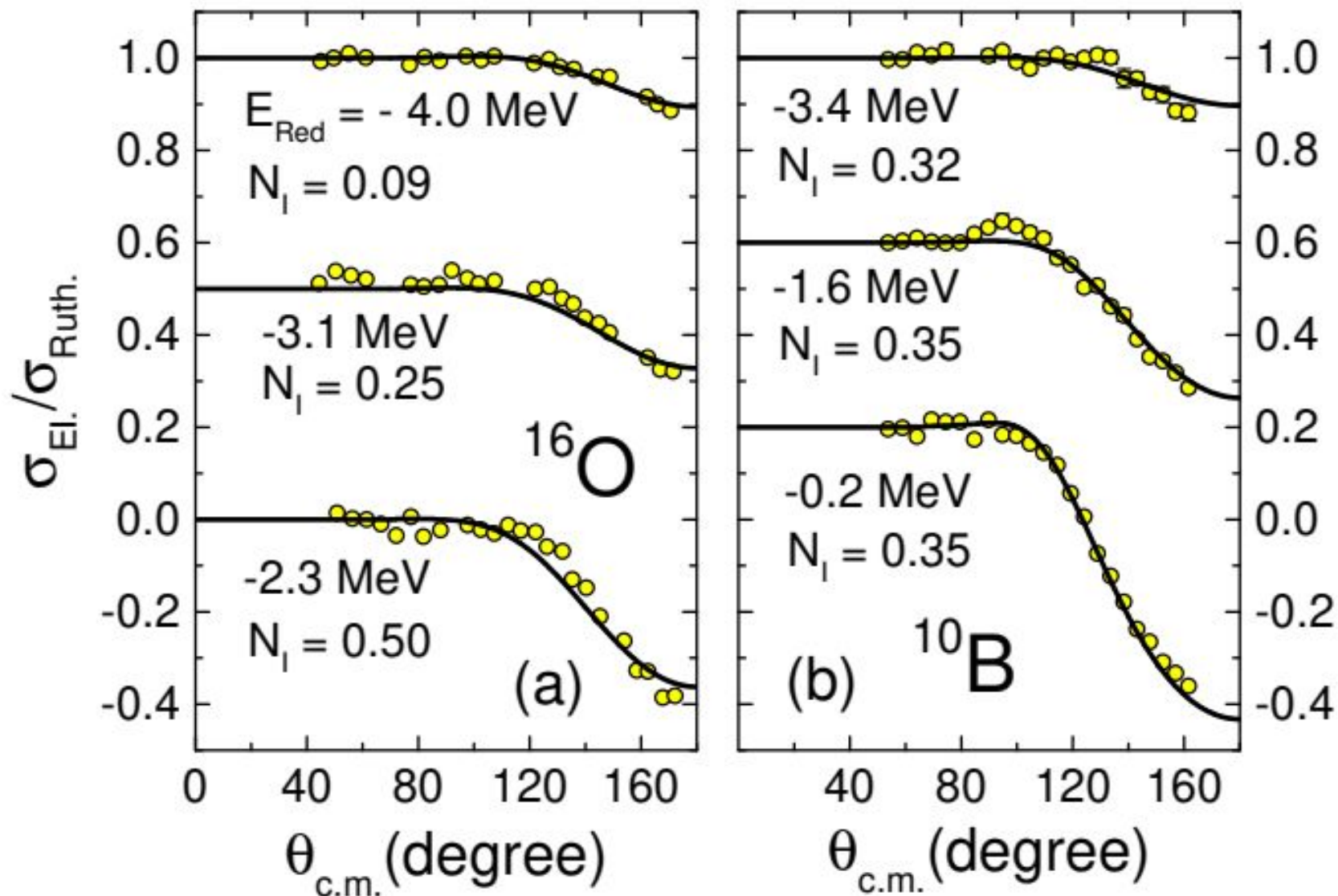
Studying the intensity of  
the imaginary potential

$$V_{SPP}(R) = V_{Fold}(R)e^{-4v^2/c^2}$$

$$V_{Fold}(R) = \int \int \rho_1(\vec{r}_1)\rho_2(\vec{r}_2)\nu_{NN}(\vec{R} - \vec{r}_1 + \vec{r}_2) d\vec{r}_1 d\vec{r}_2$$

# Sub-barrier region

$$E_{Red} = E_{c.m.} - V_B$$





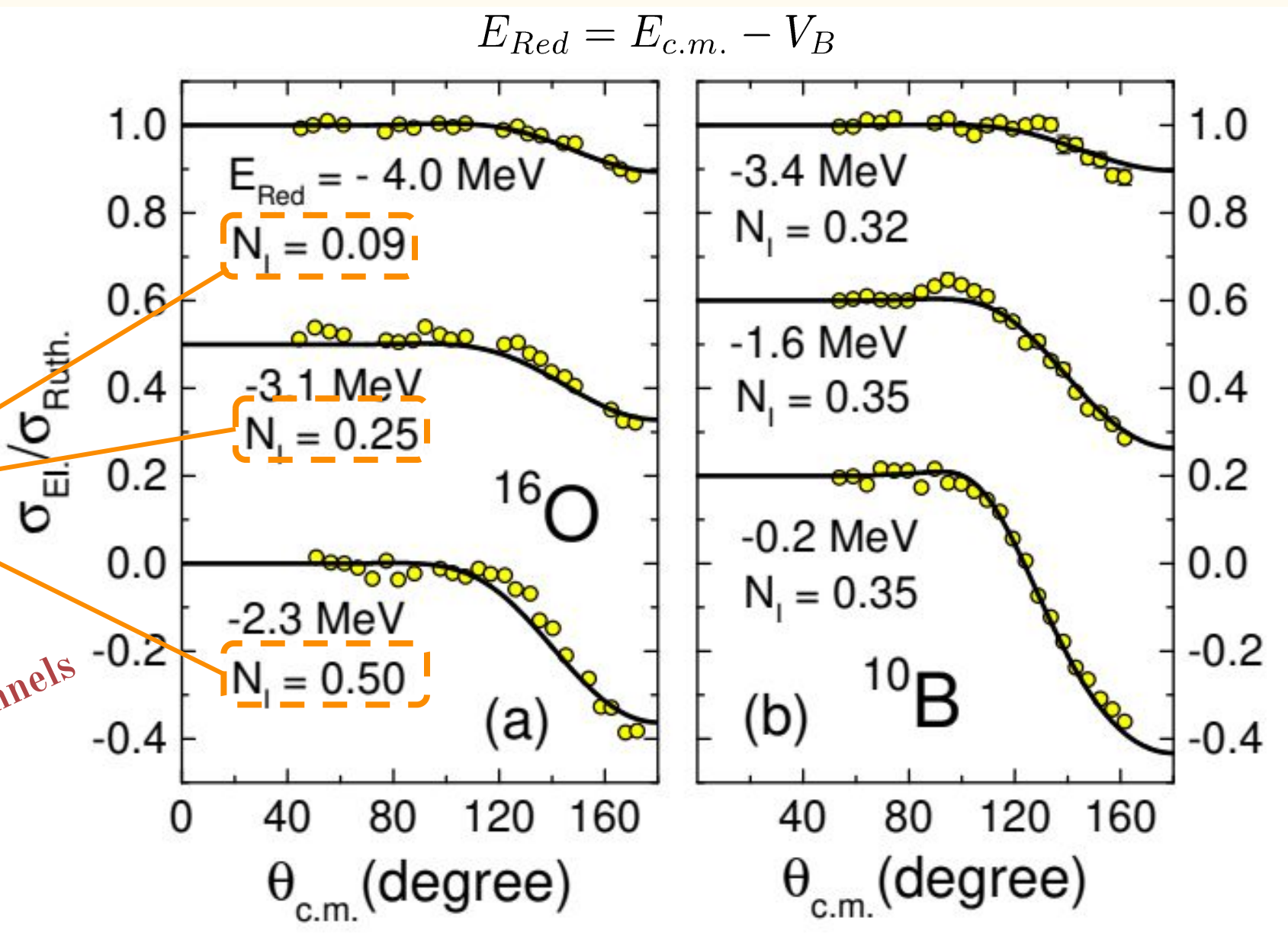
# Sub-barrier region

$$E_{Red} = E_{c.m.} - V_B$$

progressive  
increasing

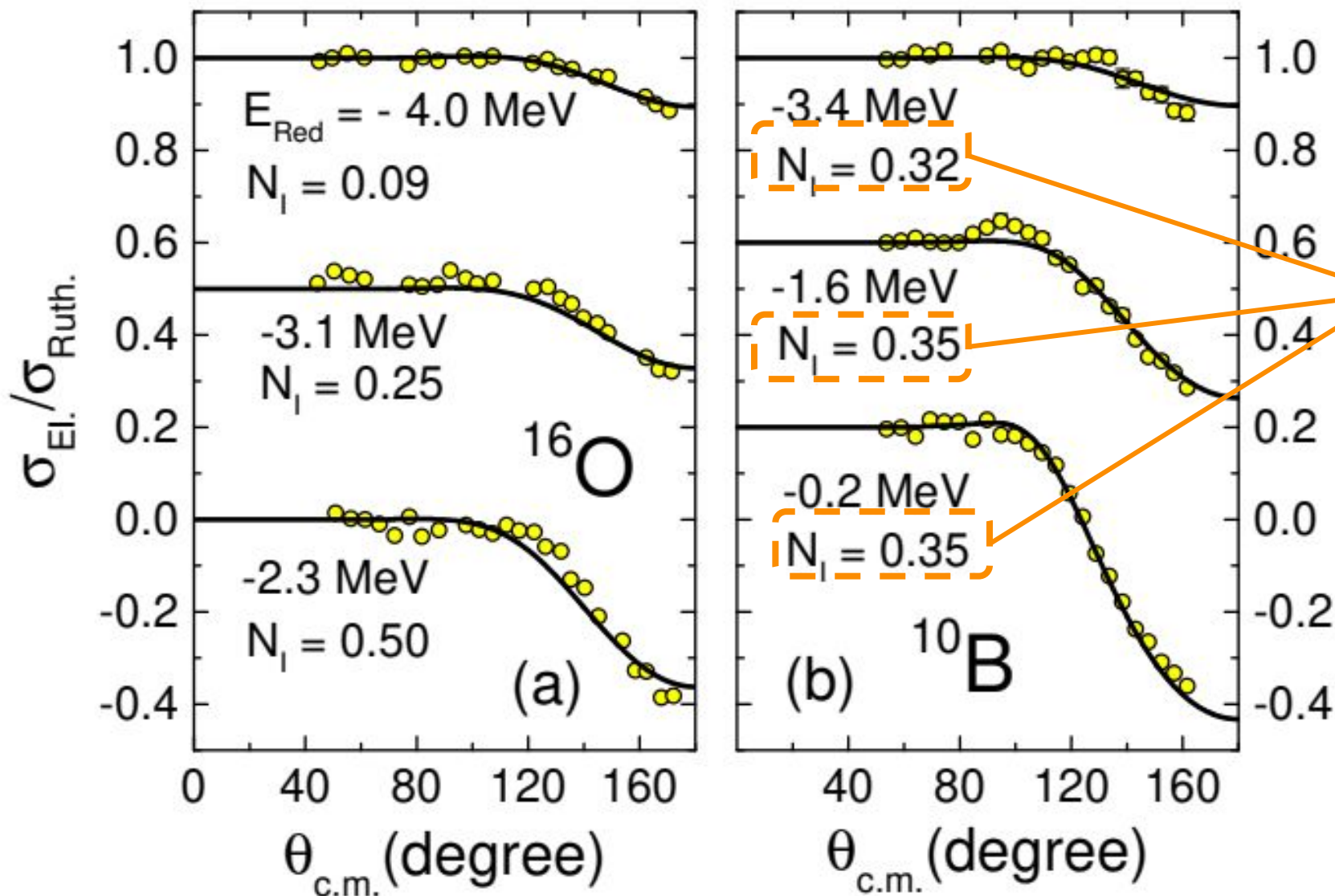


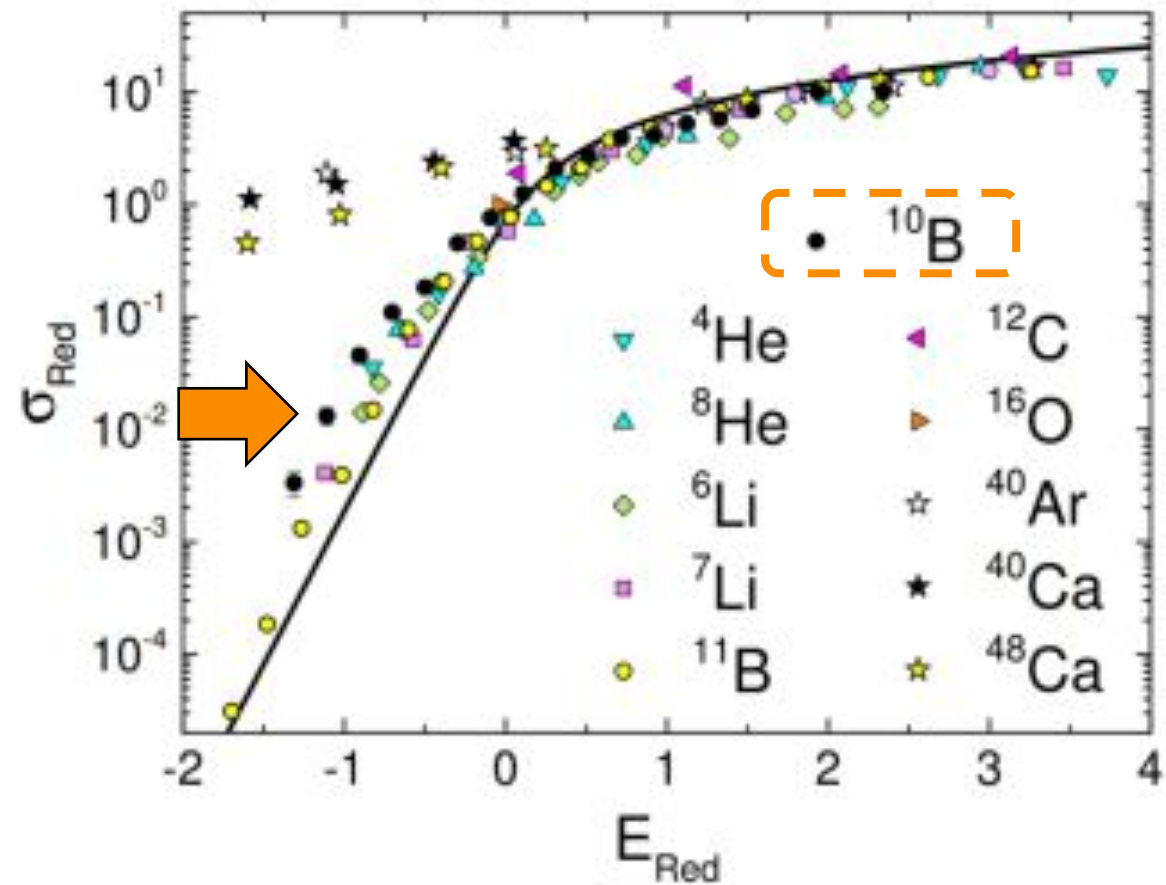
progressive  
opening of  
reaction channels



# Sub-barrier region

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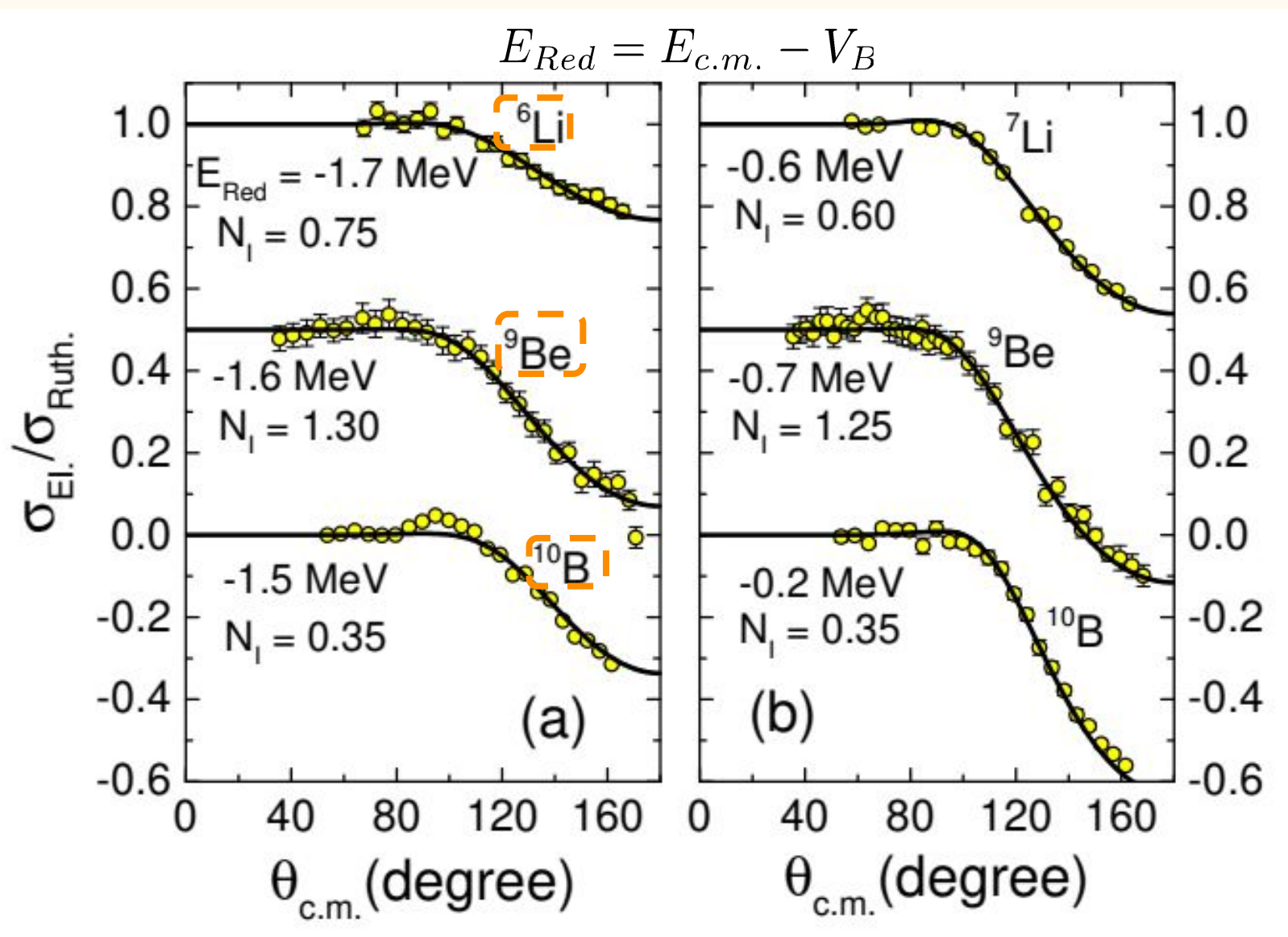


*M. Aversa et al., Phys. Rev. C 101, 044601 (2020)*

FIG. 9. (Color online) Experimental reduced fusion cross section as a function of the reduced energy, for several systems involving the same target nucleus:  $^{197}\text{Au}$ . The solid lines represent the reduced BPM cross section.

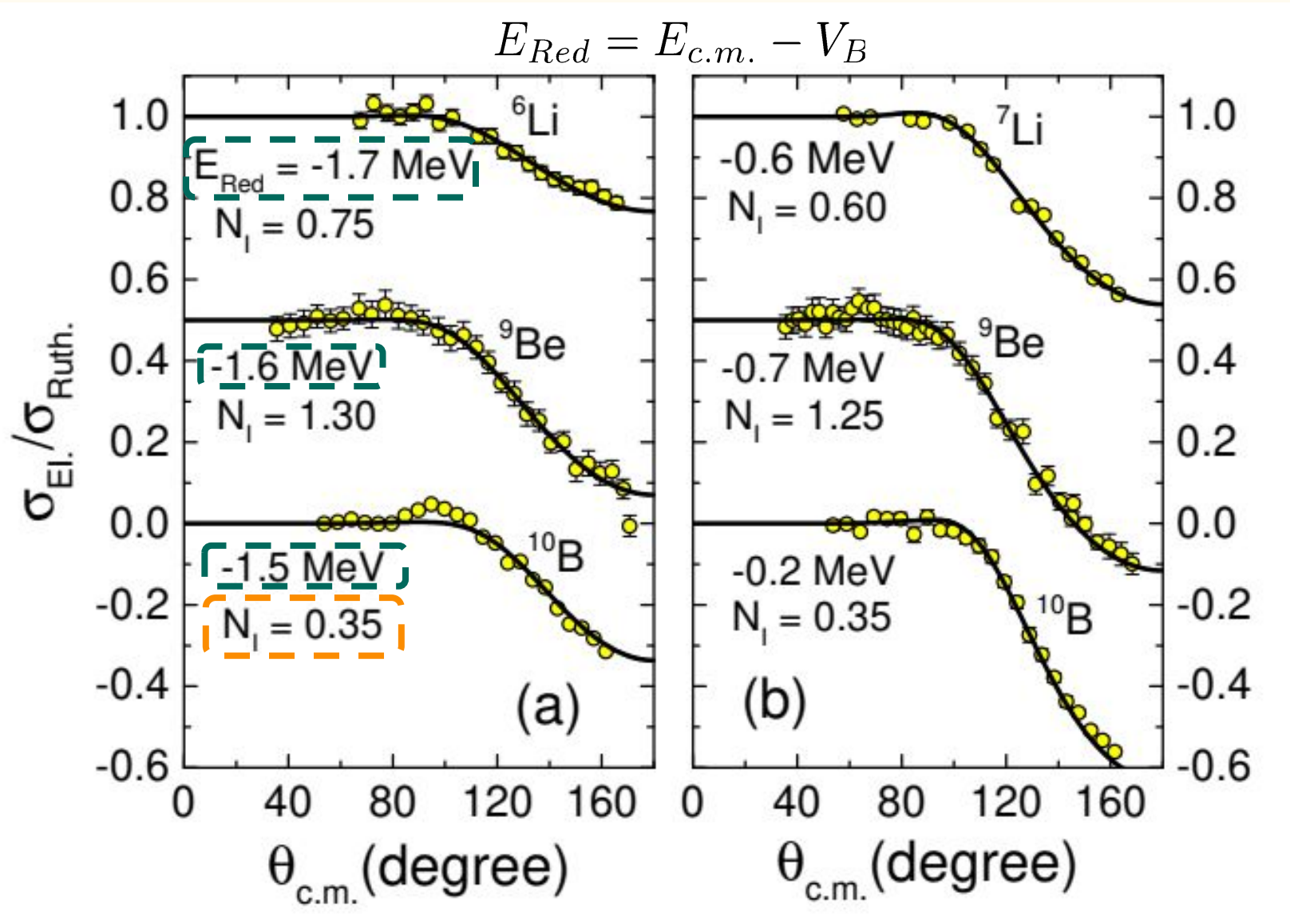
Fusion is somehow favored for  $^{10}\text{B}$ , while peripheral reaction channels, which are connected to strong surface absorption processes, are favored for the other weakly bound nuclei.

# Sub-barrier region



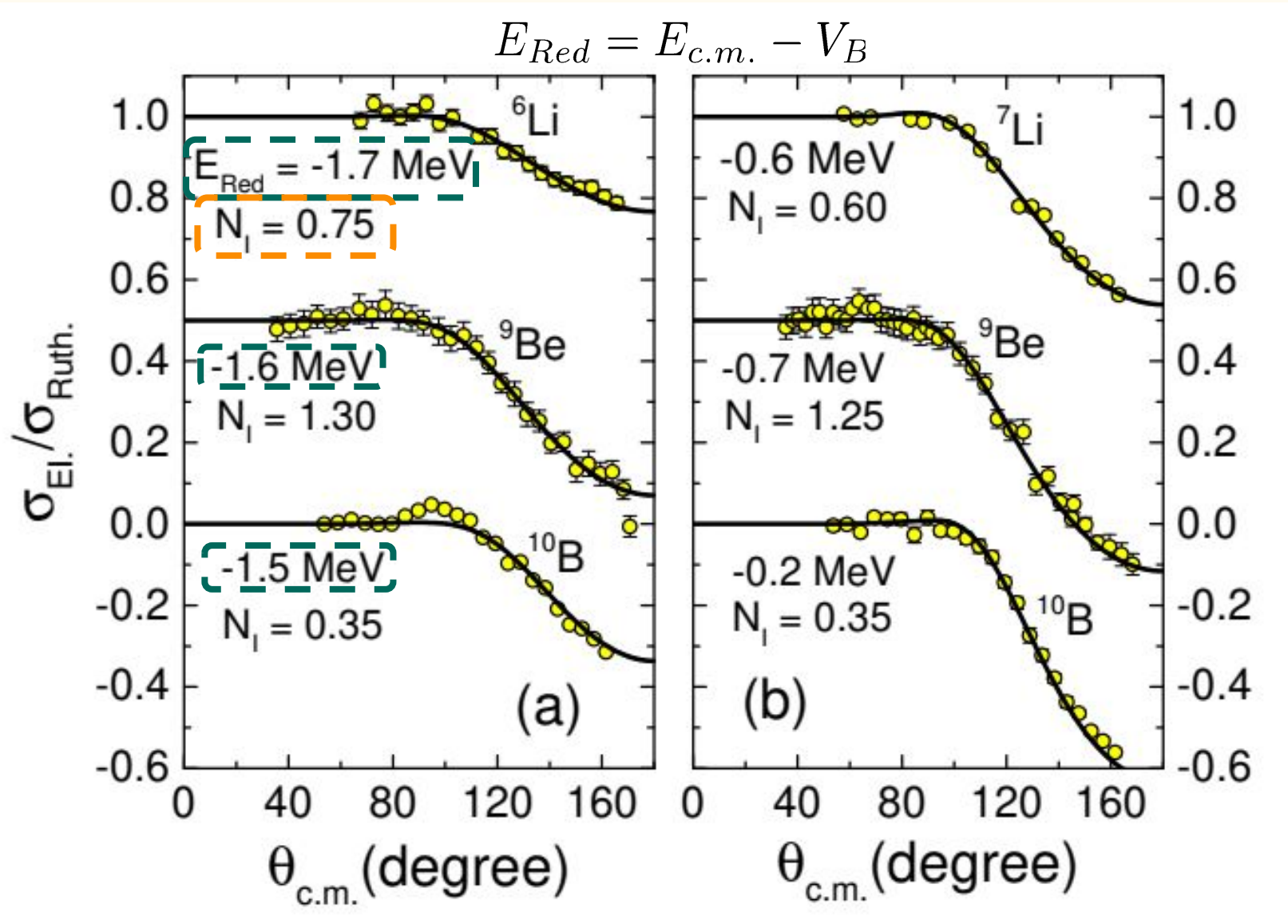
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Progressive  
increasing



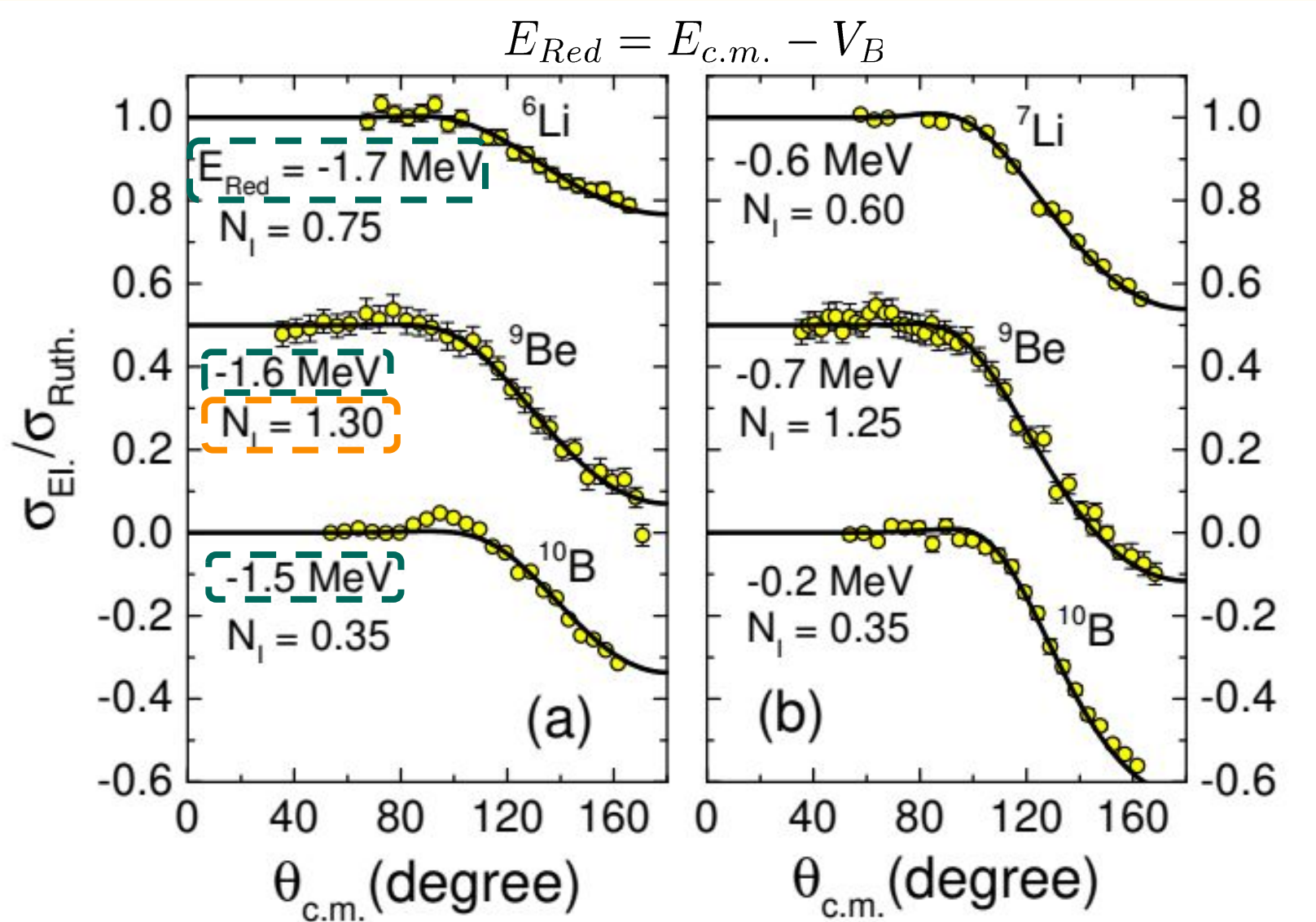
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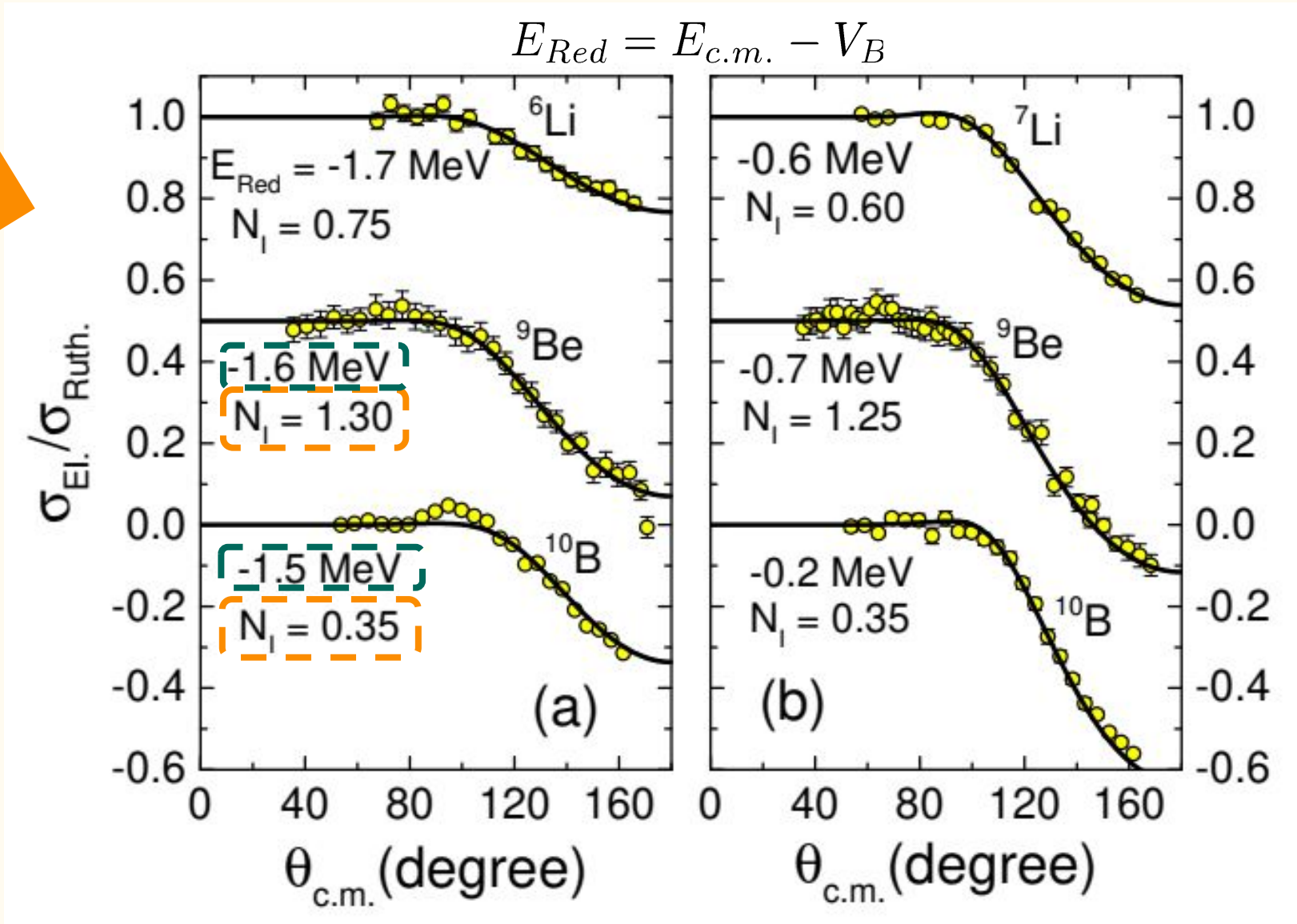
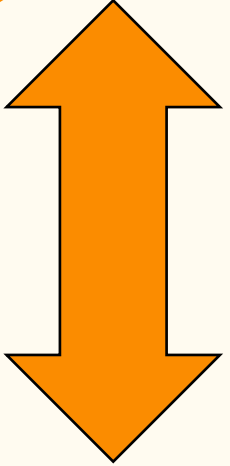
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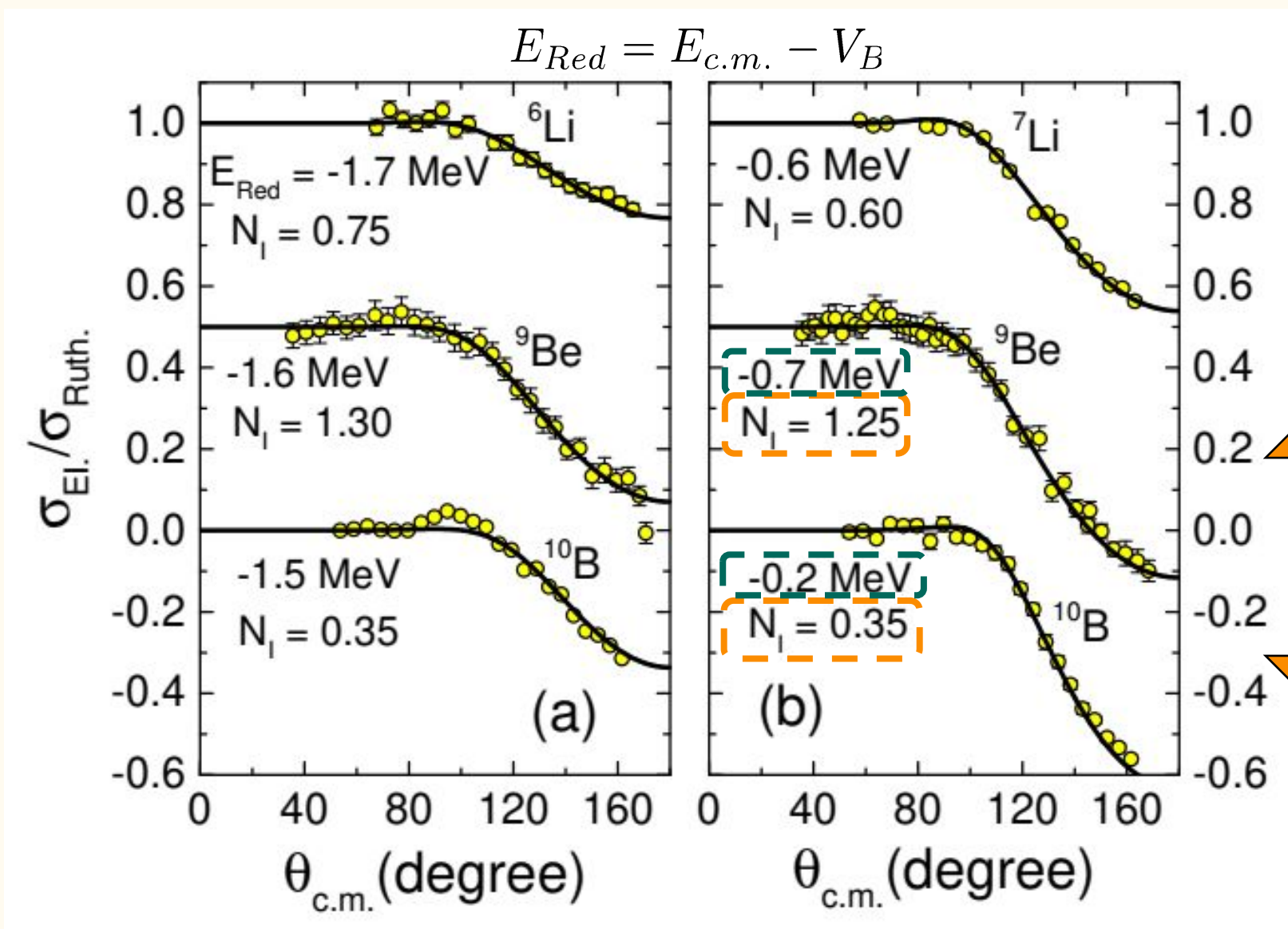
# Sub-barrier region

strong differences



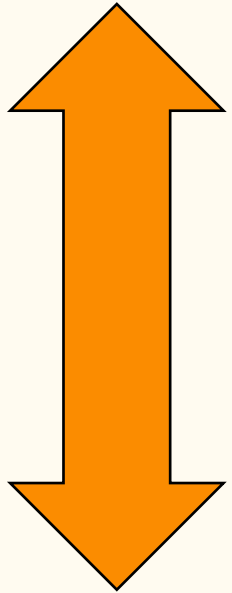
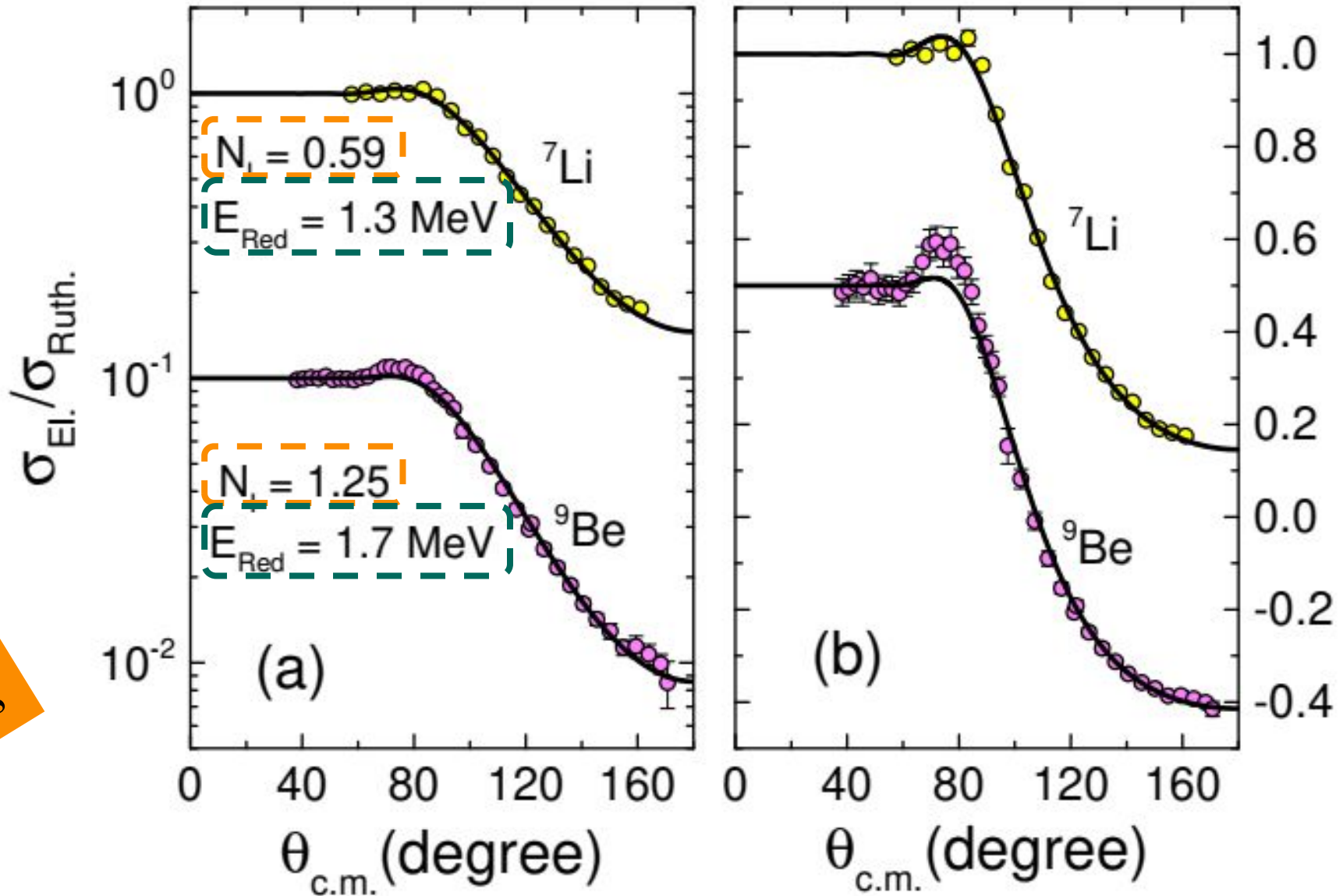


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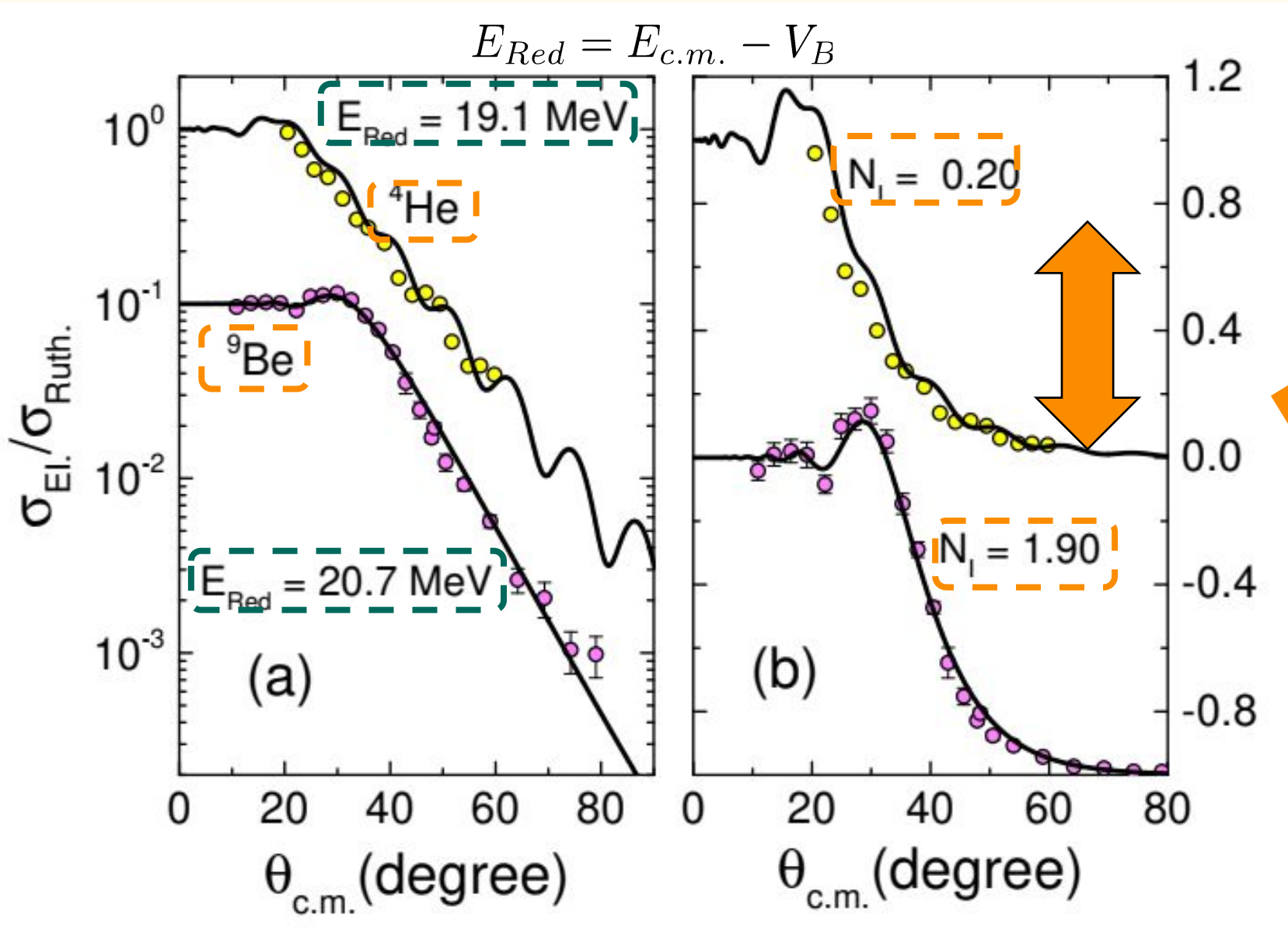
# Above-barrier region

$$E_{Red} = E_{c.m.} - V_B$$



strong differences

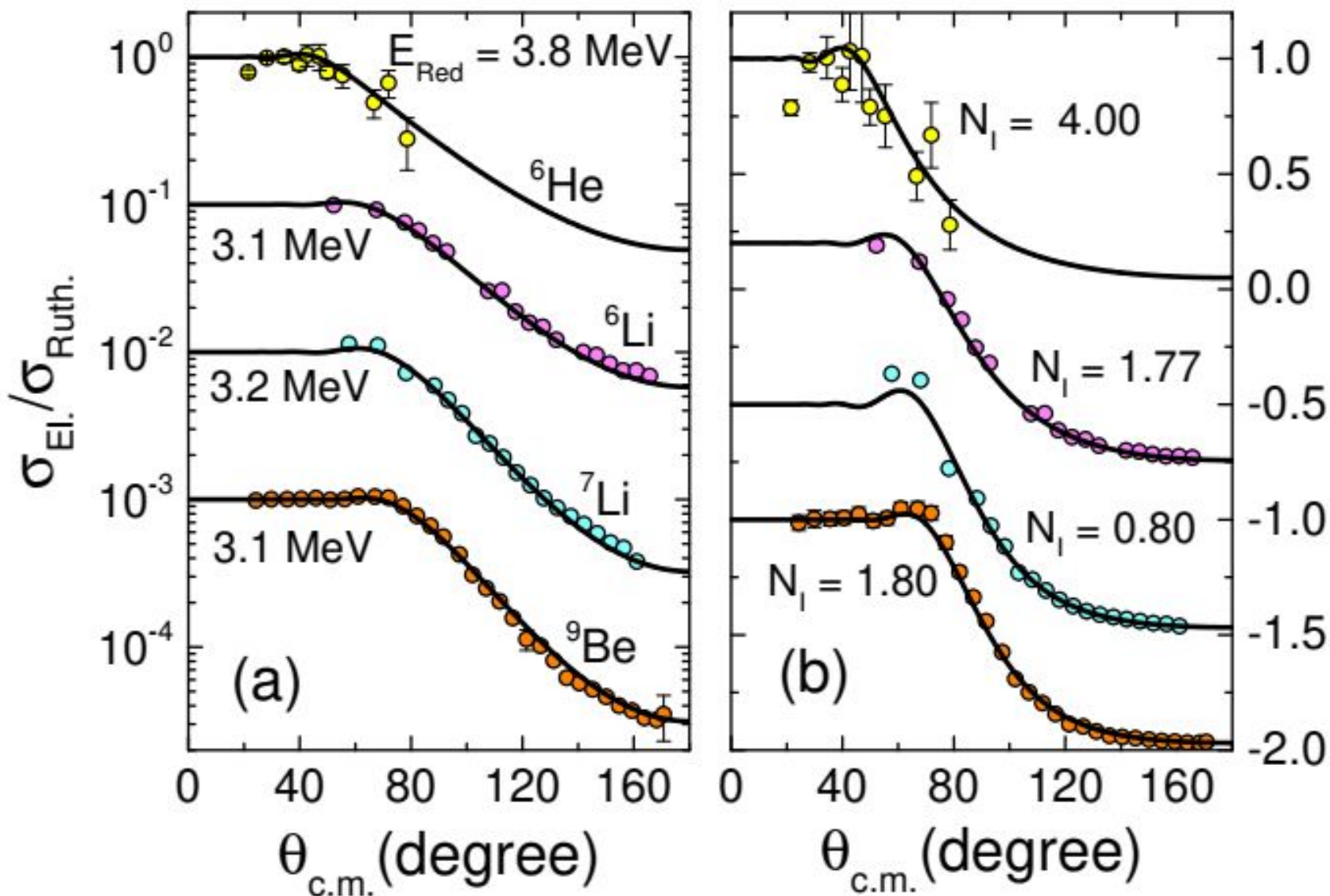
# Above-barrier region



strong differences

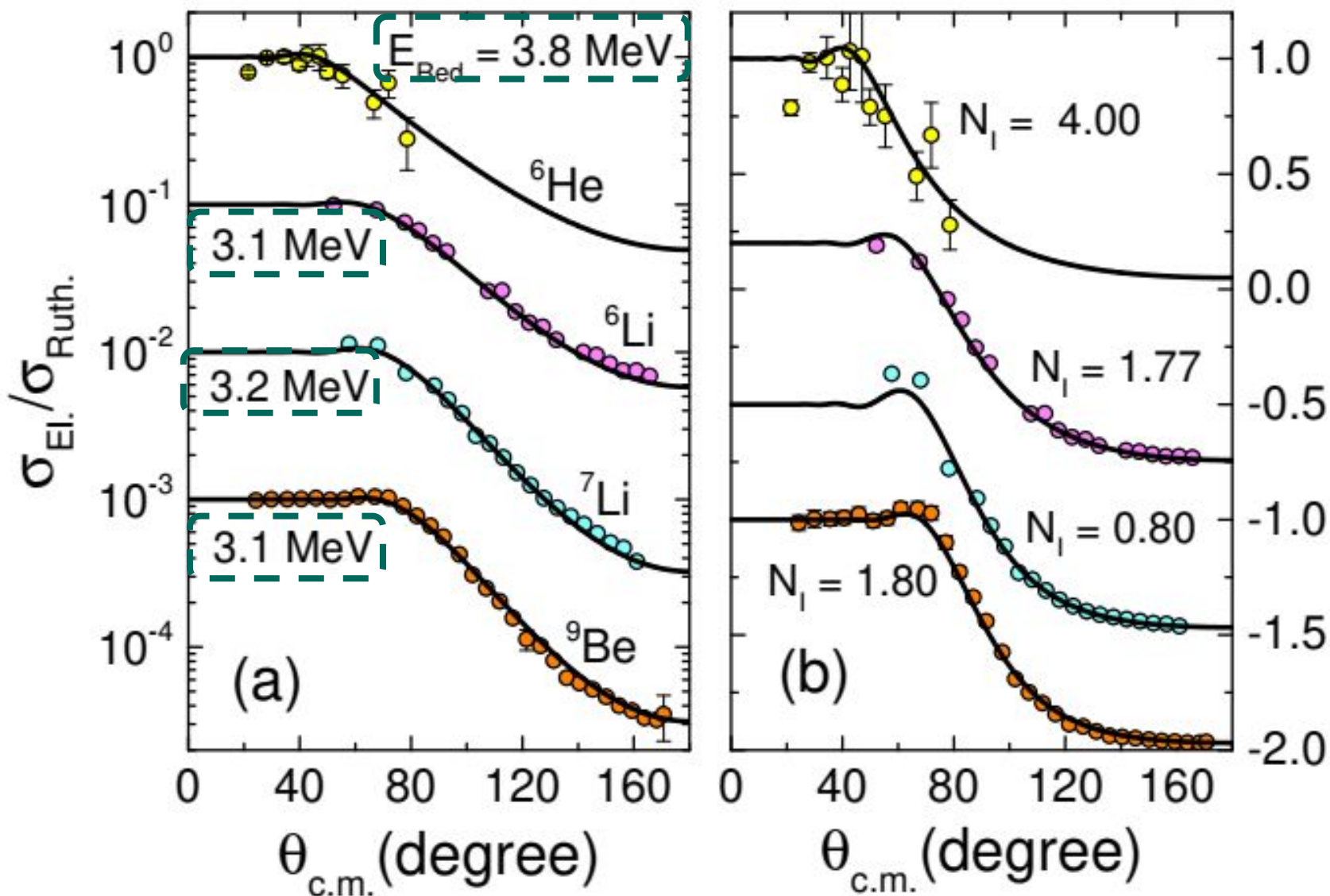
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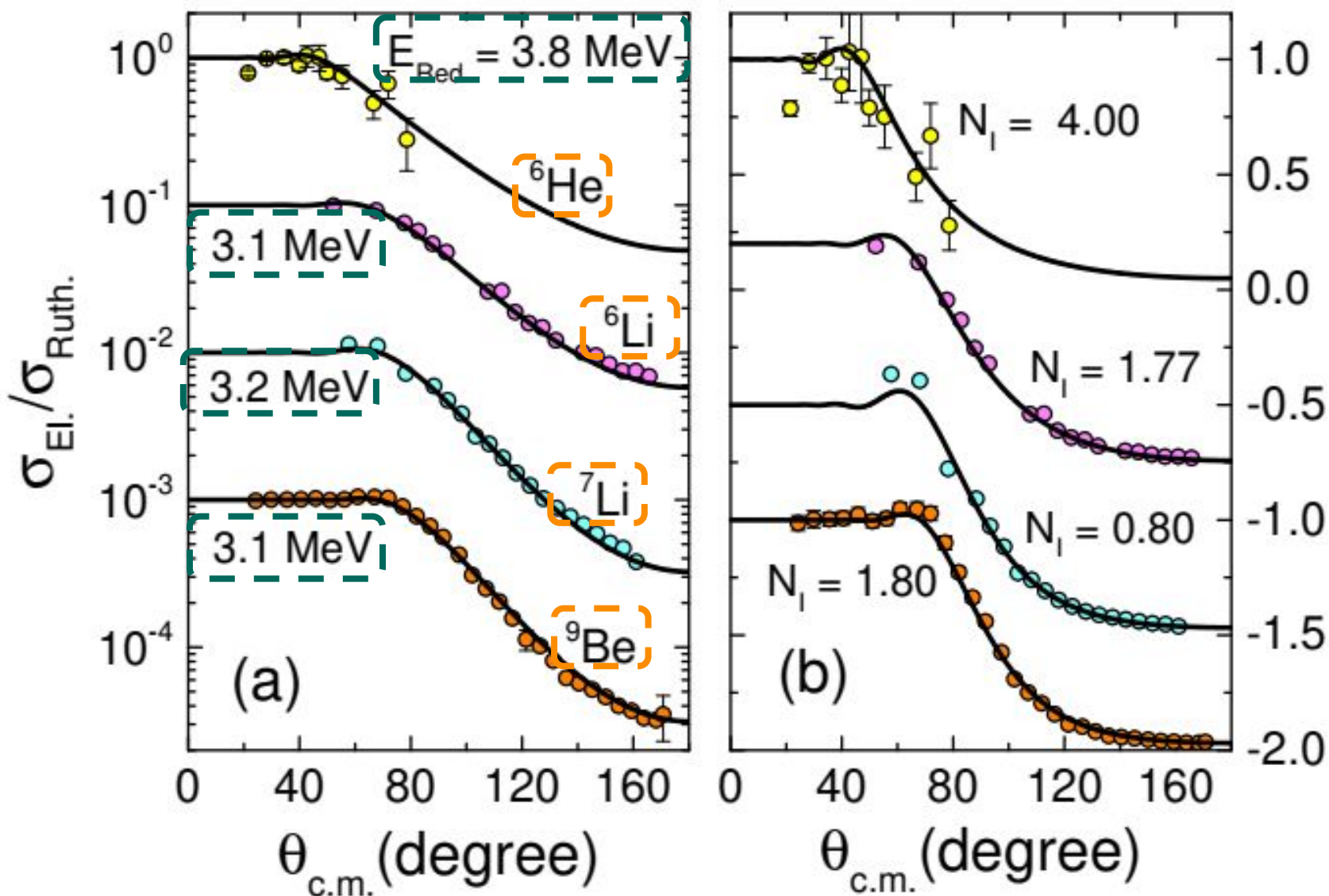
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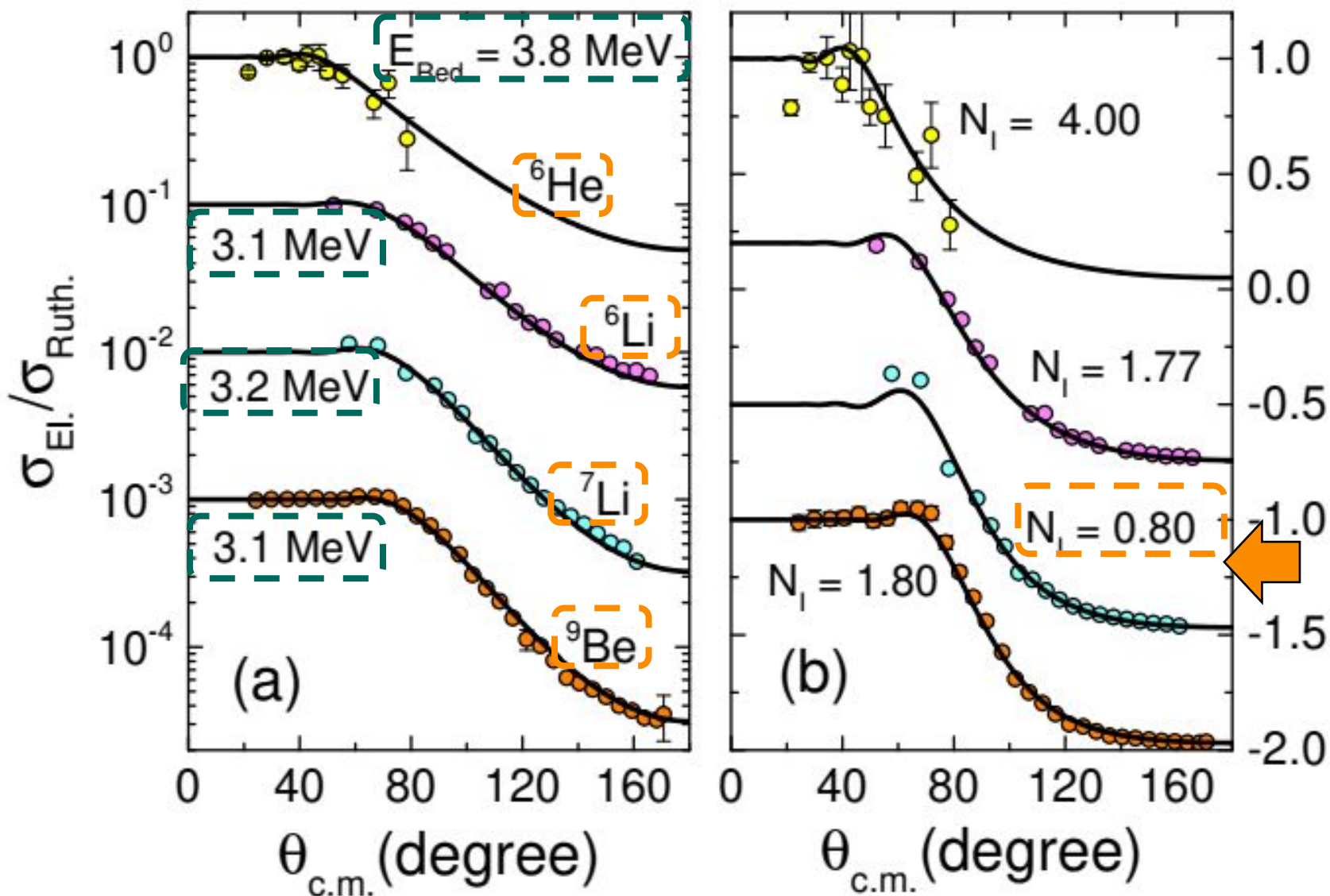
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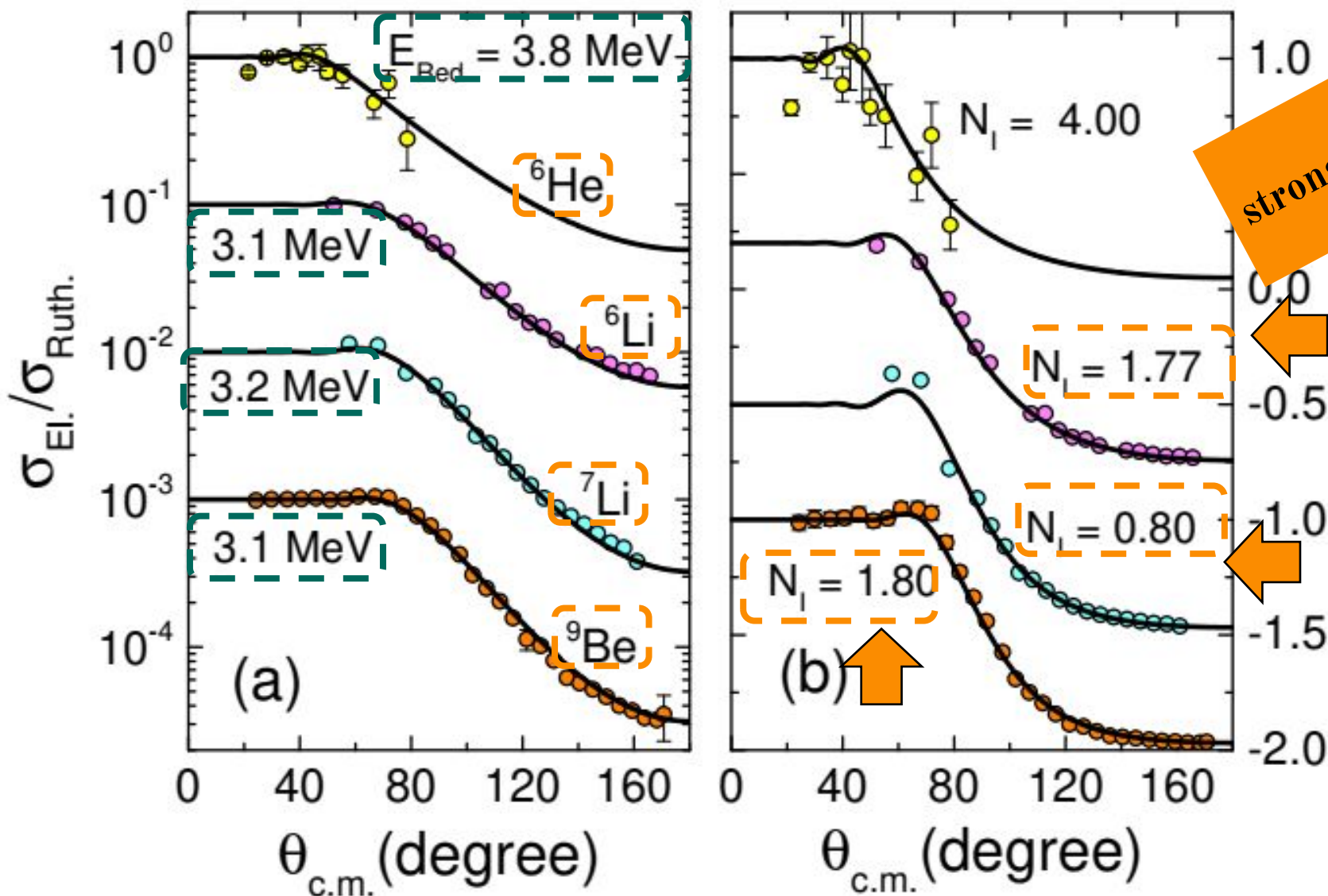
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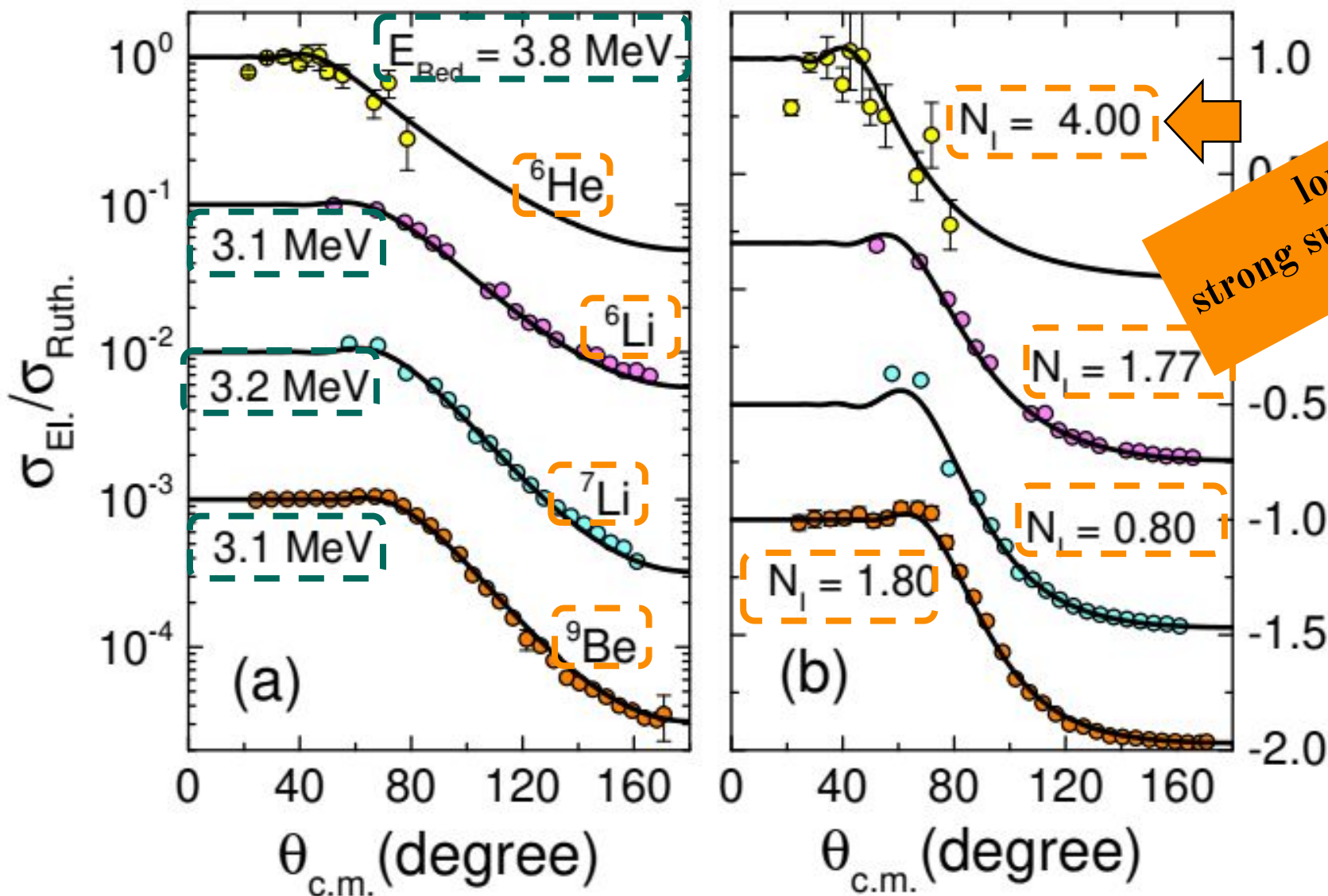


TABLE I. Break-up threshold of light stable and exotic nuclei.

system	cluster	$\varepsilon_b$ (MeV)
$^{11}\text{Li}$	$^9\text{Li}+2\text{n}$	-0.396
$^{11}\text{Be}$	$^{10}\text{Be}+1\text{n}$	-0.501
$^6\text{He}$	$^4\text{He}+2\text{n}$	-0.975
$^6\text{Li}$	$\alpha+\text{d}$	-1.473
$^9\text{Be}$	$^8\text{Be}+1\text{n}$	-1.574
$^9\text{Be}$	$\alpha+\alpha+1\text{n}$	-1.664
$^7\text{Li}$	$\alpha+\text{t}$	-2.467
$^9\text{Li}$	$^7\text{Li}+2\text{n}$	-4.062
$^{10}\text{B}$	$^6\text{Li}+\alpha$	-4.461
$^{18}\text{O}$	$^{14}\text{C}+\alpha$	-6.228
$^{16}\text{O}$	$^{12}\text{C}+\alpha$	-7.162
$^{12}\text{C}^{g.s.}$	$^8\text{Be}+\alpha$	-7.367
$^{12}\text{C}^{H.s.}$	$^8\text{Be}+\alpha$	-7.653
$^4\text{He}$	$^3\text{He}+1\text{n}$	-20.6

projectile	reaction products	$Q$ (MeV)
$^6\text{Li}$	$^{121}\text{Sn} + \alpha + p$	2.472
$^6\text{Li}$	$^{121}\text{Sb} + \alpha + n$	2.092
$^7\text{Li}$	$^{122}\text{Sn} + \alpha + p$	4.036
$^7\text{Li}$	$^{122}\text{Sb} + \alpha + n$	1.247
$^9\text{Be}$	$^{121}\text{Sn} + \alpha + \alpha$	4.597
$^9\text{Be}$	$^{120}\text{Sn} + ^8\text{Be} + n$	4.505
$^{10}\text{B}$	$^{121}\text{Sn} + 2\alpha + p$	-1.989
$^{10}\text{B}$	$^{121}\text{Sb} + 2\alpha + n$	-2.368

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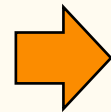


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$^{10}\text{B}$	$^6\text{Li}+\alpha$	-4.461
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$^{12}\text{C}^{H.s.}$	$^8\text{Be}+\alpha$	-7.653
$^4\text{He}$	$^3\text{He}+1n$	-20.6

projectile	reaction products	$Q$ (MeV)
$^6\text{Li}$	$^{121}\text{Sn} + \alpha + p$	2.472
$^6\text{Li}$	$^{121}\text{Sb} + \alpha + n$	2.092
$^7\text{Li}$	$^{122}\text{Sn} + \alpha + p$	4.036
$^7\text{Li}$	$^{122}\text{Sb} + \alpha + n$	1.247
$^9\text{Be}$	$^{121}\text{Sn} + \alpha + \alpha$	4.597
$^9\text{Be}$	$^{120}\text{Sn} + ^8\text{Be} + n$	4.505
$^{10}\text{B}$	$^{121}\text{Sn} + 2\alpha + p$	-1.989
$^{10}\text{B}$	$^{121}\text{Sb} + 2\alpha + n$	-2.368

TABLE I. Break-up threshold of light stable and exotic nuclei.

system	cluster	$\varepsilon_b$ (MeV)
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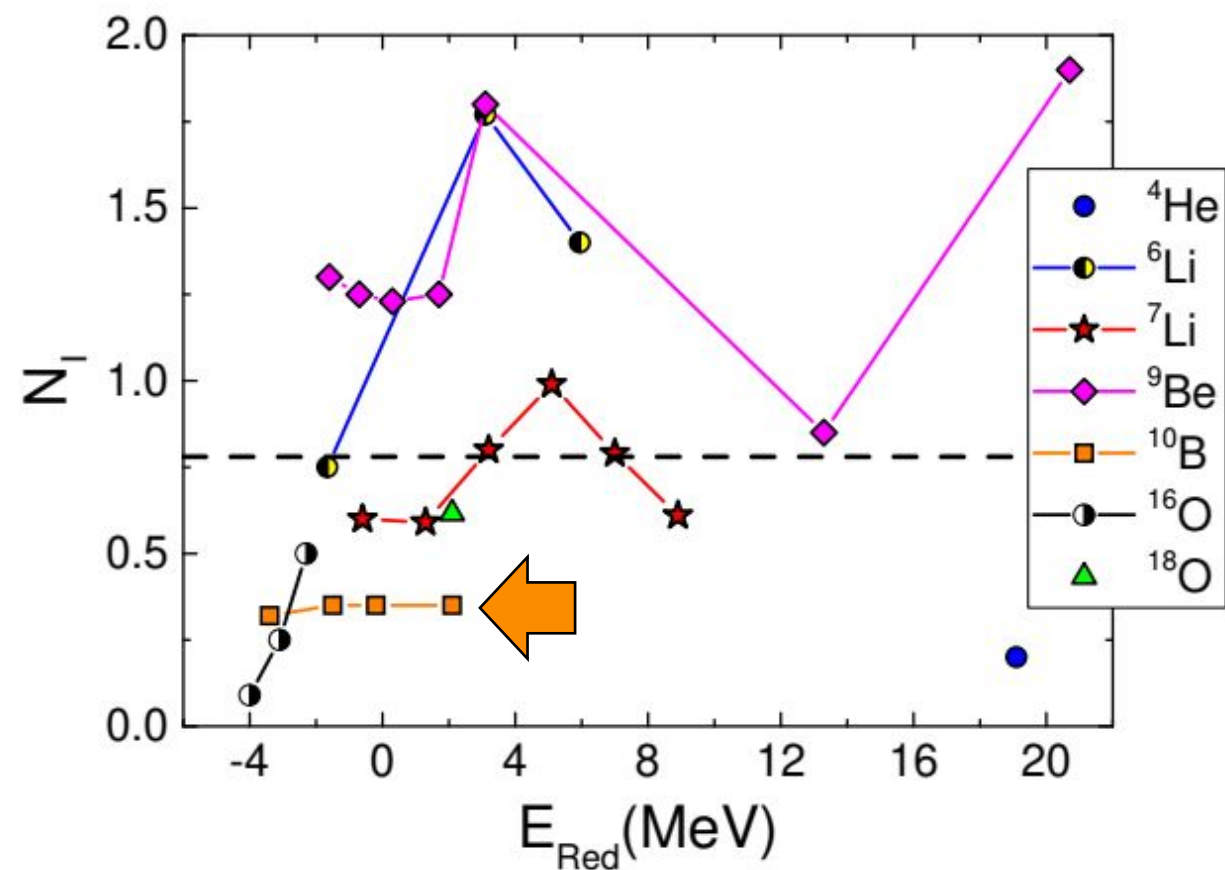


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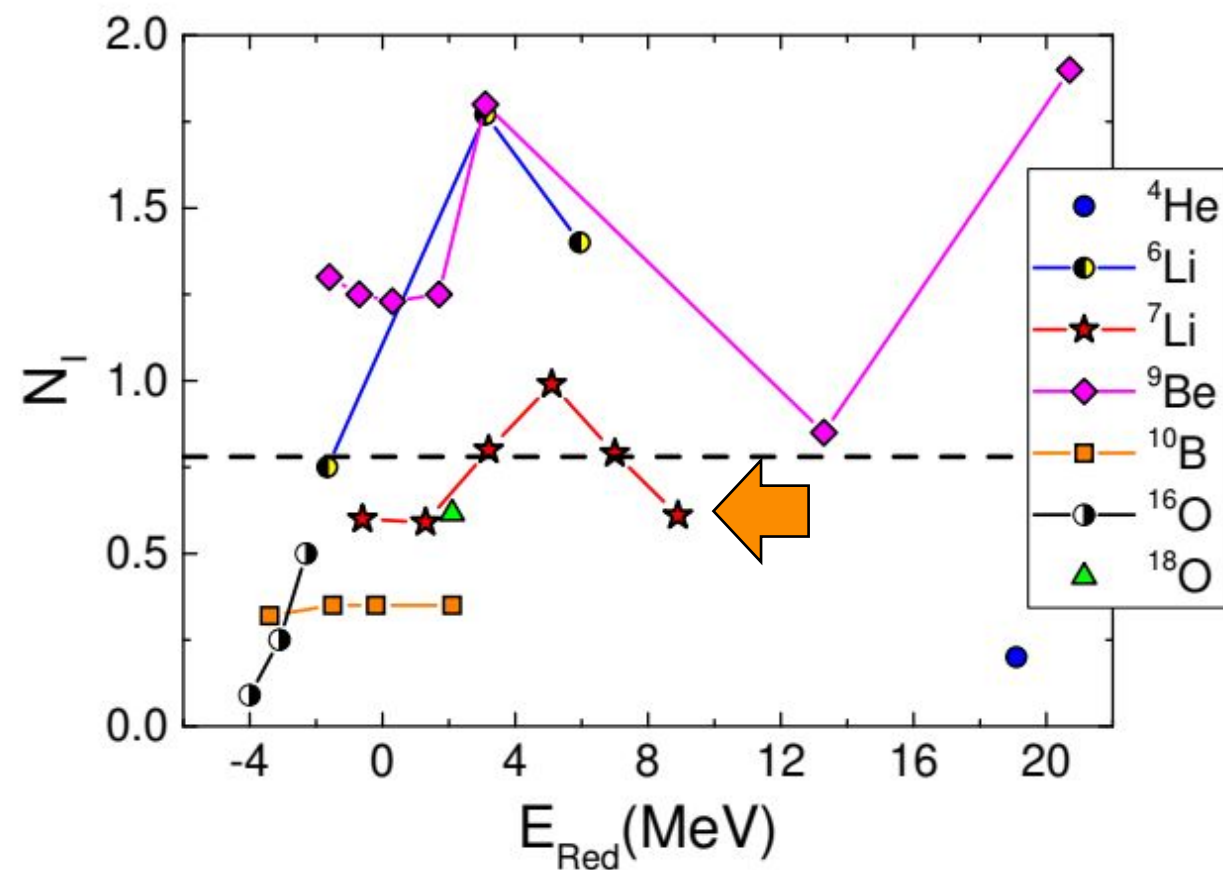


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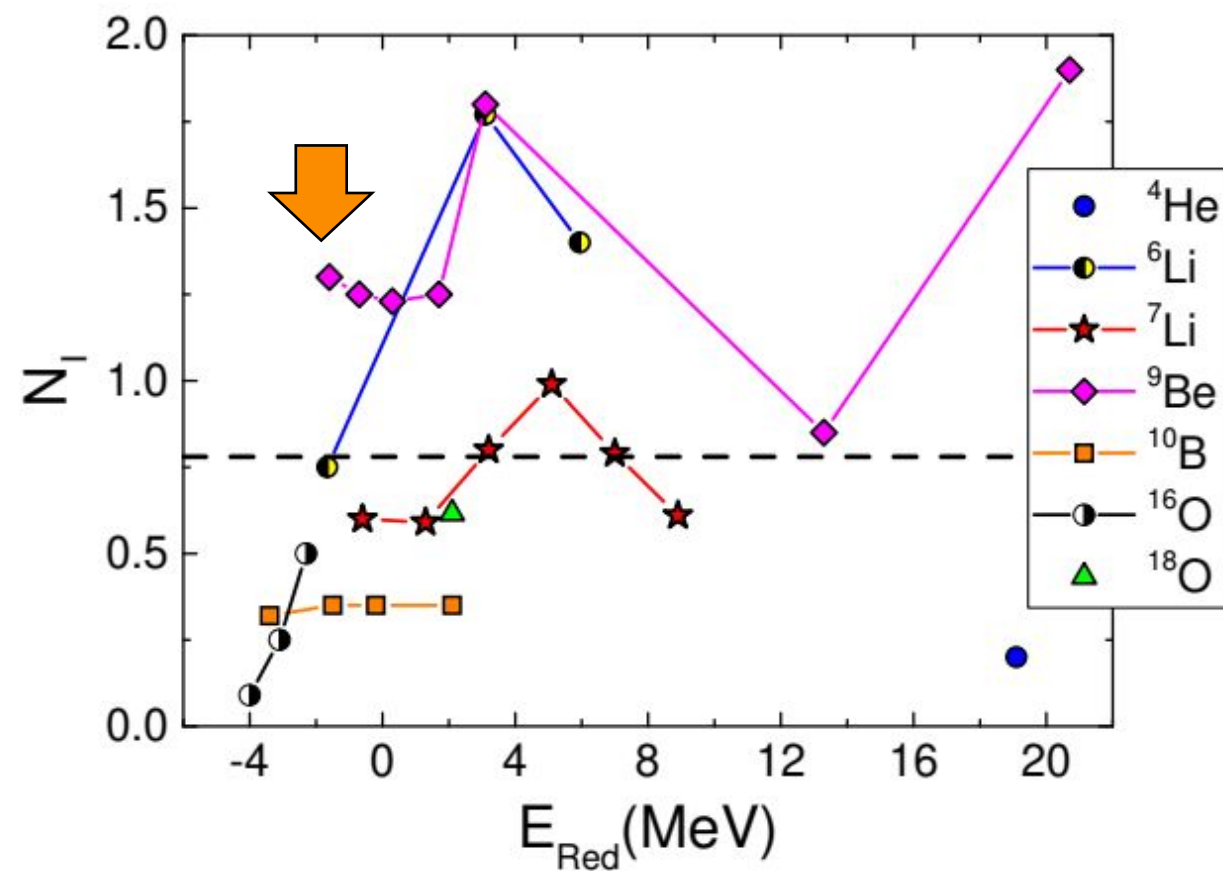


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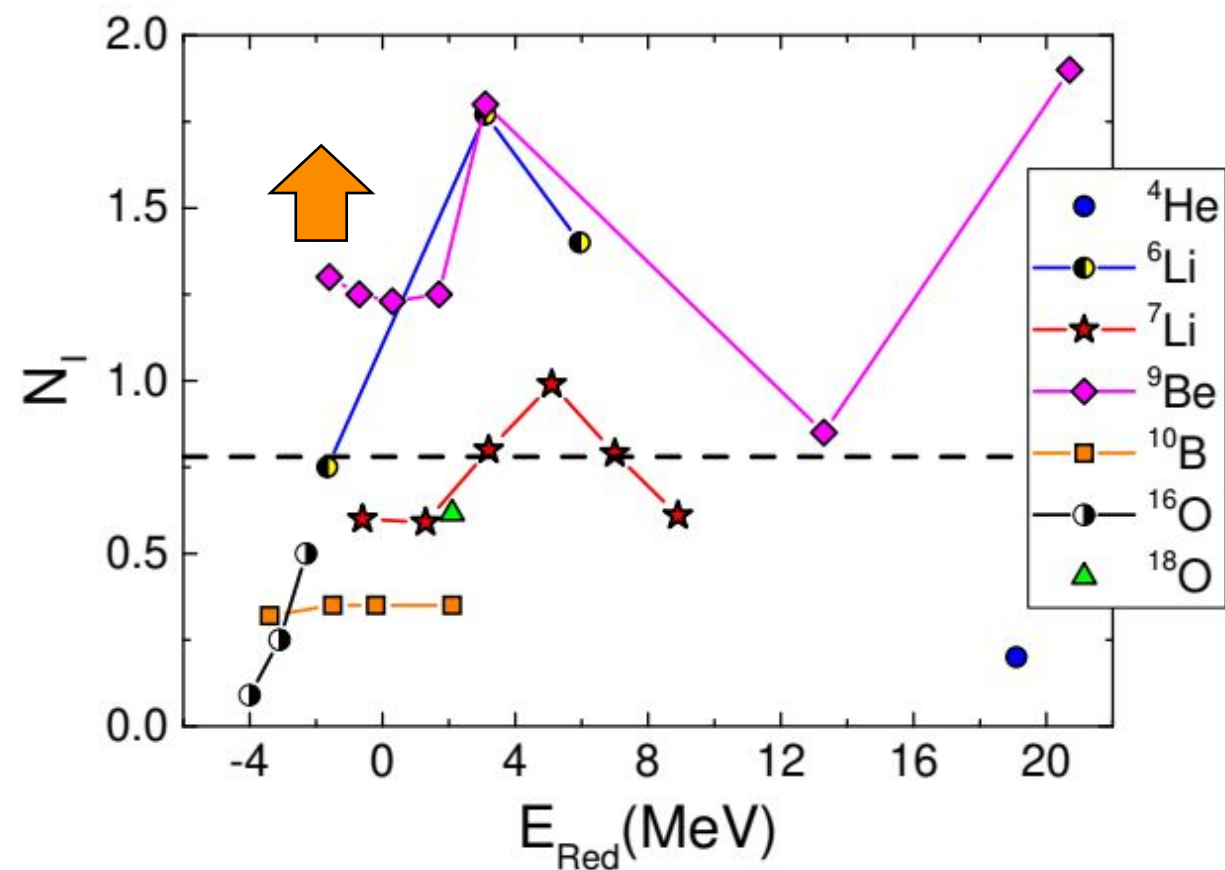




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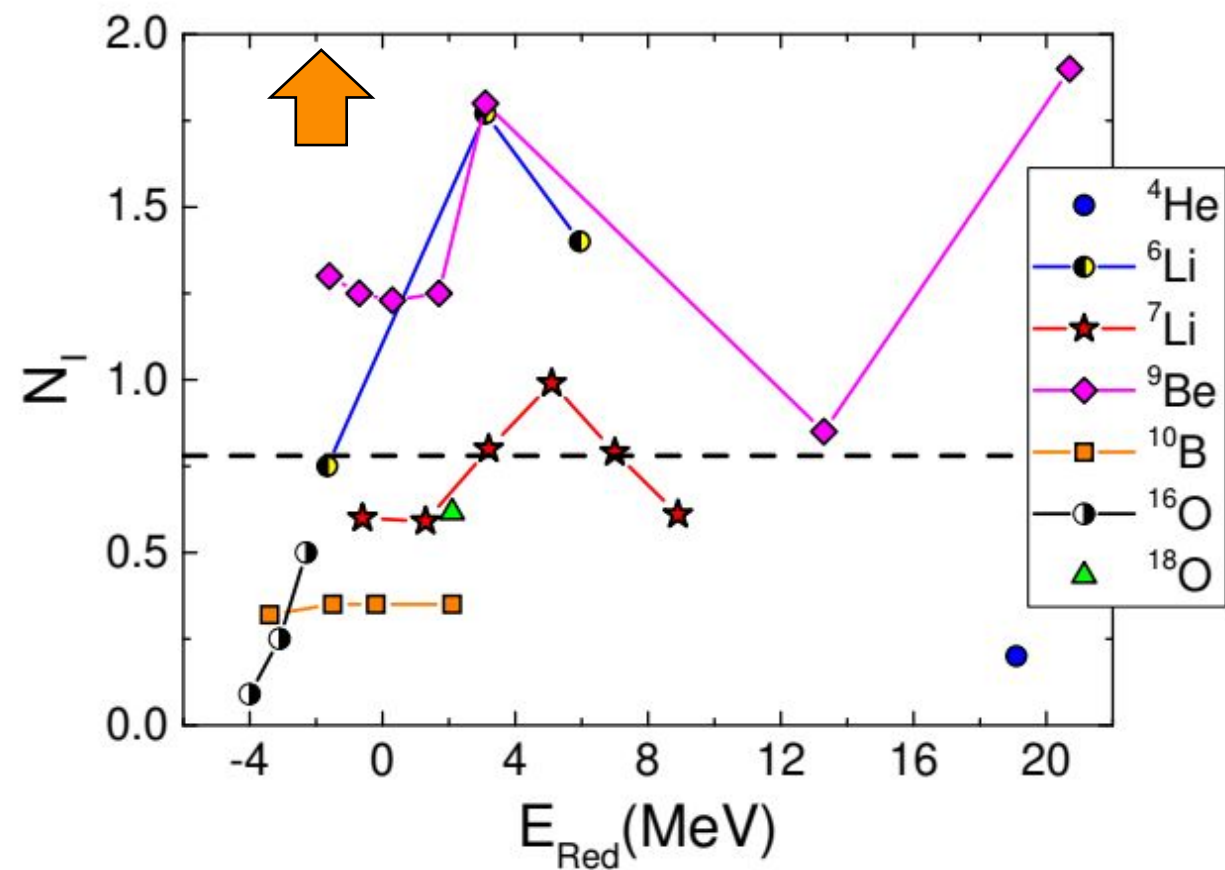


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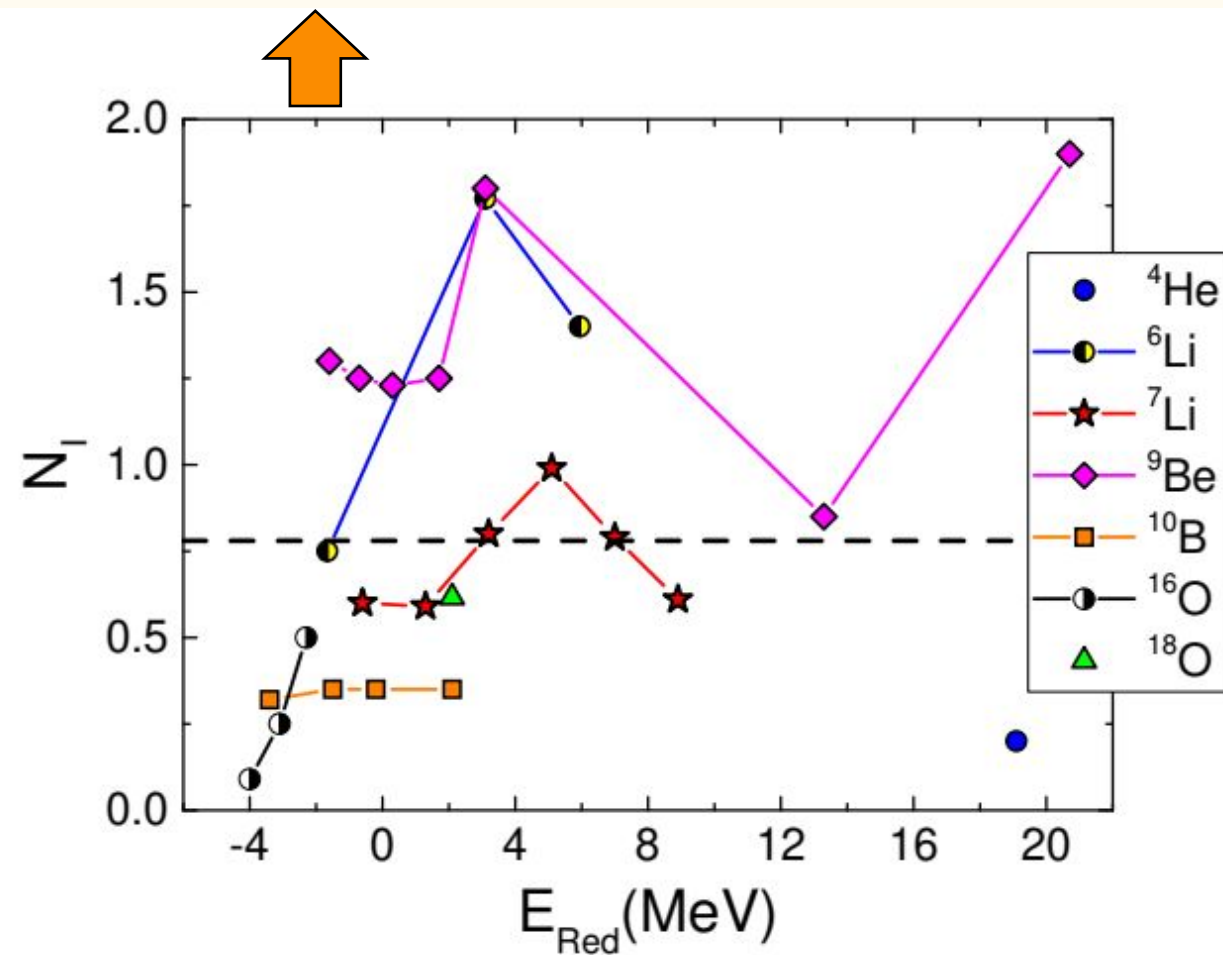
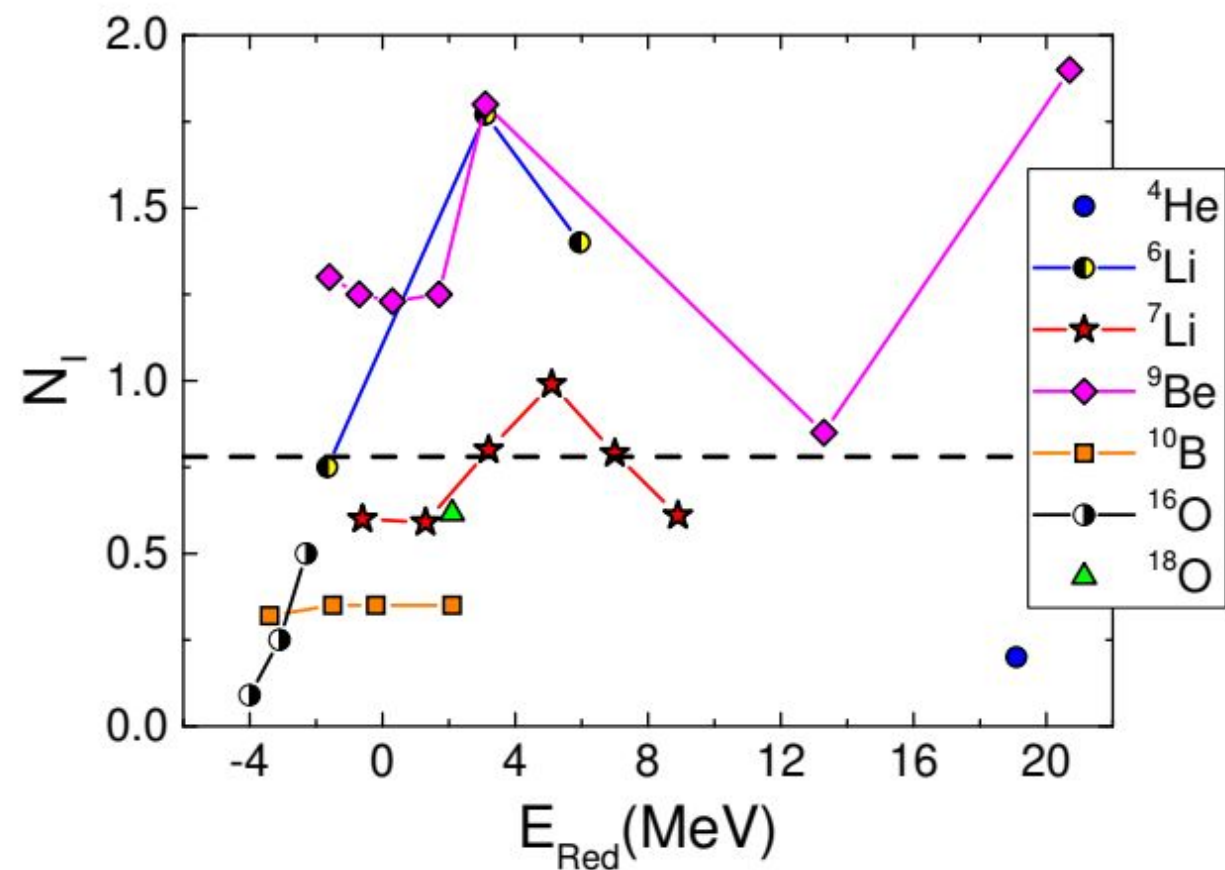
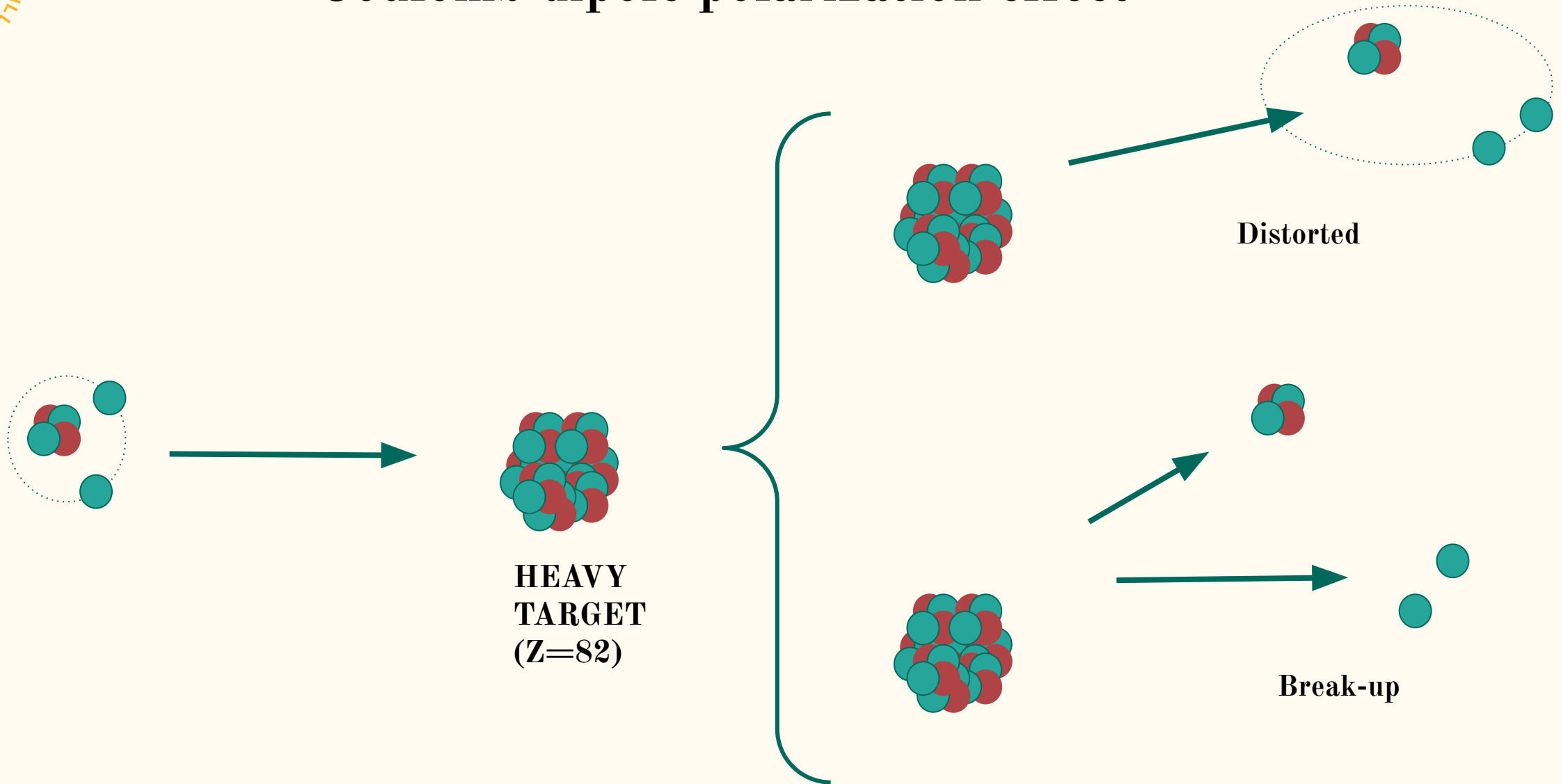


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# Coulomb dipole polarization effect



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A simple analytical formula for the **Coulomb dipole polarization (CDP)** potential was derived in:

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$$U_{pol} = -\frac{4\pi}{9} \frac{Z_t^2}{\hbar v} \frac{1}{(r - a_0)^2 r} \int_{\varepsilon_b}^{\infty} d\varepsilon \frac{dB(E1, \varepsilon)}{d\varepsilon} \left( g\left(\frac{r}{a_0} - 1, \xi\right) + if\left(\frac{r}{a_0} - 1, \xi\right) \right)$$

$\frac{dB(E1)}{d\varepsilon}$  is the probability distribution of the dipolar electric transition;

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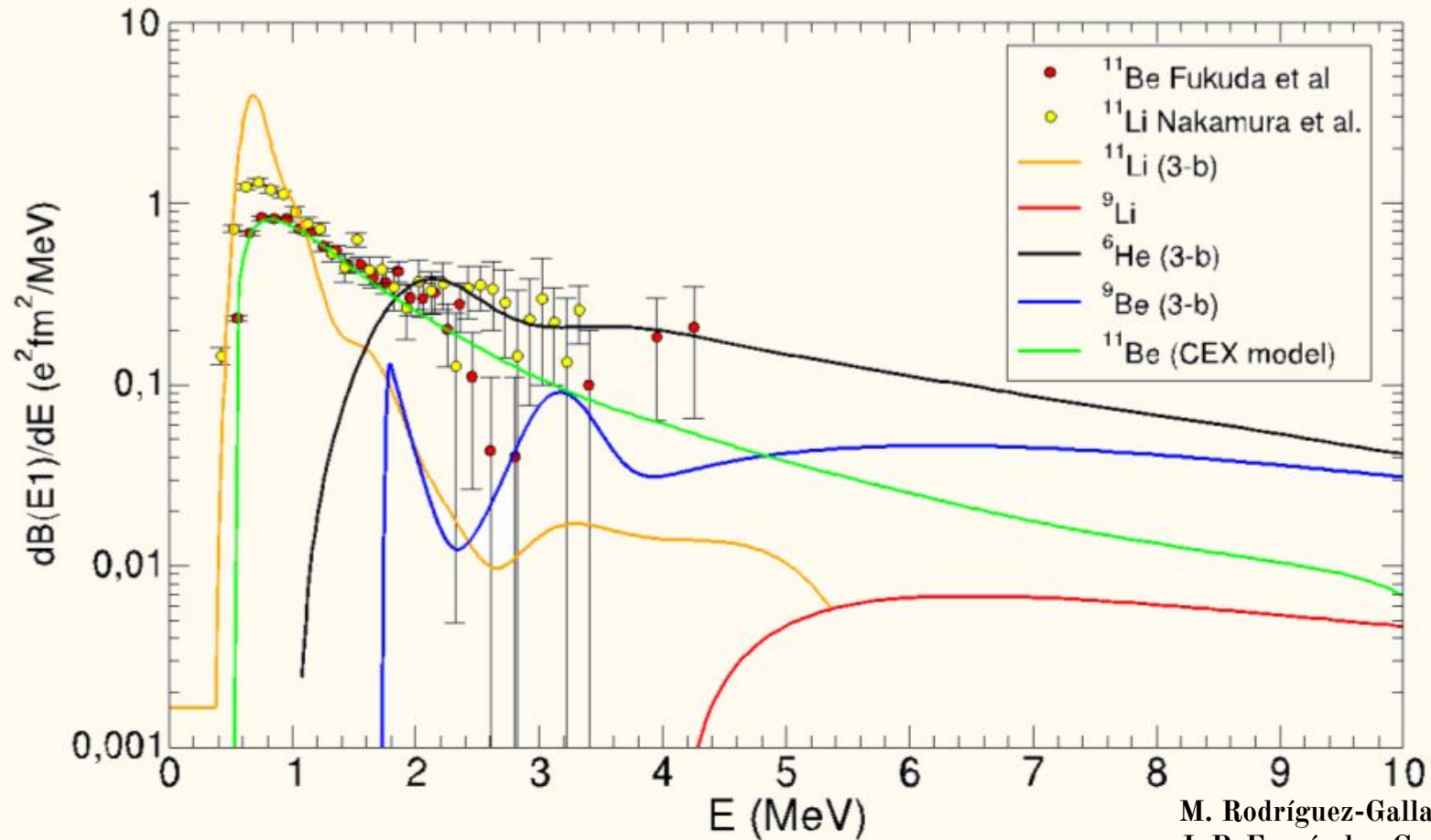
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## Experimental and theoretical $B(E1)$ distributions



M. Rodríguez-Gallardo *et al.*, PRC 80, 051601 (R) (2009).  
 J. P. Fernández-García *et al.* PRL 110, 142701 (2013).  
 T. Nakamura *et al.*, Phys. Rev. Lett. 96, 252502 (2006).  
 N. Fukuda *et al.*, Phys. Rev. C 70, 054606 (2004).




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**nuclear potential**

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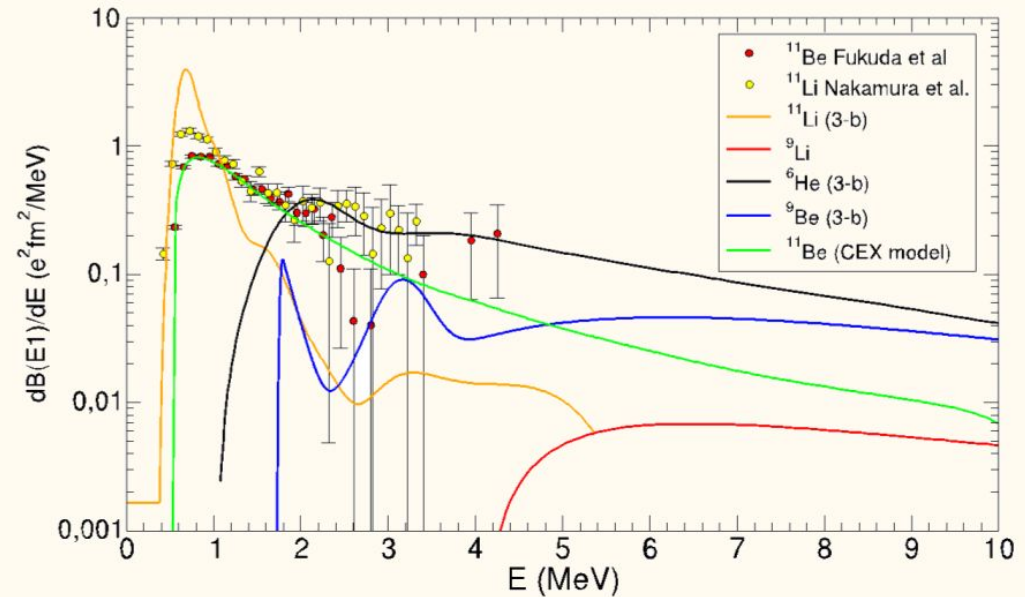
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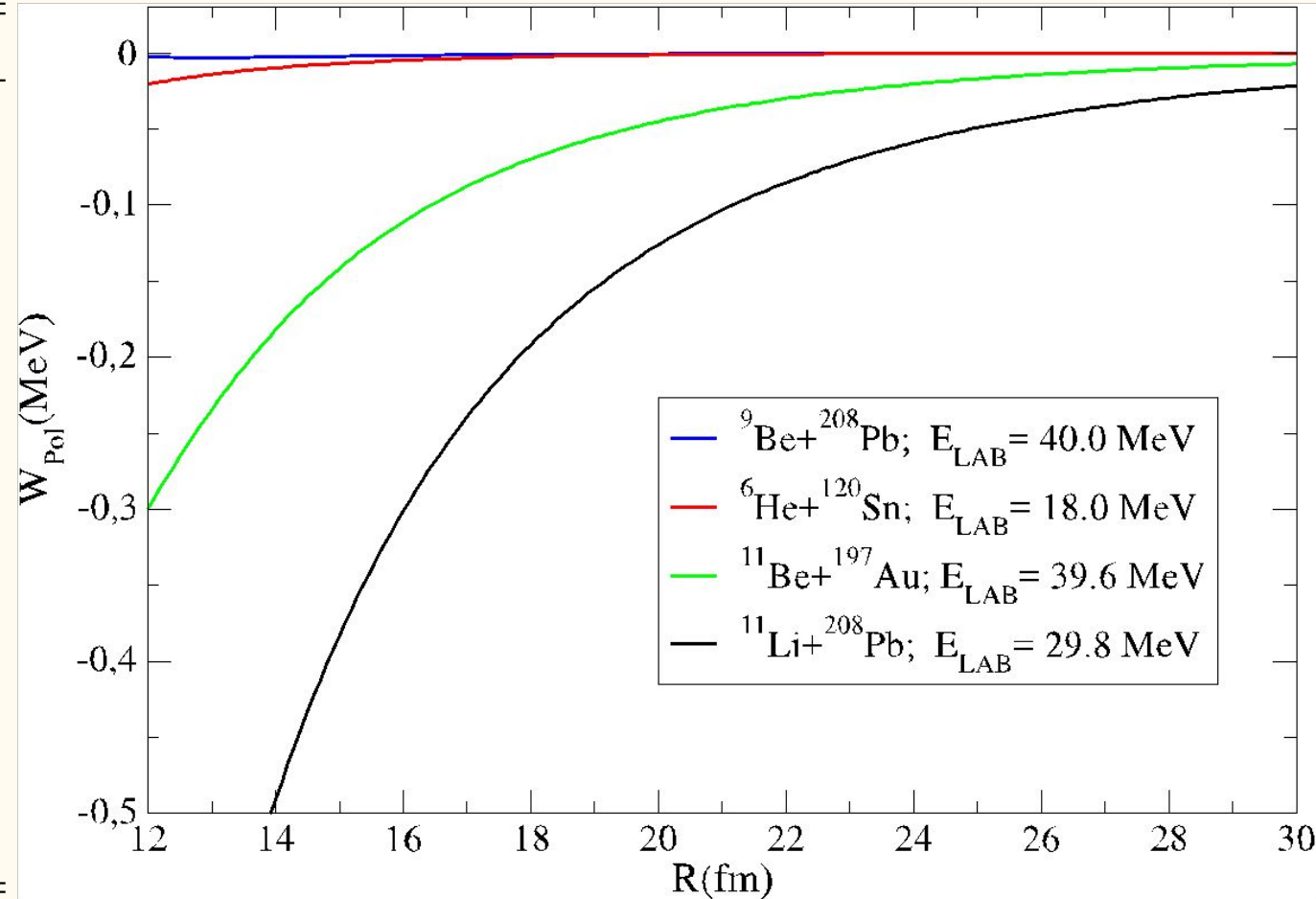


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studying the intensity of  
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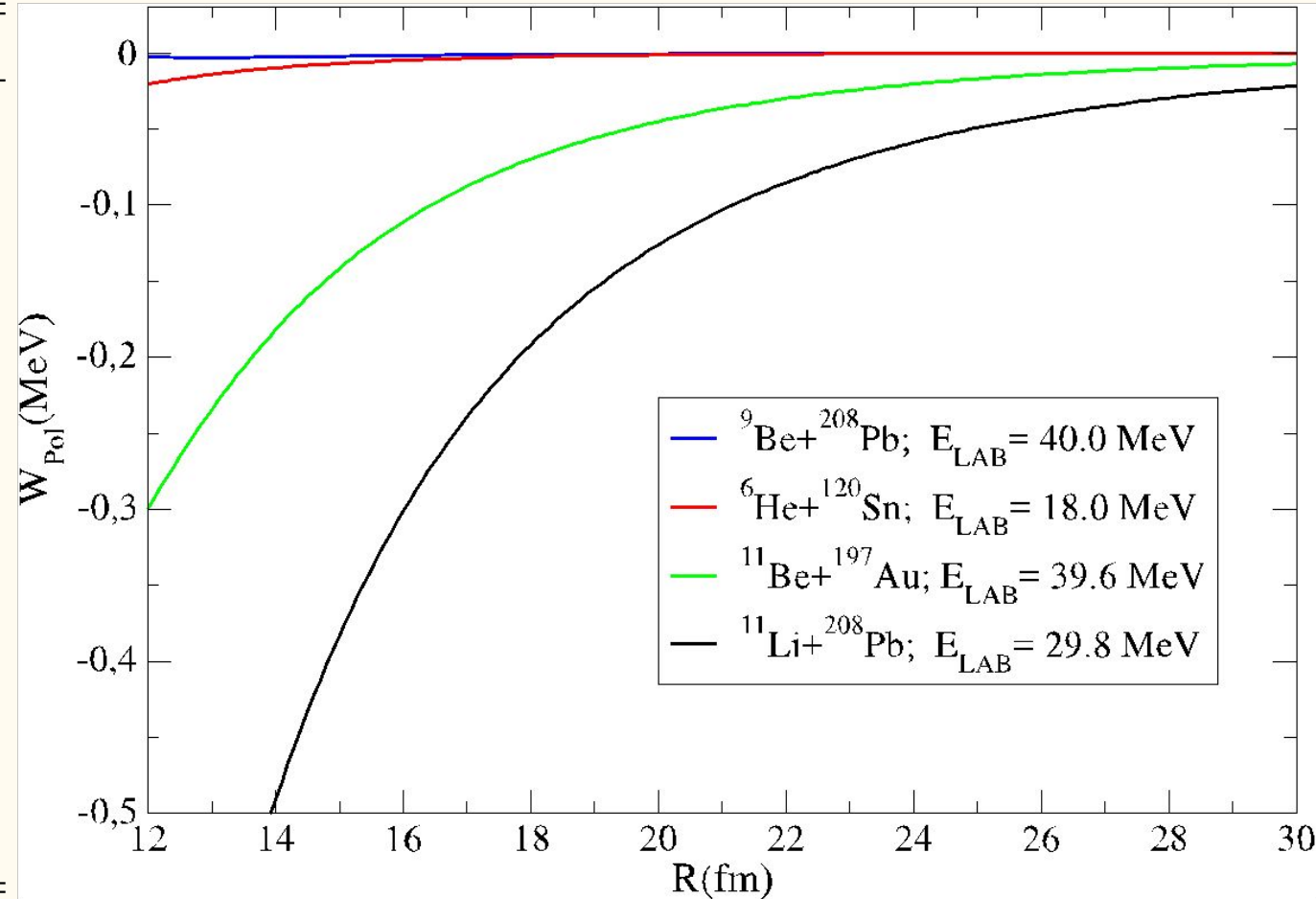


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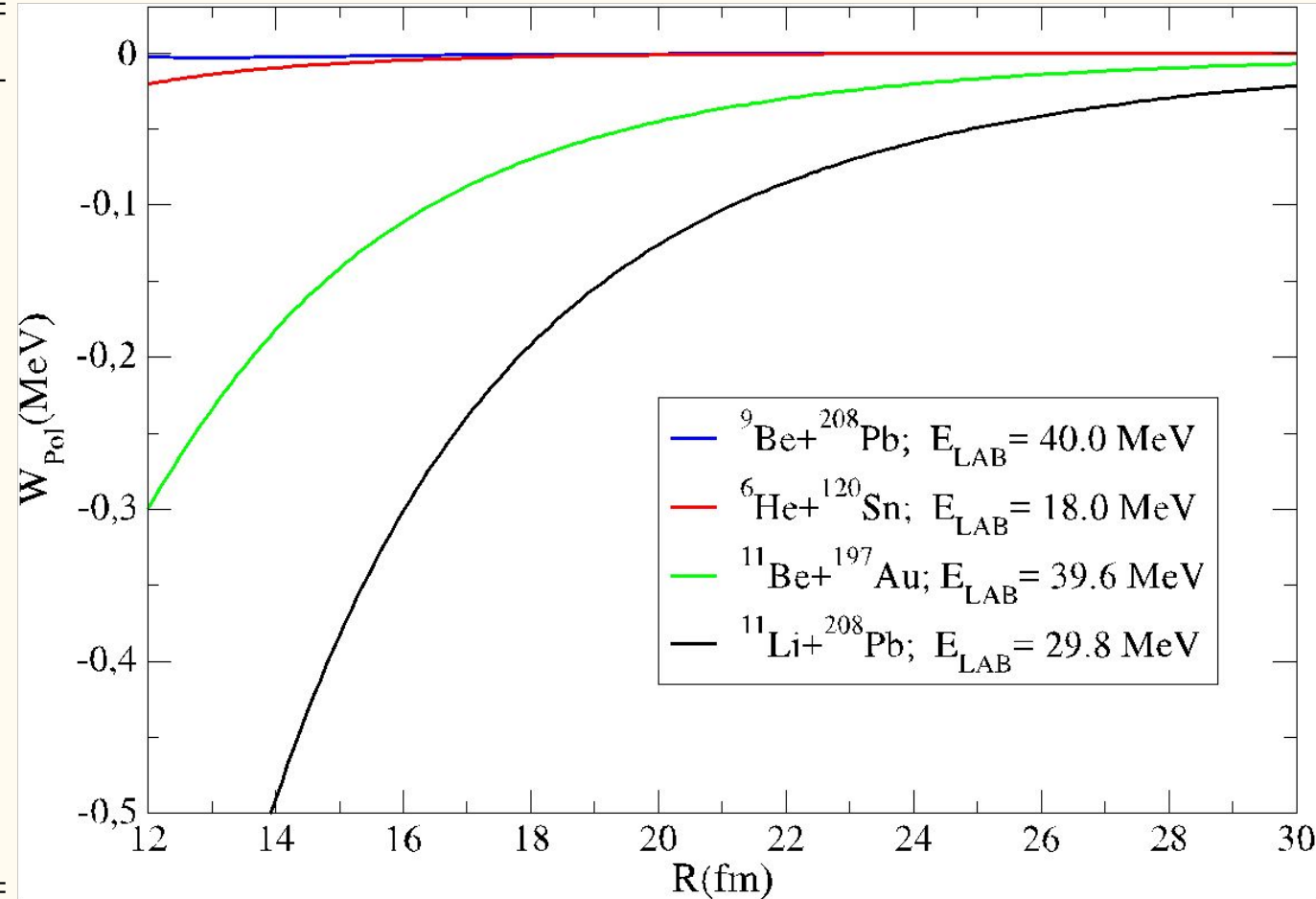


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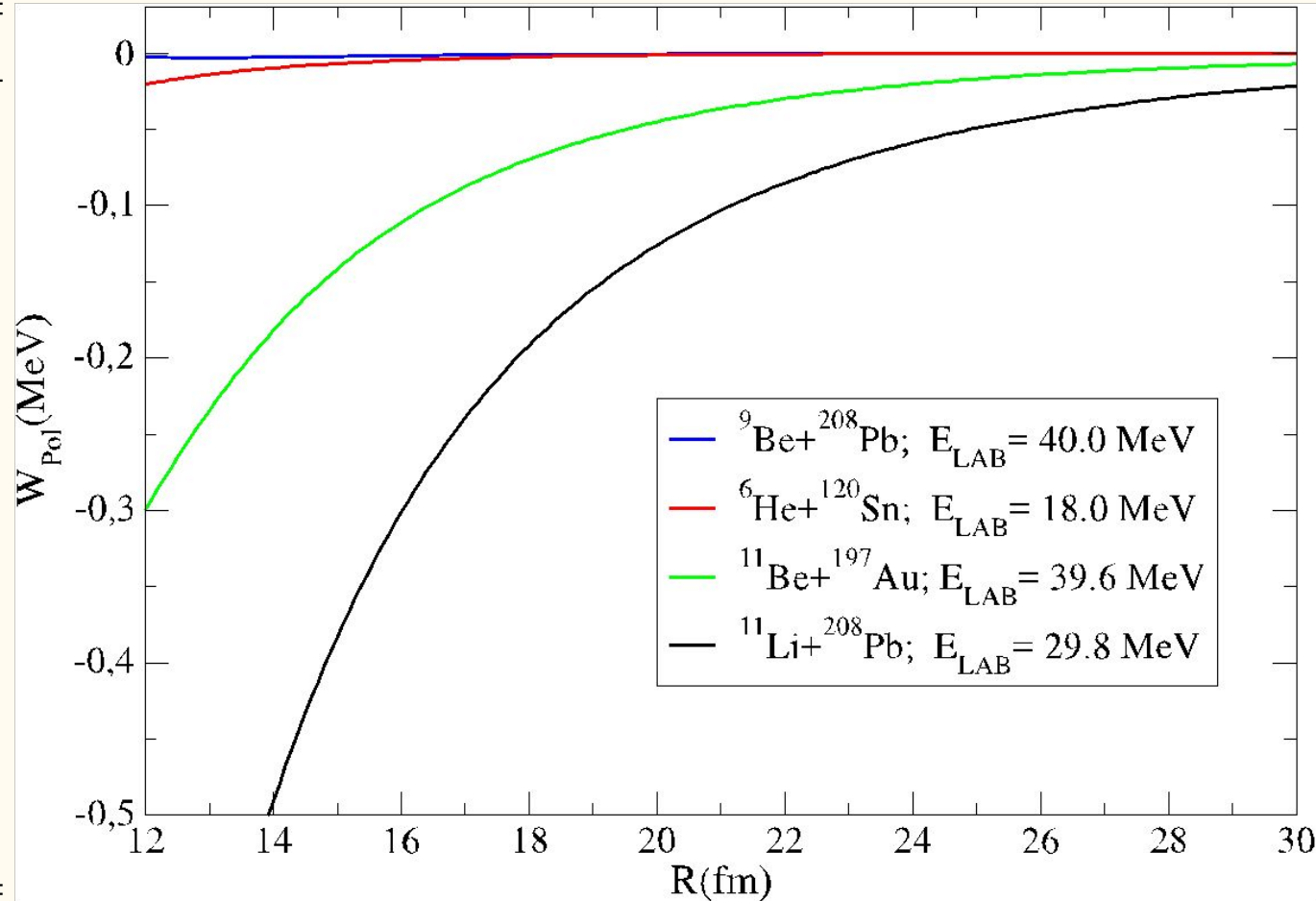


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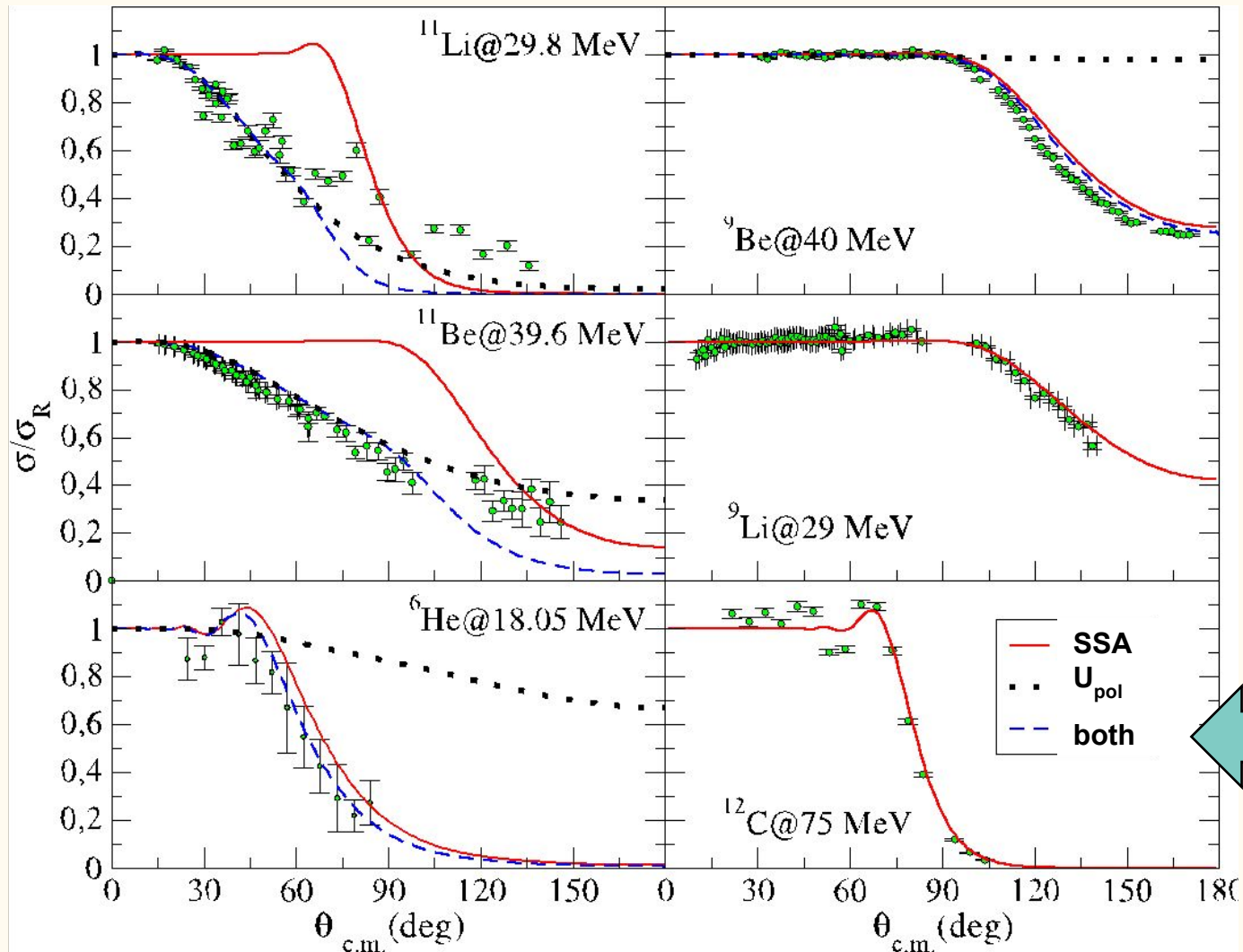
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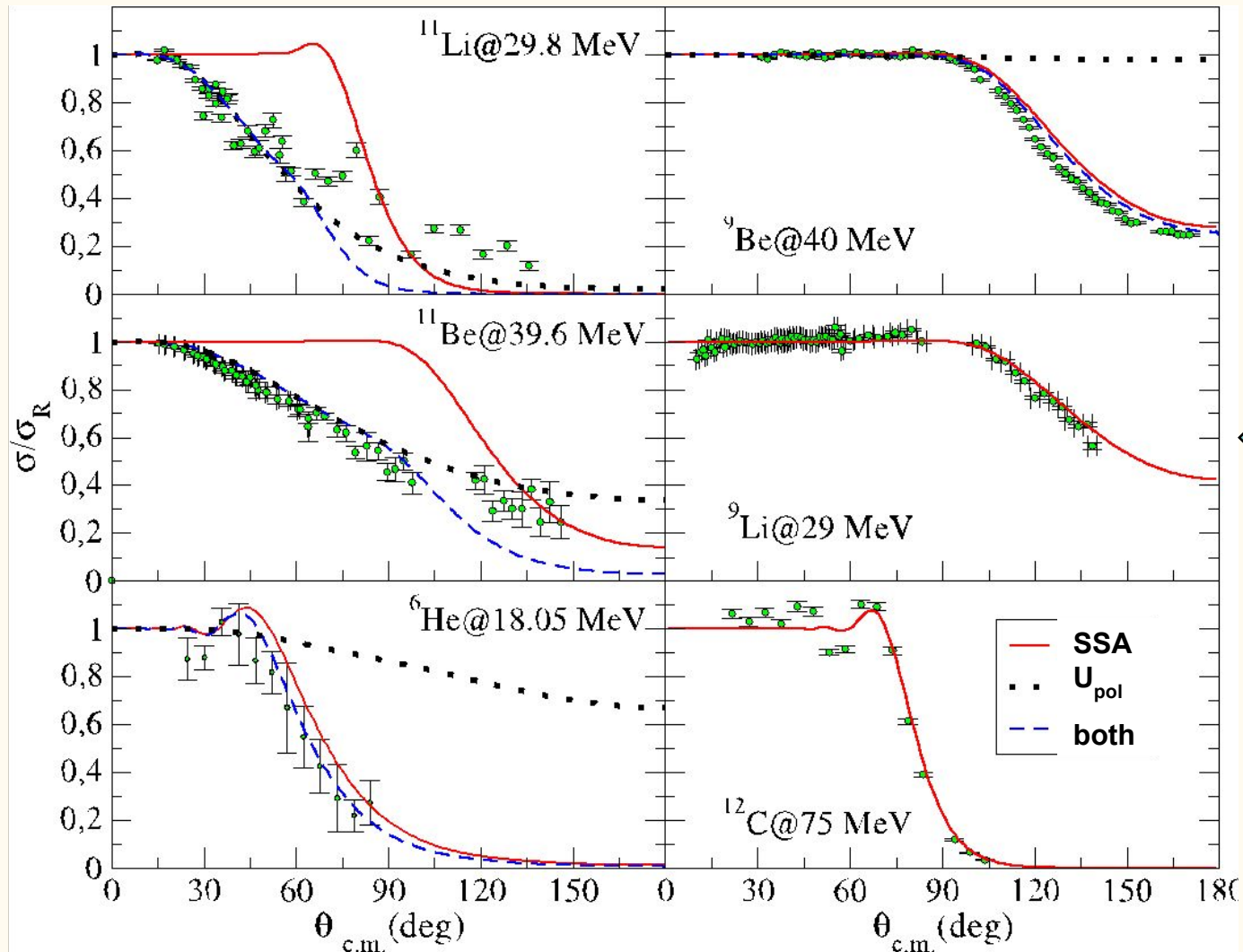
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←  $^{12}\text{C} + ^{208}\text{Pb}$

# Coulomb dipole polarization effect

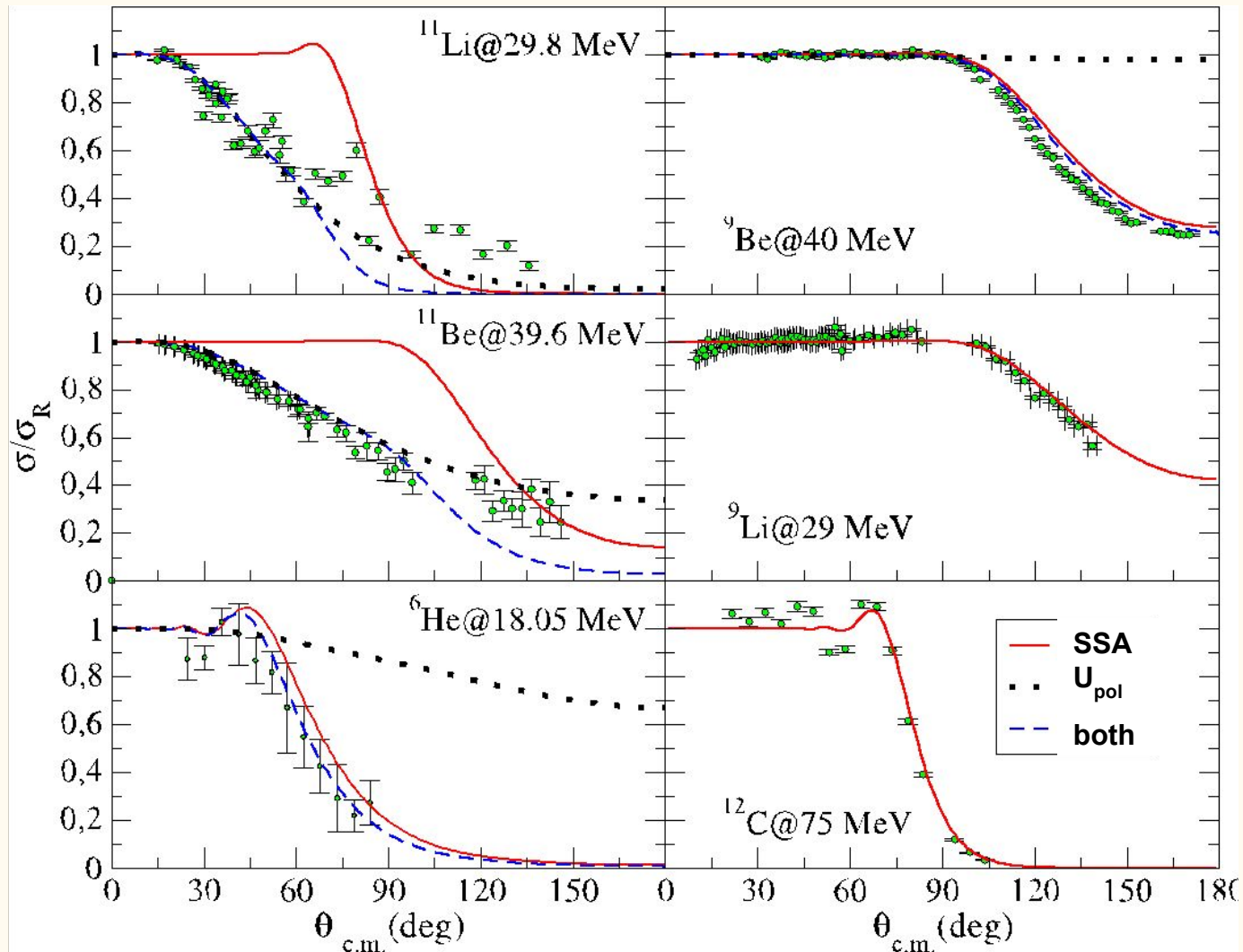
$$U_{opt}(R) = \boxed{V_{SPP}(R) + iN_I V_{SPP}(R)} + \dot{V}_{pol}(R) + i\dot{W}_{pol}(R)$$



←  $^9\text{Li} + ^{208}\text{Pb}$

# Coulomb dipole polarization effect

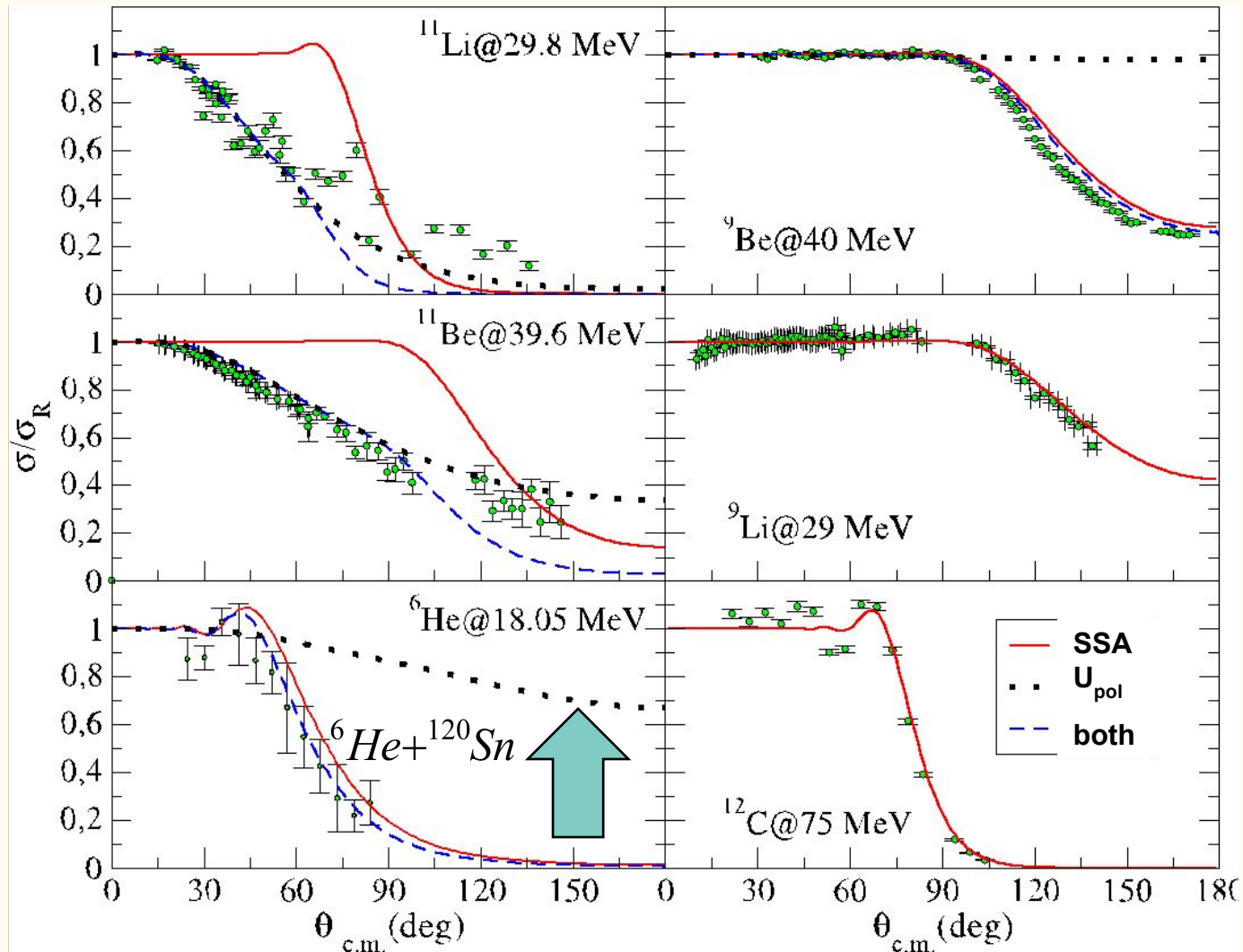
$$U_{opt}(R) = \boxed{V_{SPP}(R) + iN_I V_{SPP}(R)} + \dot{V}_{pol}(R) + i\dot{W}_{pol}(R)$$



←  ${}^9\text{Be} + {}^{208}\text{Pb}$

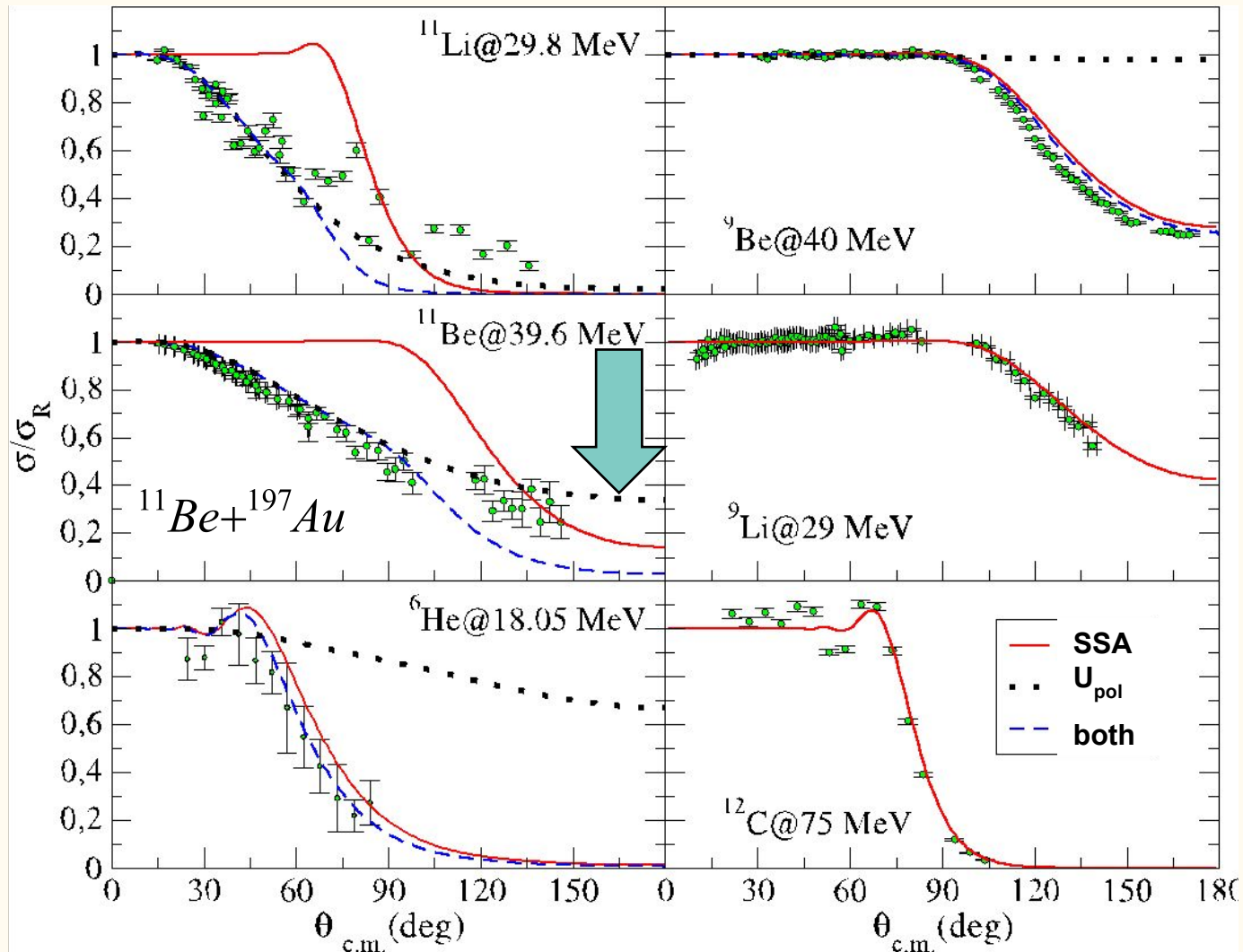
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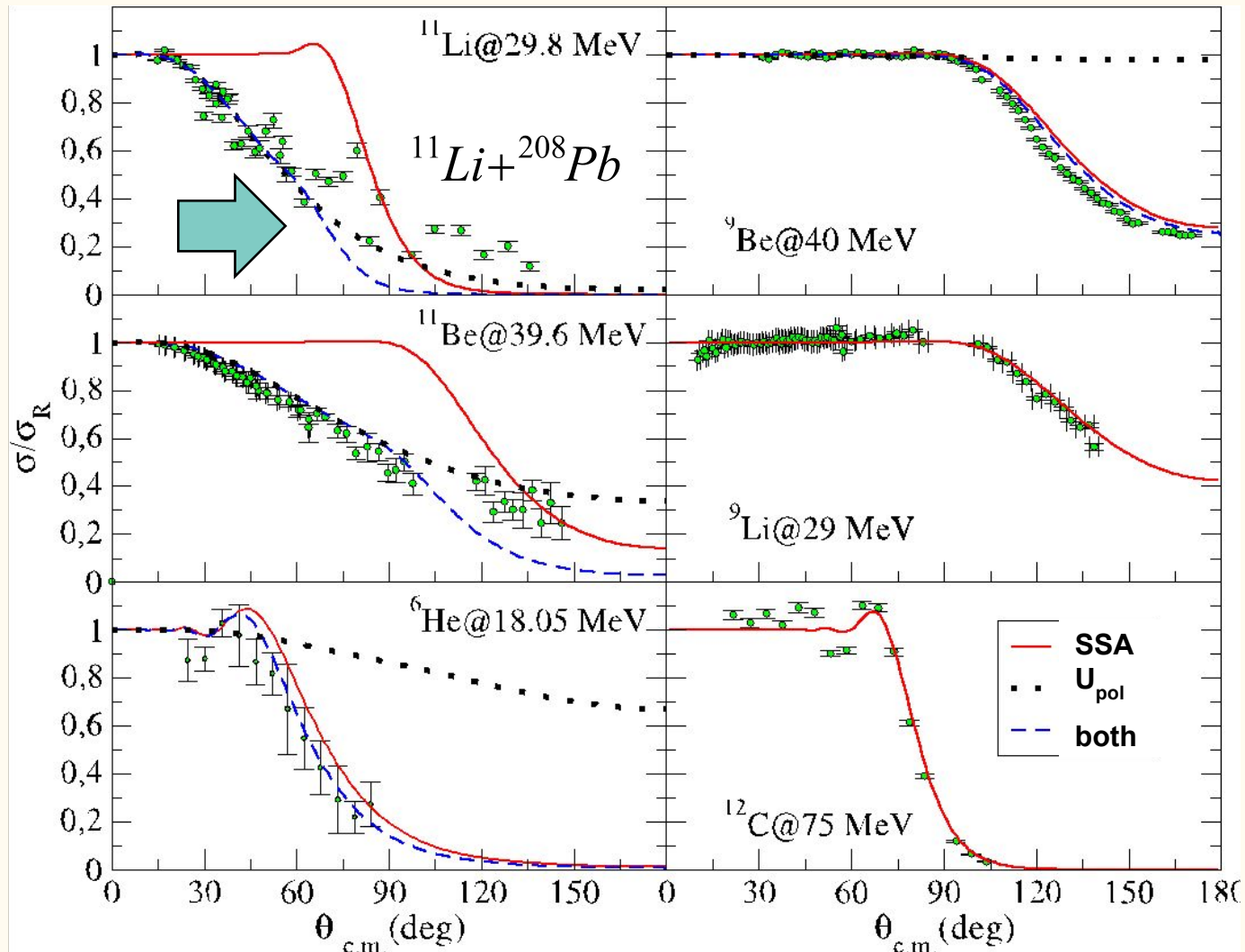
# Coulomb dipole polarization effect

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# Coulomb dipole polarization effect

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- 1. The Laboratories and SETUP's**
- 2. The Theoretical Optical Model**
- 3. Experimental Data x Theoretical Calculations**
- 4. Conclusions**

## CONCLUSIONS:




- ❑ We work on an international network based on using pelletron-tandem facilities.
- ❑ We have analysed 40 elastic scattering angular distributions of stable strongly bound, weakly bound and exotic nuclei, mainly on  $^{120}\text{Sn}$ , at energies below, around and above the Coulomb barriers.
- ❑ We have analysed them with an OP based on the nuclear São Paulo Potential, allowing the most sensitive parameter to vary, which showed to be strongly connected to the projectile binding energy.
- ❑ Within this context, we have also showed the importance of the Coulomb dipole polarization potential, derived from the semi-classical theory of Coulomb excitation.
- ❑ We identified the evolution of *long-range absorption* as a function of the projectile binding energy, which, for more exotic nuclei, is dominated by the Coulomb interaction.
- ❑ The proposed approach shows to be a fundamental basis to study any nuclear reaction.



## Systematic study of optical potential strengths in reactions on $^{120}\text{Sn}$ involving strongly bound, weakly bound, and exotic nuclei

M. A. G. Alvarez , J. P. Fernández-García , and J. L. León-García  
*Departamento FAMN, Universidad de Sevilla, Apartado 1065, 41080 Sevilla, Spain*

M. Rodríguez-Gallardo  
*Departamento FAMN, Universidad de Sevilla, Apartado 1065, 41080 Sevilla, Spain  
and Instituto Carlos I de Física Teórica y Computacional, Universidad de Sevilla, Spain*

L. R. Gasques , L. C. Chamon , V. A. B. Zagatto, A. Lépine-Szily, and J. R. B. Oliveira   
*Universidade de Sao Paulo, Instituto de Física, Rua do Matao, 1371, 05508-090 Sao Paulo, SP, Brazil*

V. Scarduelli  
*Instituto de Física, Universidade Federal Fluminense, 24210-340 Niterói, Rio de Janeiro, Brazil  
and Instituto de Física da Universidade de São Paulo, 05508-090 São Paulo, SP, Brazil*

B. V. Carlson  
*Departamento de Física, Instituto Tecnológico de Aeronáutica, São José dos Campos, SP, Brazil*

J. Casal  
*Dipartimento di Fisica e Astronomia "G. Galilei" and INFN-Sezione di Padova, Via Marzolo, 8, I-35131 Padova, Italy*

A. Arazi  
*Laboratorio TANDAR, Comisión Nacional de Energía Atómica, Av. Gral. Paz 1499, BKNA1650 San Martín, Argentina*

D. A. Torres  and F. Ramirez   
*Departamento de Física, Universidad Nacional de Colombia, Bogotá, Colombia*

## RECENT PUBLICATIONS:

- ❑ **Physical Review C 101, 044604 (2020)**
- ❑ **Physical Review C 101, 044601 (2020)**
- ❑ **Physical Review C 100, 064602 (2019)**
- ❑ **Physical Review C 99, 054605 (2019)**
- ❑ **Physical Review C 99, 064617 (2019)**
- ❑ **Physical Review C 99, 014601 (2019)**
- ❑ **Physical Review C 98, 064601 (2018)**
- ❑ **Physical Review C 98, 034615 (2018)**
- ❑ **Physical Review C 98, 024621 (2018)**
- ❑ **Physical Review C 97, 034629 (2018)**
- ❑ **Physical Review C 95, 064614 (2017)**

**THANK YOU FOR YOUR  
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